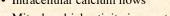
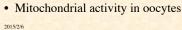


10



•

11

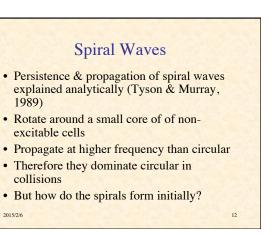


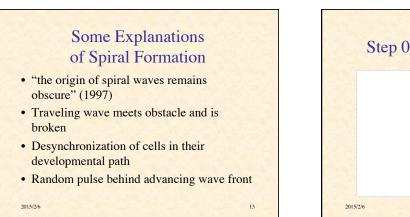
## Cause of **Concentric Circular Waves**

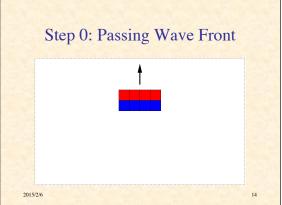
• Excitability is not enough

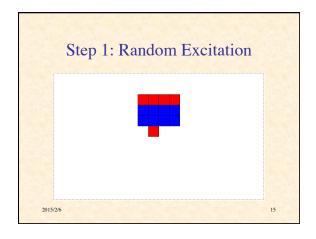
2015/2/6

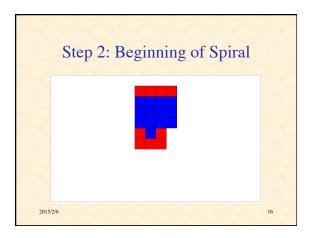
- But at certain developmental stages, cells can operate as pacemakers
- When stimulated by cAMP, they begin emitting regular pulses of cAMP

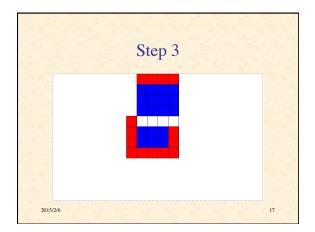


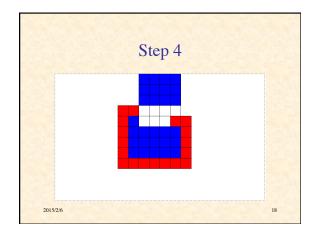


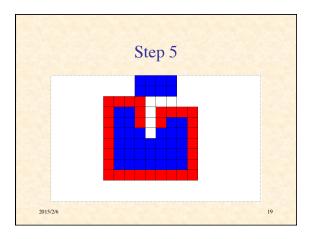


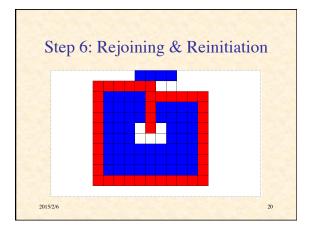




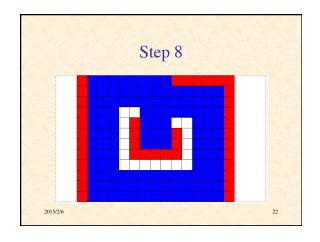


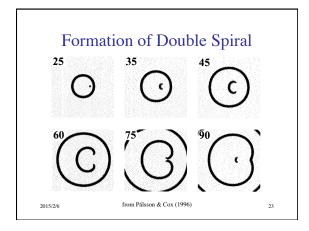


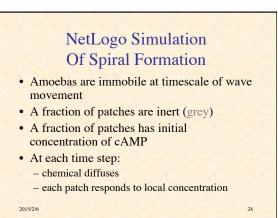


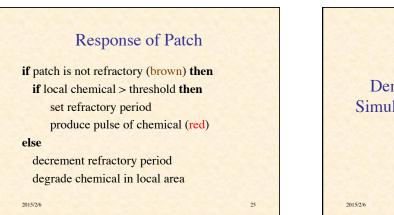




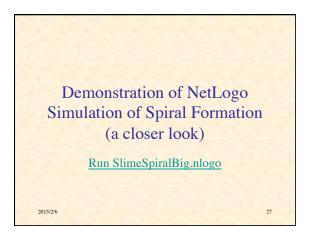












## Observations

- Excitable media can support circular and spiral waves
- Spiral formation can be triggered in a variety of ways
- All seem to involve inhomogeneities (broken symmetries):
  - in space

2015/2/6

2015/2/6

- in time
- in activity
- Amplification of random fluctuations
- Circles & spirals are to be expected

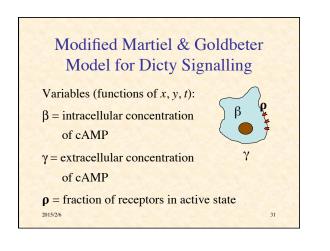
## NetLogo Simulation of Streaming Aggregation

- 1. chemical diffuses
- 2. **if** cell is refractory (yellow)
- 3. then chemical degrades
- 4. **else** (it's excitable, colored white)
- if chemical > movement threshold then take step up chemical gradient
- else if chemical > relay threshold then produce more chemical (red) become refractory
- 3. else wait

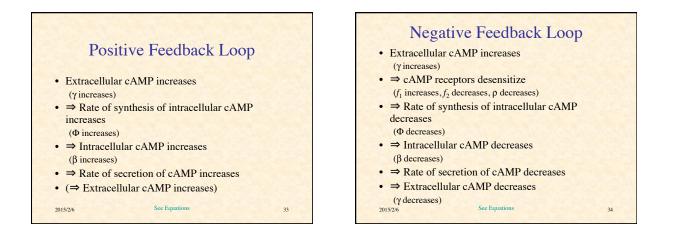
2015/2/6

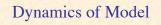


30



Equations			
$\frac{d\beta(x,y,t)}{dt} = s\Phi(\rho,\gamma)$	$-\beta k_{\rm i}$	$-\beta k_{t}$	[1]
Rate of change in $[cAMP] = \frac{Production}{of cAMP}$	<ul> <li>Intracellula hydrolysis</li> </ul>	ar - Secretion of cAMP	
$\frac{d\gamma(x,y,t)}{dt} = \frac{k_t}{h}\beta$	$-k_{\rm e}\gamma$	$+ D  abla^2 \gamma$	[2]
Rate of change in extracellular $[cAMP]$ = $\begin{cases} Secretion \\ of cAMP \end{cases}$	<ul> <li>Extracellul</li> <li>hydrolysis</li> </ul>	$ar + \frac{\text{Diffusion}}{\text{of cAMP}}$	
$\frac{d\rho(x,y,t)}{dt} = f_2(\gamma)(1-\rho)$	$-f_1(\gamma)\rho$		[3]
Rate of change in frac- tion of active receptor $=$ Tylation of receptor	or - Phosphory of receptor	r r	
2015/2/6			32





• Unperturbed

2015/2/6

- $\Rightarrow$  cAMP concentration reaches steady state
- Small perturbation in extracellular cAMP ⇒ returns to steady state
- Perturbation > threshold
   ⇒ large transient in cAMP, then return to steady state
- Or oscillation (depending on model parameters)

## Typical Equations for Excitable Medium (ignoring diffusion)

• Excitation variable:

$$\dot{u} = f(u, v)$$

• Recovery variable:

2015/2/6

 $\dot{v} = g(u,v)$ 

