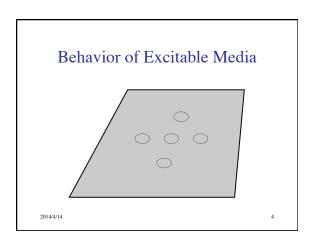
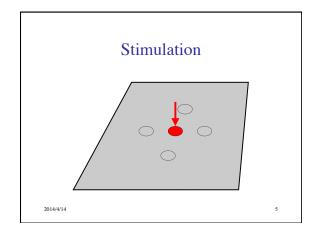
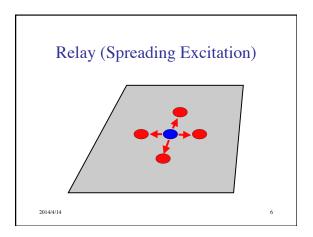


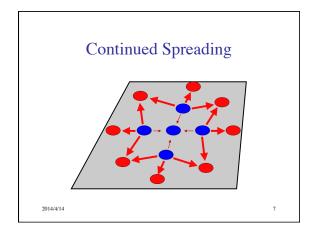
Examples of Excitable Media • Slime mold amoebas • Cardiac tissue (& other muscle tissue) • Cortical tissue • Certain chemical systems (e.g., BZ reaction) • Hodgepodge machine

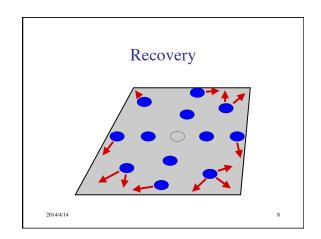
Characteristics of Excitable Media • Local spread of excitation - for signal propagation • Refractory period - for unidirectional propagation • Decay of signal - avoid saturation of medium

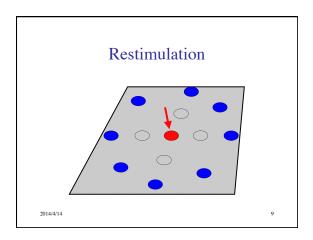












Circular & Spiral Waves Observed in:

- Slime mold aggregation
- Chemical systems (e.g., BZ reaction)
- Neural tissue
- · Retina of the eye
- Heart muscle
- Intracellular calcium flows
- · Mitochondrial activity in oocytes

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Cause of Concentric Circular Waves

- Excitability is not enough
- But at certain developmental stages, cells can operate as pacemakers
- When stimulated by cAMP, they begin emitting regular pulses of cAMP

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Spiral Waves

- Persistence & propagation of spiral waves explained analytically (Tyson & Murray, 1989)
- Rotate around a small core of of nonexcitable cells
- Propagate at higher frequency than circular
- Therefore they dominate circular in collisions
- But how do the spirals form initially?

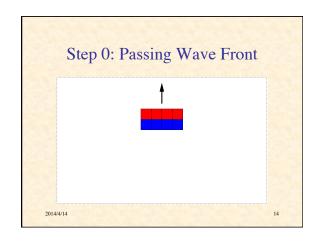
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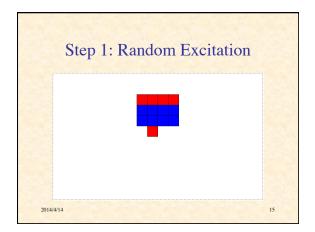
12

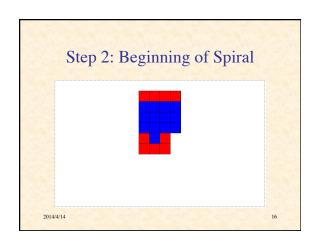
Some Explanations of Spiral Formation

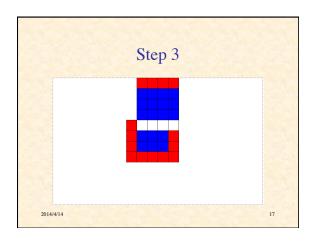
- "the origin of spiral waves remains obscure" (1997)
- Traveling wave meets obstacle and is broken
- Desynchronization of cells in their developmental path
- Random pulse behind advancing wave front

