

Example: Conway's Game of Life

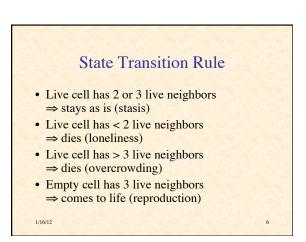
- Invented by Conway in late 1960s
- A simple CA capable of universal computation
- Structure:

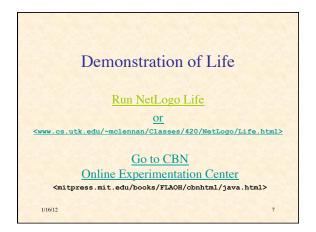
CA

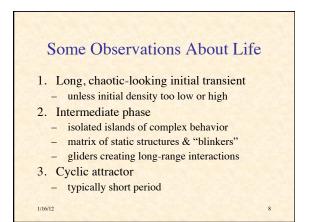
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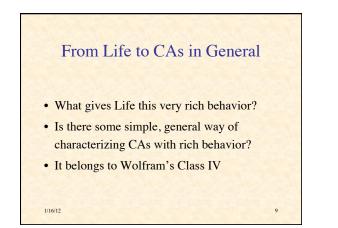
- 2D space
- rectangular lattice of cells
- binary states (alive/dead)
- neighborhood of 8 surrounding cells (& self)
- simple population-oriented rule

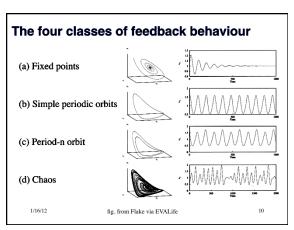
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Wolfram's Classification

- Class I: evolve to fixed, homogeneous state ~ limit point
- Class II: evolve to simple separated periodic structures
 - ~ limit cycle

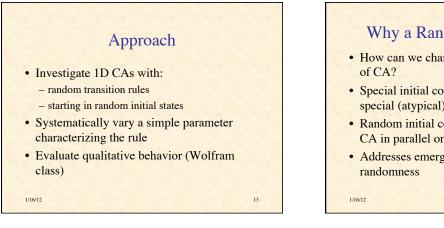
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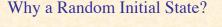
- Class III: yield chaotic aperiodic patterns
 ~ strange attractor (chaotic behavior)
- Class IV: complex patterns of localized structure ~ long transients, no analog in dynamical systems

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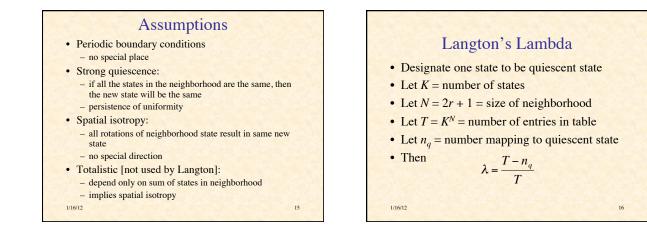
Langton's Investigation Under what conditions can we expect a complex dynamics of information to emerge spontaneously and come to dominate the behavior of a CA?

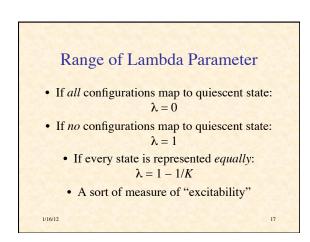
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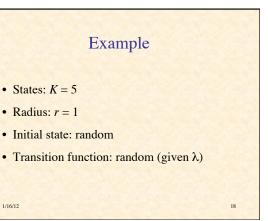


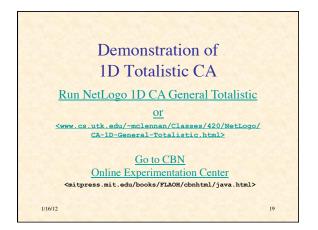


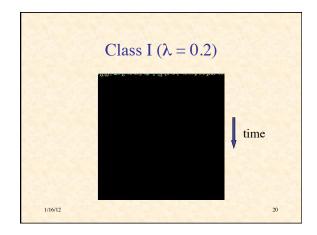
- How can we characterize typical behavior of CA?
- Special initial conditions may lead to special (atypical) behavior
- Random initial condition effectively runs CA in parallel on a sample of initial states
- Addresses emergence of order from randomness

