











Differential Interaction Ranges

- How can a system using strictly local interactions discriminate between states at long and short range?
- E.g. cells in developing organism
- Can use two different *morphogens* diffusing at two different rates

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- activator diffuses slowly (short range)
- inhibitor diffuses rapidly (long range)
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Framework for Complexity change = source terms + transport terms source terms = local coupling interactions local to a small region transport terms = spatial coupling interactions with contiguous regions advection + diffusion

- advection: non-dissipative, time-reversible
- diffusion: dissipative, irreversible

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Continuous-time Activator-Inhibitor System

• Activator A and inhibitor I may diffuse at different rates in x and y directions

 $\frac{\partial A}{\partial t} = d_{Ax} \frac{\partial^2 A}{\partial x^2} + d_{Ay} \frac{\partial^2 A}{\partial y^2} + k_A (A + B - I)$

 $\frac{\partial I}{\partial t} = d_{\rm Ix} \frac{\partial^2 I}{\partial x^2} + d_{\rm Iy} \frac{\partial^2 I}{\partial v^2} + k_{\rm I} (A + B - I)$

- Cell becomes more active if activator + bias exceeds inhibitor
- Otherwise, less active

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• A and I are limited to [0, 100] (depletion/saturation)

Demonstration of NetLogo Program for Activator/Inhibitor Pattern Formation with Continuous State Change

Run Activator-Inhibitor.nlogo

Turing Patterns

- Alan Turing studied the mathematics of reaction-diffusion systems
- Turing, A. (1952). The chemical basis of morphogenesis. *Philosophical Transactions of the Royal Society* **B 237**: 37–72.
- The resulting patterns are known as *Turing* patterns

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Observations

- With local activation and lateral inhibition
- And with a random initial state
- You can expect to get Turing patterns
- These are stationary states (dynamic equilibria)
- Macroscopically, Class I behavior

 Microscopically, may be class III

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A Key Element of Self-Organization

- Activation vs. Inhibition
- Cooperation vs. Competition
- Amplification vs. Stabilization
- Growth vs. Limit
- Positive Feedback vs. Negative Feedback – Positive feedback creates
 - Negative feedback shapes
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- restore broken contours
- detect edges
- improve contrast

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