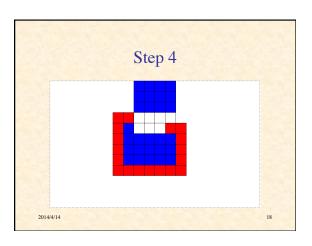
14/4/14

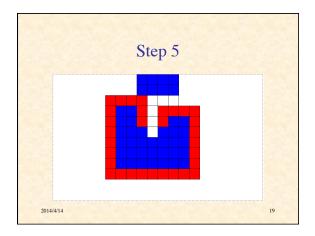


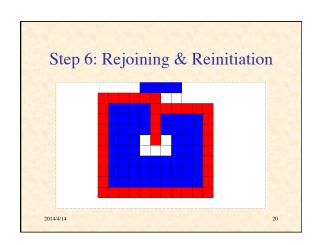


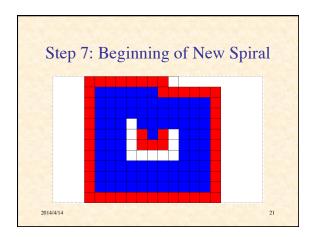


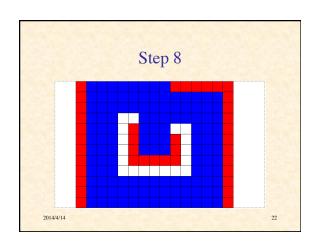


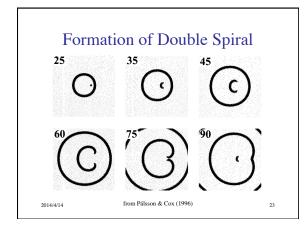












NetLogo Simulation Of Spiral Formation • Amoebas are immobile at timescale of wave movement • A fraction of patches are inert (grey) • A fraction of patches has initial concentration of cAMP • At each time step: - chemical diffuses - each patch responds to local concentration

Response of Patch

if patch is not refractory (brown) then
 if local chemical > threshold then
 set refractory period
 produce pulse of chemical (red)
else

decrement refractory period degrade chemical in local area

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Demonstration of NetLogo Simulation of Spiral Formation

Run SlimeSpiral.nlogo

Demonstration of NetLogo Simulation of Spiral Formation (a closer look)

Run SlimeSpiralBig.nlogo

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Observations

- Excitable media can support circular and spiral waves
- Spiral formation can be triggered in a variety of ways
- All seem to involve inhomogeneities (broken symmetries):
 - in space
 - in time
 - in activity
- · Amplification of random fluctuations
- Circles & spirals are to be expected

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NetLogo Simulation of Streaming Aggregation

- 1. chemical diffuses
- 2. **if** cell is refractory (yellow)
- 3. then chemical degrades
- 4. **else** (it's excitable, colored white)
 - if chemical > movement threshold then
 take step up chemical gradient
 - else if chemical > relay threshold then produce more chemical (red) become refractory
 - 3. else wait

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Demonstration of NetLogo Simulation of Streaming

Run SlimeStream.nlogo

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Typical Equations for Excitable Medium (ignoring diffusion)

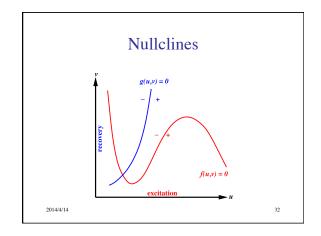
• Excitation variable:

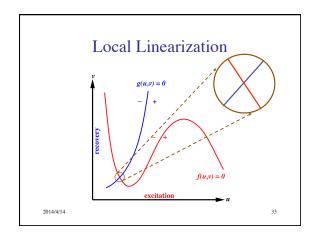
$$\dot{u} = f(u,v)$$

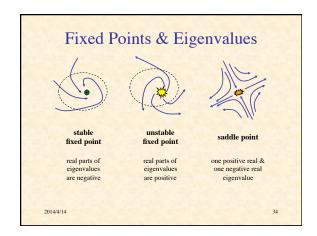
• Recovery variable:

$$\dot{v} = g(u,v)$$

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FitzHugh-Nagumo Model

- A simplified model of action potential generation in neurons
- The neuronal membrane is an excitable medium
- *B* is the input bias:

$$\dot{u} = u - \frac{u^3}{3} - v + B$$

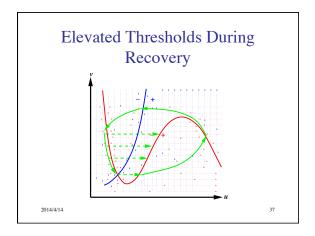
$$\dot{v} = \varepsilon (b_0 + b_1 u - v)$$

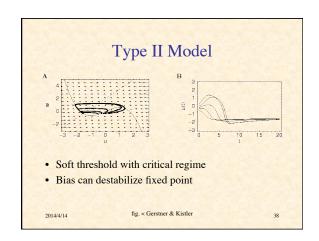
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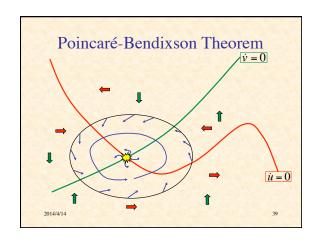
 $= \mathcal{E}(\mathcal{D}_0 + \mathcal{D}_1 \mathcal{U} - \mathcal{V})$