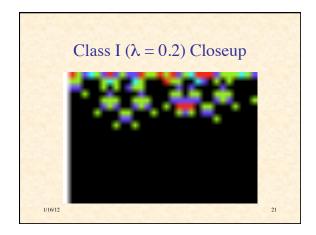


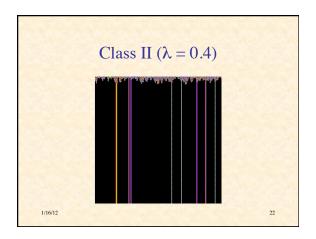


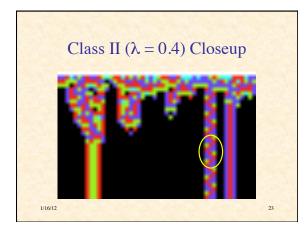


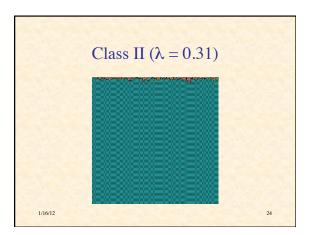


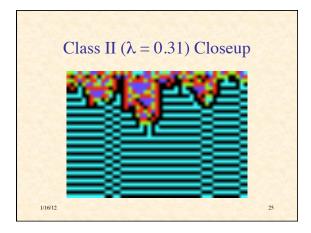


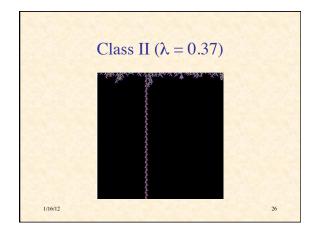


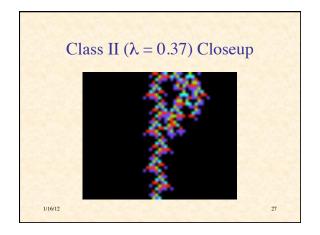


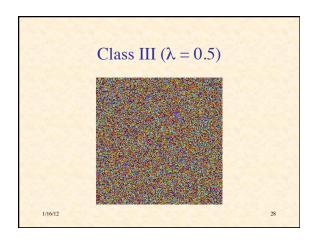


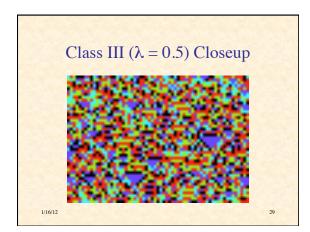


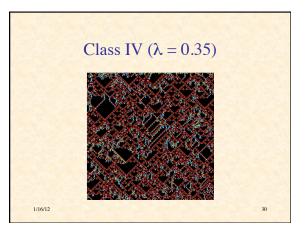


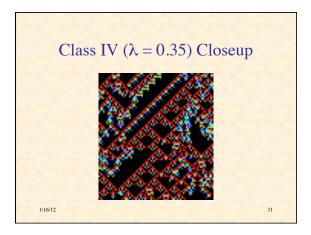


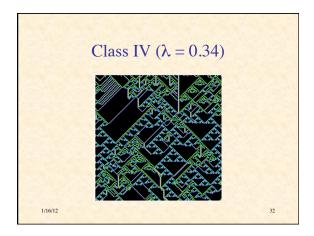


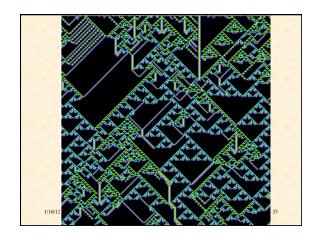


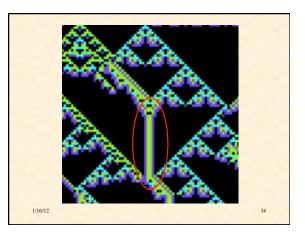


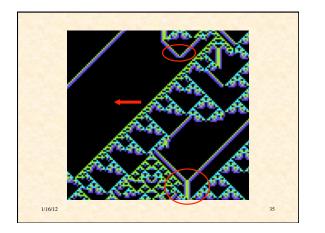


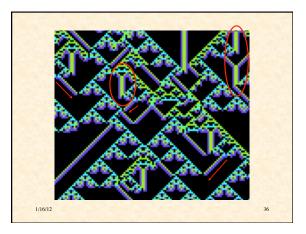


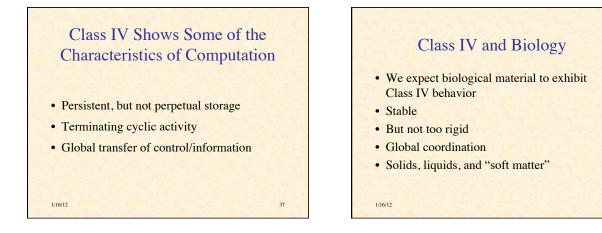


