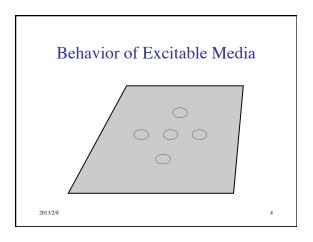
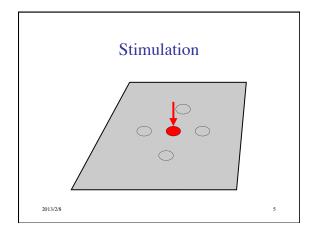
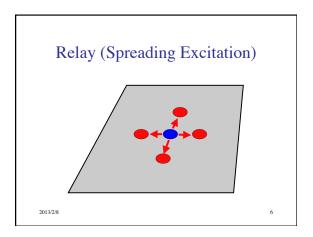


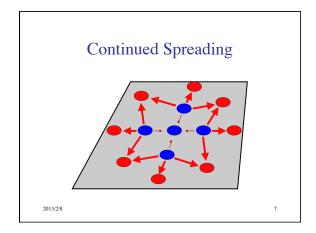
## Examples of Excitable Media • Slime mold amoebas • Cardiac tissue (& other muscle tissue) • Cortical tissue • Certain chemical systems (e.g., BZ reaction) • Hodgepodge machine

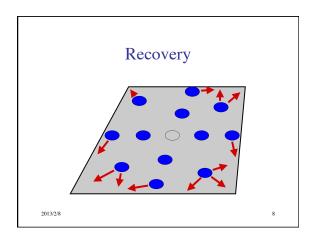
# Characteristics of Excitable Media • Local spread of excitation - for signal propagation • Refractory period - for unidirectional propagation • Decay of signal - avoid saturation of medium

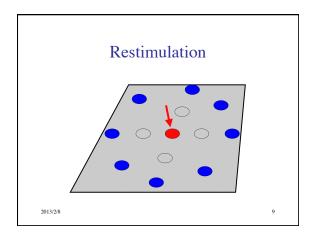












#### Circular & Spiral Waves Observed in:

- Slime mold aggregation
- Chemical systems (e.g., BZ reaction)
- Neural tissue
- Retina of the eye
- · Heart muscle
- Intracellular calcium flows
- · Mitochondrial activity in oocytes

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### Cause of Concentric Circular Waves

- Excitability is not enough
- But at certain developmental stages, cells can operate as pacemakers
- When stimulated by cAMP, they begin emitting regular pulses of cAMP

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#### Spiral Waves

- Persistence & propagation of spiral waves explained analytically (Tyson & Murray, 1989)
- Rotate around a small core of of nonexcitable cells
- Propagate at higher frequency than circular
- Therefore they dominate circular in collisions
- But how do the spirals form initially?

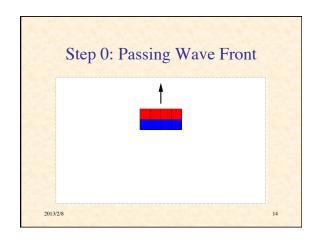
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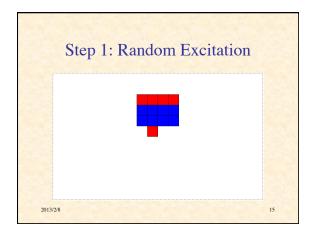
12

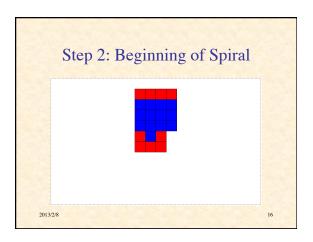
### Some Explanations of Spiral Formation

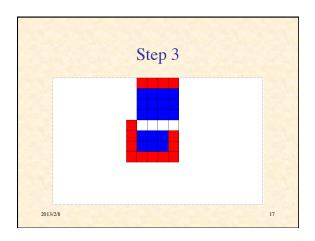
- "the origin of spiral waves remains obscure" (1997)
- Traveling wave meets obstacle and is broken
- Desynchronization of cells in their developmental path
- Random pulse behind advancing wave front

