# V. Evolutionary Computing

A. Genetic Algorithms

### Genetic Algorithms

- · Developed by John Holland in '60s
- Did not become popular until late '80s
- · A simplified model of genetics and evolution by natural selection
- Most widely applied to optimization problems (maximize "fitness")

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#### Assumptions

- · Existence of fitness function to quantify merit of potential solutions
  - this "fitness" is what the GA will maximize
- A mapping from bit-strings to potential solutions
  - best if each possible string generates a legal potential solution
  - choice of mapping is important
  - can use strings over other finite alphabets

## Outline of Simplified GA

- 1. Random initial population P(0)
- 2. Repeat for  $t = 0, ..., t_{\text{max}}$  or until converges:
  - a) create empty population P(t+1)
  - b) repeat until P(t + 1) is full:
    - 1) select two individuals from P(t) based on fitness
    - 2) optionally mate & replace with offspring
    - 3) optionally mutate offspring
    - 4) add two individuals to P(t+1)

#### Fitness-Biased Selection

- Want the more "fit" to be more likely to reproduce
  - always selecting the best
  - ⇒ premature convergence
  - probabilistic selection ⇒ better exploration
- Roulette-wheel selection: probability ∝ relative fitness:

$$\Pr\{i \text{ mates}\} = \frac{f_i}{\sum_{j=1}^{n} f_j}$$

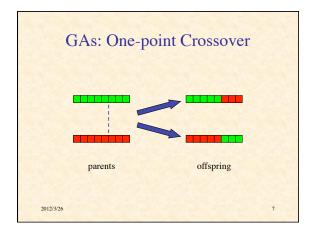
Crossover: Biological Inspiration

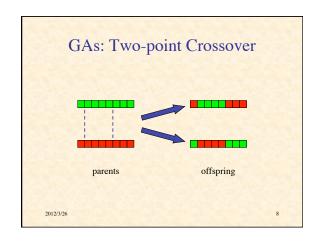
· Occurs during meiosis, when haploid gametes are formed

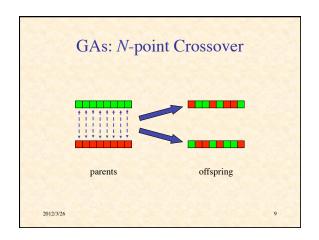
· Randomly mixes genes from two parents

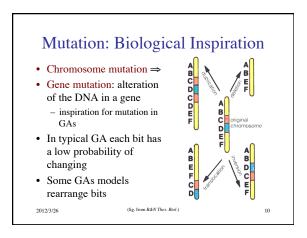
· Creates genetic variation in gametes

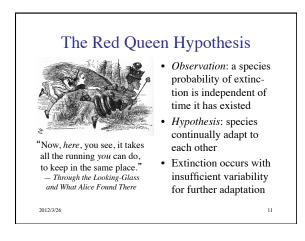
(fig. from B&N Thes. Biol.)

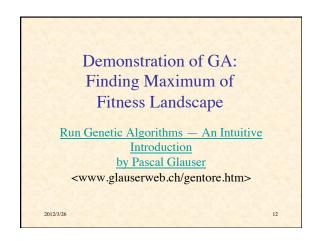












Demonstration of GA: Evolving to Generate a Pre-specified Shape (Phenotype)

Run Genetic Algorithm Viewer <a href="https://www.rennard.org/alife/english/gavgb.html">www.rennard.org/alife/english/gavgb.html</a>

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Demonstration of GA: Eaters Seeking Food

http://math.hws.edu/xJava/GA/

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# Morphology Project by Michael "Flux" Chang

- Senior Independent Study project at UCLA
  - users.design.ucla.edu/~mflux/morphology
- Researched and programmed in 10 weeks
- Programmed in Processing language
  - www.processing.org

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## Genotype ⇒ Phenotype

- · Cells are "grown," not specified individually
- Each gene specifies information such as:
  - angle
  - distance
  - type of cell
  - how many times to replicate
  - following gene
- Cells connected by "springs"
- Run phenome:

<users.design.ucla.edu/~mflux/morphology/gallery/sketches/phenome>

#### Complete Creature

- Neural nets for control (blue)
  - integrate-and-fire neurons
- Muscles (red)
  - decrease "spring length" when fire
- Sensors (green)
  - fire when exposed to "light"
- Structural elements (grey)
  - anchor other cells together
- Creature embedded in a fluid
- Run <u>users\_design\_ucla\_edu/~mflux/morphology/gallery/sketches/creature></u>
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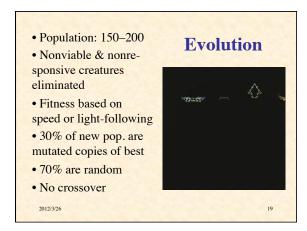
#### Effects of Mutation

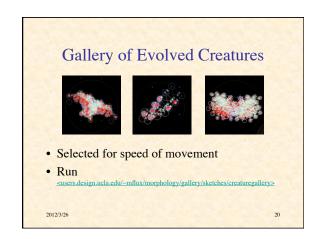
- Neural nets for control (blue)
- Muscles (red)
- Sensors (green)
- Structural elements (grey)
- Creature embedded in a fluid
- Run