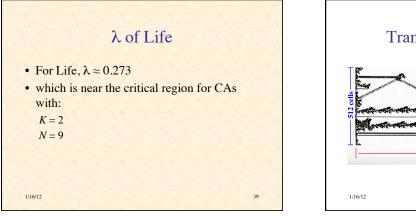


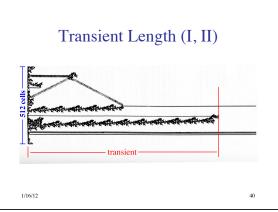


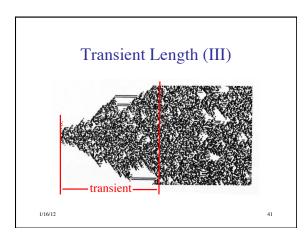


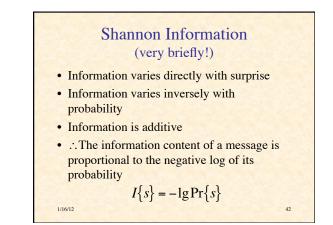


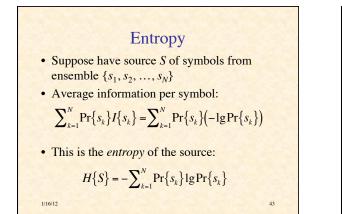


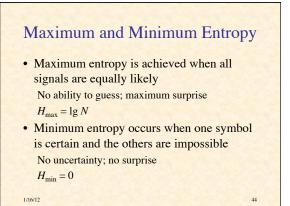


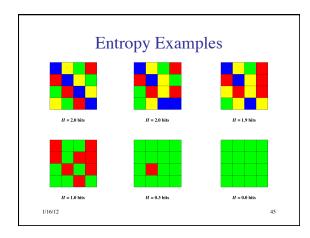


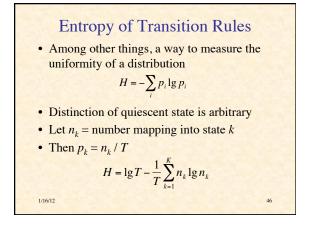


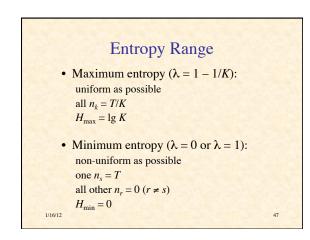


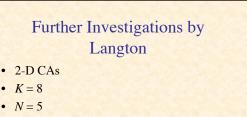








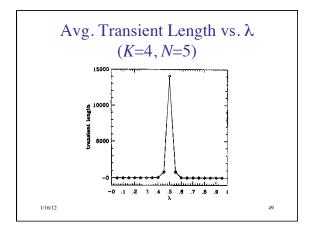


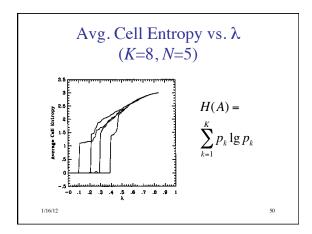


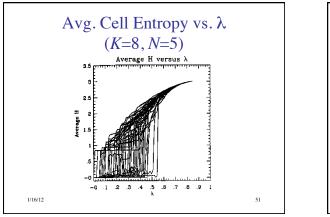
• 64 × 64 lattice

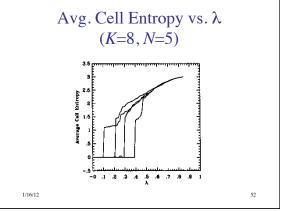
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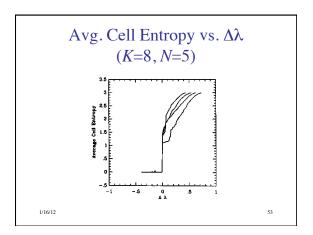
• periodic boundary conditions