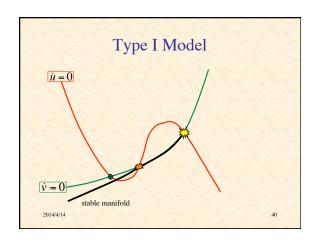
NetLogo Simulation of
Excitable Medium
in 2D Phase Space

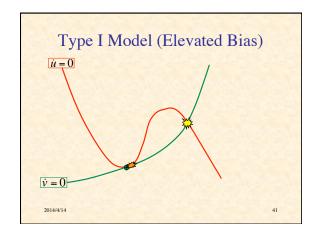
(EM-Phase-Plane.nlogo)

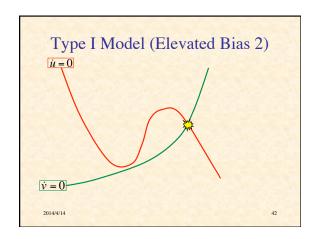


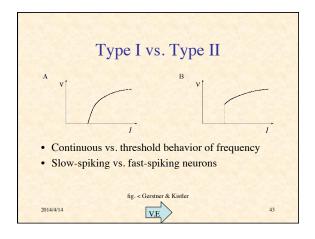


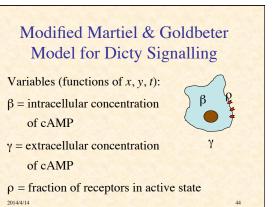












Equations $\frac{d\beta(x,y,t)}{dt} = s\Phi(\rho,\gamma) \qquad -\beta k_i \qquad -\beta k_t \qquad \textbf{[1]}$ Rate of change in intracellular [cAMP] = $\frac{Production}{of cAMP}$ - $\frac{Intracellular}{hydrolysis}$ - $\frac{Secretion}{of cAMP}$ $\frac{d\gamma(x,y,t)}{dt} = \frac{k_t}{h}\beta \qquad -k_c\gamma \qquad +D\nabla^2\gamma \qquad \textbf{[2]}$ Rate of change in extracellular [cAMP] = $\frac{Secretion}{of cAMP}$ - $\frac{Extracellular}{hydrolysis}$ + $\frac{Diffusion}{of cAMP}$ $\frac{d\rho(x,y,t)}{dt} = f_2(\gamma)(1-\rho) \qquad -f_1(\gamma)\rho \qquad \textbf{[3]}$ Rate of change in fraction of active receptor = $\frac{Dephosphotoropylation}{rylation of receptor}$ - $\frac{Phosphorylation}{of receptor}$

Positive Feedback Loop • Extracellular cAMP increases (γ increases) • ⇒ Rate of synthesis of intracellular cAMP increases (Φ increases) • ⇒ Intracellular cAMP increases (β increases) • ⇒ Rate of secretion of cAMP increases • (⇒ Extracellular cAMP increases)

Negative Feedback Loop • Extracellular cAMP increases (γ increases) • ⇒ cAMP receptors desensitize (f₁ increases, f₂ decreases, ρ decreases) • ⇒ Rate of synthesis of intracellular cAMP decreases (Φ decreases) • ⇒ Intracellular cAMP decreases (β decreases) • ⇒ Rate of secretion of cAMP decreases (γ decreases) • ⇒ Extracellular cAMP decreases (γ decreases) See Equations 47

Dynamics of Model • Unperturbed ⇒ cAMP concentration reaches steady state • Small perturbation in extracellular cAMP ⇒ returns to steady state • Perturbation > threshold ⇒ large transient in cAMP, then return to steady state • Or oscillation (depending on model parameters)

Additional Bibliography

- Kessin, R. H. Dictyostelium: Evolution, Cell Biology, and the Development of Multicellularity. Cambridge, 2001.

 Gerhardt, M., Schuster, H., & Tyson, J. J. "A Cellular Automaton Model of Excitable Media Including Curvature and Dispersion," Science 247 (1990): 1563-6.

 Tyson, J. J., & Keener, J. P. "Singular Perturbation Theory of Traveling Waves in Excitable Media (A Review)," Physica D 32 (1988): 327-61.

 Camazine, S. Deneubourg, L. J. Franks, N. P. Spayel, L.

- (1988): 327-61.

 Camazine, S., Deneubourg, J.-L., Franks, N. R., Sneyd, J.,
 Theraulaz, G., & Bonabeau, E. Self-Organization in Biological
 Systems. Princeton, 2001.

 Pálsson, E., & Cox, E. C. "Origin and Evolution of Circular Waves
 and Spiral in Dictyostelium discoideum Territories," Proc. Natl.
 Acad. Sci. USA: 93 (1996): 1151-5.

 Solé, R., & Goodwin, B. Signs of Life: How Complexity Pervades
 Biology. Basic Books, 2000.

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