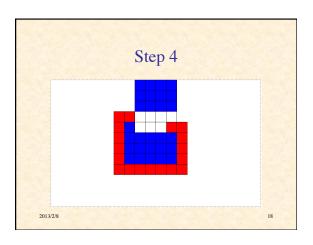
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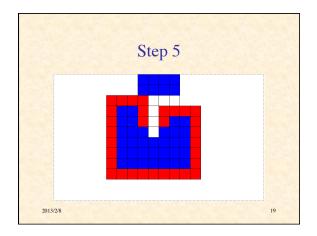


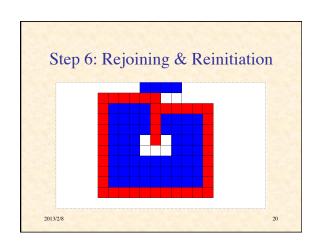


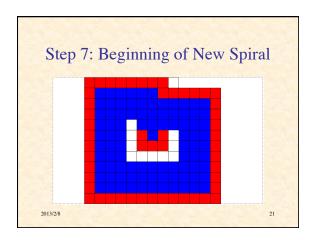


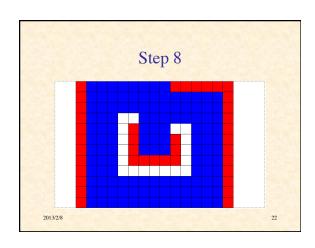


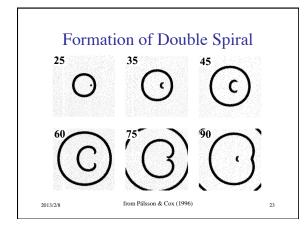












## NetLogo Simulation Of Spiral Formation • Amoebas are immobile at timescale of wave movement • A fraction of patches are inert (grey) • A fraction of patches has initial concentration of cAMP • At each time step: - chemical diffuses - each patch responds to local concentration

#### Response of Patch

if patch is not refractory (brown) then
 if local chemical > threshold then
 set refractory period
 produce pulse of chemical (red)
else

decrement refractory period degrade chemical in local area

V8

#### Demonstration of NetLogo Simulation of Spiral Formation

Run SlimeSpiral.nlogo

13/2/8

#### Demonstration of NetLogo Simulation of Spiral Formation (a closer look)

Run SlimeSpiralBig.nlogo

2013/2/8

#### Observations

- Excitable media can support circular and spiral
- Spiral formation can be triggered in a variety of ways
- All seem to involve inhomogeneities (broken symmetries):
  - in space
  - in time
  - in activity
- · Amplification of random fluctuations
- Circles & spirals are to be expected

### NetLogo Simulation of Streaming Aggregation

- 1. chemical diffuses
- 2. **if** cell is refractory (yellow)
- 3. then chemical degrades
- 4. else (it's excitable, colored white)
  - if chemical > movement threshold then take step up chemical gradient
  - else if chemical > relay threshold then produce more chemical (red) become refractory
  - 3. else wait

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Demonstration of NetLogo Simulation of Streaming

Run SlimeStream.nlogo

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### Typical Equations for Excitable Medium (ignoring diffusion)

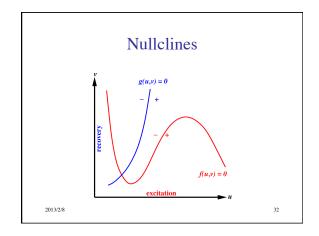
• Excitation variable:

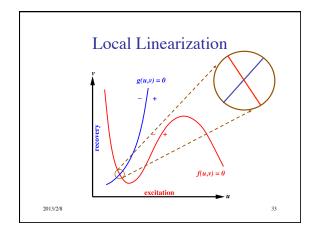
$$\dot{u} = f(u,v)$$

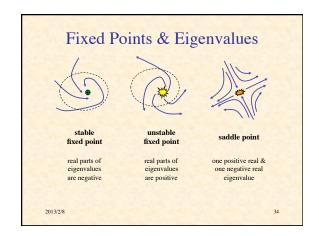
· Recovery variable:

$$\dot{v} = g(u, v)$$

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#### FitzHugh-Nagumo Model

- A simplified model of action potential generation in neurons
- The neuronal membrane is an excitable medium
- *B* is the input bias:

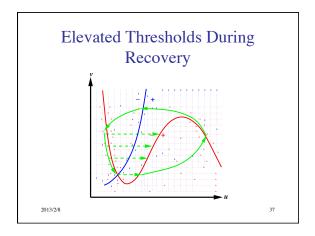
$$\dot{u} = u - \frac{u^3}{3} - v + B$$

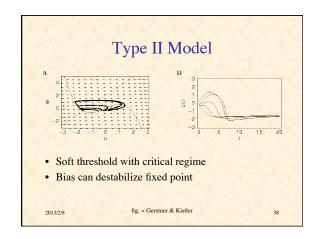
$$\dot{v} = \varepsilon (b_0 + b_1 u - v)$$

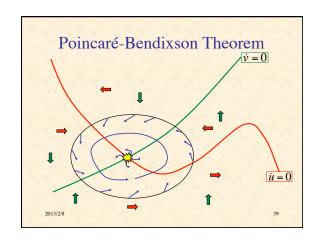
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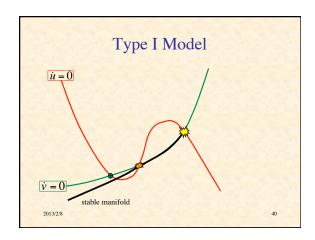
NetLogo Simulation of
Excitable Medium
in 2D Phase Space

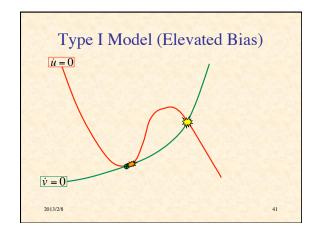
(EM-Phase-Plane.nlogo)

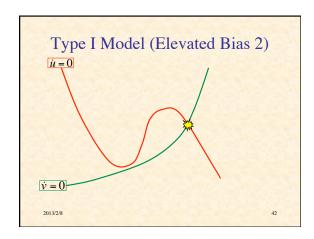


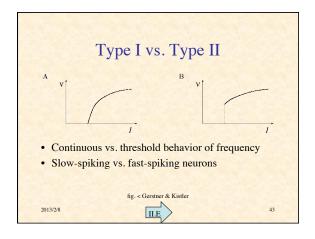


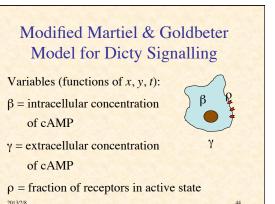












## Equations $\frac{d\beta(xy,t)}{dt} = s\Phi(\rho,\gamma) \qquad -\beta k_i \qquad -\beta k_t \qquad [1]$ Rate of change in of cAMP of the camp of cAMP o

### Positive Feedback Loop • Extracellular cAMP increases (γ increases) • ⇒ Rate of synthesis of intracellular cAMP increases (Φ increases) • ⇒ Intracellular cAMP increases (β increases) • ⇒ Rate of secretion of cAMP increases • (⇒ Extracellular cAMP increases)

# Negative Feedback Loop • Extracellular cAMP increases (γ increases) • ⇒ cAMP receptors desensitize (f₁ increases, f₂ decreases, ρ decreases) • ⇒ Rate of synthesis of intracellular cAMP decreases (Φ decreases) • ⇒ Intracellular cAMP decreases (β decreases) • ⇒ Rate of secretion of cAMP decreases • ⇒ Extracellular cAMP decreases (γ decreases) See Equations 47

## Dynamics of Model • Unperturbed ⇒ cAMP concentration reaches steady state • Small perturbation in extracellular cAMP ⇒ returns to steady state • Perturbation > threshold ⇒ large transient in cAMP, then return to steady state • Or oscillation (depending on model parameters)

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