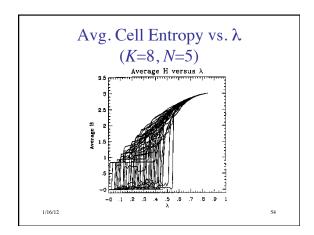


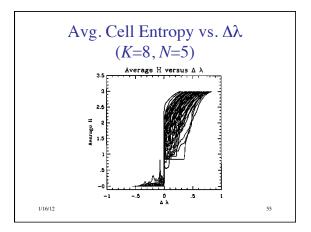


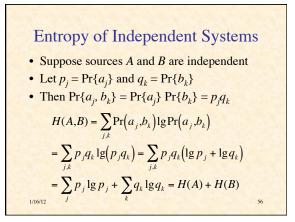


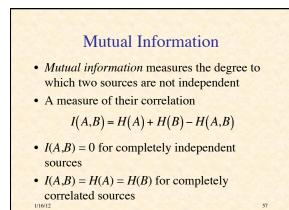


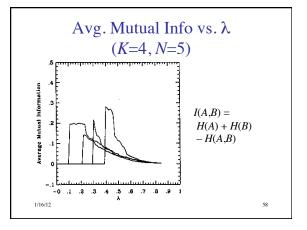


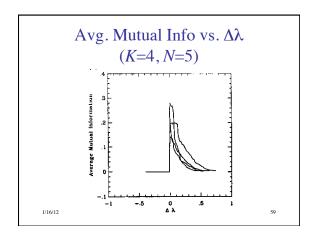


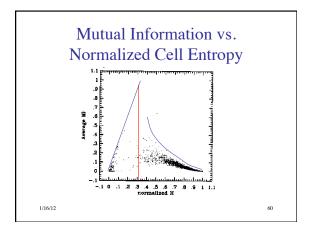


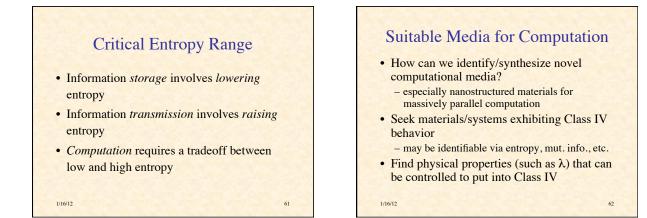


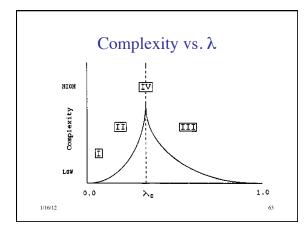


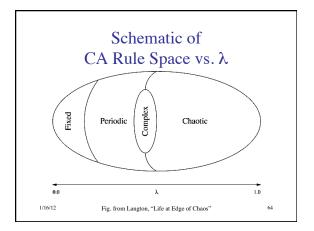


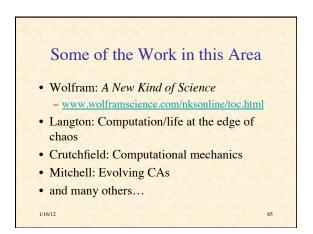












Some Other Simple Computational Systems Exhibiting the Same Behavioral Classes

- CAs (1D, 2D, 3D, totalistic, etc.)
- Mobile Automata
- Turing Machines
- Substitution Systems
- Tag Systems

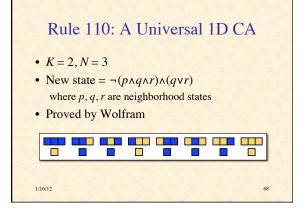
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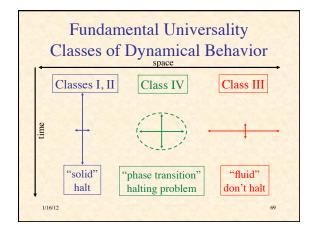
- Cyclic Tag Systems
- Symbolic Systems (combinatory logic, lambda calculus)
- Continuous CAs (coupled map lattices)
- PDEs
- Probabilistic CAs

Universality

- A system is *computationally universal* if it can compute anything a Turing machine (or digital computer) can compute
- The Game of Life is universal
- Several 1D CAs have been proved to be universal
- Are all complex (Class IV) systems universal?
- Is universality rare or common?

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Wolfram's Principle of computational equivalence ** a fundamental unity exists across a vast range of processes in nature and elsewhere: despite all their detailed differences every process can be viewed as corresponding to a computation that is utimately equivalent in its sophistication" (NKS 210) ** Conjecture: "among all possible systems with behavior that is not obviously simple an overwhelming fraction are universal" (NKS 721)

Computational Irreducibility

- "systems one uses to make predictions cannot be expected to do computations that are any more sophisticated than the computations that occur in all sorts of systems whose behavior we might try to predict" (*NKS* 741)
- "even if in principle one has all the information one needs to work out how some particular system will behave, it can still take an irreducible amount of computational work to do this" (*NKS* 739)
- That is: for Class IV systems, you can't (in general) do better than simulation.

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Additional Bibliography 1. Langton, Christopher G. "Computation at the Edge of Chaos: Phase Transitions and Emergent Computation," in Emergent Computation, ed. Stephanie Forrest. North-Holland, 1990. Langton, Christopher G. "Life at the Edge of 2. Chaos," in Artificial Life II, ed. Langton et al. Addison-Wesley, 1992. 3. Emmeche, Claus. The Garden in the Machine: The Emerging Science of Artificial Life. Princeton, 1994. Wolfram, Stephen. A New Kind of Science. 4. Wolfram Media, 2002. 1/16/12 Part 2B 72