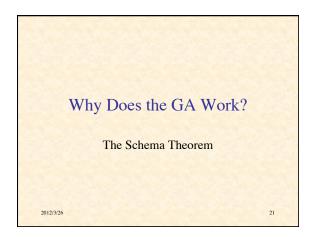
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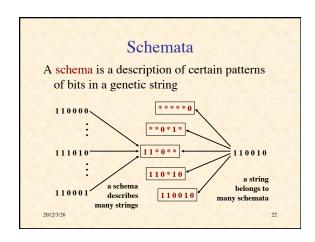
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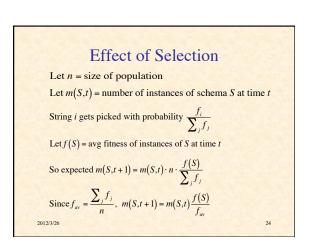








# The Fitness of Schemata The schemata are the building blocks of solutions We would like to know the average fitness of all possible strings belonging to a schema We cannot, but the strings in a population that belong to a schema give an estimate of the fitness of that schema Each string in a population is giving information about all the schemata to which it belongs (implicit parallelism)



# **Exponential Growth**

- We have discovered:  $m(S, t+1) = m(S, t) \cdot f(S) / f_{av}$
- Suppose  $f(S) = f_{av} (1 + c)$
- Then  $m(S, t) = m(S, 0) (1 + c)^t$
- That is, exponential growth in aboveaverage schemata

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#### Effect of Crossover

\*\*1 ... 0\*\*\* |←δ→|

- Let  $\lambda$  = length of genetic strings
- Let  $\delta(S)$  = defining length of schema S
- Probability {crossover destroys *S*}:  $p_d \le \delta(S) / (\lambda 1)$
- Let  $p_c$  = probability of crossover
- Probability schema survives:

$$p_{\rm s} \ge 1 - p_{\rm c} \frac{\delta(S)}{\lambda - 1}$$

## Selection & Crossover Together

$$m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{av}} \left[ 1 - p_c \frac{\delta(S)}{\lambda - 1} \right]$$

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#### Effect of Mutation

- Let  $p_{\rm m}$  = probability of mutation
- So  $1 p_{\rm m} =$  probability an allele survives
- Let o(S) = number of fixed positions in S
- The probability they all survive is  $(1 p_m)^{o(S)}$
- If  $p_{\rm m} << 1$ ,  $(1 p_{\rm m})^{o(S)} \approx 1 o(S) p_{\rm m}$

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# Schema Theorem: "Fundamental Theorem of GAs"

$$m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{\text{av}}} \left[ 1 - p_c \frac{\delta(S)}{\lambda - 1} - o(S) p_m \right]$$

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#### The Bandit Problem

- Two-armed bandit:
  - random payoffs with (unknown) means  $m_1, m_2$  and variances  $\sigma_1, \sigma_2$
  - optimal strategy: allocate exponentially greater number of trials to apparently better lever
- k-armed bandit: similar analysis applies
- Analogous to allocation of population to schemata
- Suggests GA may allocate trials optimally

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# Goldberg's Analysis of Competent & Efficient GAs

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#### Paradox of GAs

- Individually uninteresting operators:
  - selection, recombination, mutation
- Selection + mutation ⇒ continual improvement
- Selection + recombination ⇒ innovation
  - fundamental to invention:
     generation vs. evaluation
- Fundamental intuition of GAs: the three work well together

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# Race Between Selection & Innovation: Takeover Time

- Takeover time  $t^*$  = average time for most fit to take over population
- Transaction selection: population replaced by *s* copies of top 1/*s*
- s quantifies selective pressure
- Estimate  $t^* \approx \ln n / \ln s$

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#### **Innovation Time**

- Innovation time t<sub>i</sub> = average time to get a better individual through crossover & mutation
- Let p<sub>i</sub> = probability a single crossover produces a better individual
- Number of individuals undergoing crossover =  $p_c n$
- Number of probable improvements =  $p_i p_c n$
- Estimate:  $t_i \approx 1 / (p_c p_i n)$

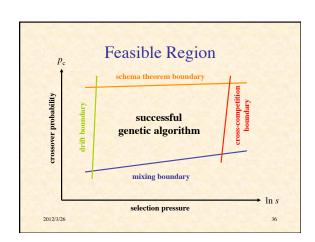
## Steady State Innovation

- Bad:  $t^* < t_i$ 
  - because once you have takeover, crossover does no good
- Good:  $t_i < t^*$ 
  - because each time a better individual is produced, the t\* clock resets
  - steady state innovation
- Innovation number:

$$Iv = \frac{t^*}{t_i} = p_c p_i \frac{n \ln n}{\ln s} > 1$$

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# Other Algorithms Inspired by Genetics and Evolution

- Evolutionary Programming
  - natural representation, no crossover, time-varying continuous mutation
- Evolutionary Strategies
  - similar, but with a kind of recombination
- Genetic Programming
  - like GA, but program trees instead of strings
- Classifier Systems
  - GA + rules + bids/payments
- · and many variants & combinations...

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Next: Agents and Self-Organization

(Re)read ch. 16

# Additional Bibliography

- 1. Goldberg, D.E. The Design of Innovation: Lessons from and for Competent Genetic Algorithms. Kluwer, 2002.
- 2. Milner, R. *The Encyclopedia of Evolution*. Facts on File, 1990.

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