



# Genetic Algorithms

- Developed by John Holland in '60s
- Did not become popular until late '80s
- A simplified model of genetics and evolution by natural selection
- Most widely applied to optimization problems (maximize "fitness")

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#### Assumptions

- Existence of fitness function to quantify merit of potential solutions
  - This "fitness" is what the GA will maximize
- A mapping from bit-strings to potential solutions
  - best if each possible string generates a legal potential solution
  - choice of mapping is important
  - can use strings over other finite alphabets

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#### Outline of Simplified GA

- 1. Random initial population P(0)
- 2. Repeat for  $t = 0, ..., t_{max}$  or until converges:
  - a) create empty population P(t+1)
  - b) repeat until P(t+1) is full:
    - 1) select two individuals from P(t) based on fitness
    - 2) optionally mate & replace with offspring
    - 3) optionally mutate offspring
    - 4) add two individuals to P(t + 1)





GAs: One-point Crossover

offspring

parents











# Mutation: Biological Inspiration

- Chromosome mutation <sup>554</sup>
  Gene mutation: alteration
- of the DNA in a gene – inspiration for mutation in
- GAs • In typical GA each bit has
- a low probability of changing
- Some GAs models rearrange bits

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# The Red Queen Hypothesis



"Now, here, you see, it takes all the running you can do, to keep in the same place." — Through the Looking-Glass and What Alice Found There

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- *Observation*: a species probability of extinction is independent of time it has existed
- *Hypothesis*: species continually adapt to each other
- Extinction occurs with insufficient variability for further adaptation

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Demonstration of GA: Finding Maximum of Fitness Landscape Run Genetic Algorithms — An Intuitive

Introduction by Pascal Glauser <www.glauserweb.ch/gentore.htm>

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Demonstration of GA: Evolving to Generate a Pre-specified Shape (Phenotype)

Run Genetic Algorithm Viewer <www.rennard.org/alife/english/gavgb.html>

Demonstration of GA: Eaters Seeking Food http://math.hws.edu/xJava/GA/

#### Morphology Project by Michael "Flux" Chang

- Senior Independent Study project at UCLA – users.design.ucla.edu/~mflux/momphology
- Researched and programmed in 10 weeks
- Programmed in Processing language
   www.processing.org

#### Genotype $\Rightarrow$ Phenotype

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- Cells are "grown," not specified individually
- Each gene specifies information such as:
  - angle

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- distance
- type of cell
- how many times to replicate
- following gene
- Cells connected by "springs"
- Run phenome:

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## **Complete Creature**

mflu x/morphology/gallery/sketches/phenome>

- Neural nets for control (blue) - integrate-and-fire neurons
- Muscles (red)
- Decrease "spring length" when fire
- Sensors (green)
- fire when exposed to "light"
- Structural elements (grey)
   anchor other cells together
- Creature embedded in a fluid
- Run <u sers.desig.nucla.ed u/~mflux/morpholog.y/g allerv/sk etches/creature>
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#### The Fitness of Schemata

- The schemata are the building blocks of solutions
- We would like to know the average fitness of all possible strings belonging to a schema
- We cannot, but the strings in a population that belong to a schema give an estimate of the fitness of that schema
- Each string in a population is giving information about all the schemata to which it belongs (implicit parallelism)

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#### Effect of Selection

Let n = size of populationLet m(S,t) = number of instances of schema S at time tString *i* gets picked with probability  $\frac{f_i}{\sum_j f_j}$ Let f(S) = avg fitness of instances of S at time tSo expected  $m(S,t+1) = m(S,t) \cdot n \cdot \frac{f(S)}{\sum_j f_j}$ Since  $f_{av} = \frac{\sum_j f_j}{n}$ ,  $m(S,t+1) = m(S,t) \frac{f(S)}{f_{av}}$ 40006

#### **Exponential Growth**

- We have discovered:
- $m(S, t+1) = m(S, t) \cdot f(S) / f_{av}$
- Suppose  $f(S) = f_{av} (1 + c)$
- Then  $m(S, t) = m(S, 0) (1 + c)^t$
- That is, exponential growth in aboveaverage schemata



Selection & Crossover Together  

$$m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{av}} \left[1 - p_c \frac{\delta(S)}{\lambda - 1}\right]$$
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- Let  $p_{\rm m}$  = probability of mutation
- So  $1 p_m$  = probability an allele survives
- Let o(S) = number of fixed positions in S

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- The probability they all survive is  $(1 - p_m)^{o(S)}$
- If  $p_{\rm m} \ll 1$ ,  $(1 p_{\rm m})^{o(S)} \approx 1 o(S) p_{\rm m}$

Schema Theorem: "Fundamental Theorem of GAs"  $m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{av}} \left[ 1 - p_c \frac{\delta(S)}{\lambda - 1} - o(S) p_m \right]$ 4006

#### The Bandit Problem

- Two-armed bandit:
  - random payoffs with (unknown) means  $m_1, m_2$ and variances  $\sigma_1^2, \sigma_2^2$
  - optimal strategy: allocate exponentially greater number of trials to apparently better lever
- *k*-armed bandit: similar analysis applies
- Analogous to allocation of population to schemata
- Suggests GA may allocate trials optimally

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Goldberg's Analysis of Competent & Efficient GAs



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# Race Between Selection & Innovation: Takeover Time

- Takeover time *t*<sup>\*</sup> = average time for most fit to take over population
- Transaction selection: population replaced by *s* copies of top 1/*s*
- s quantifies selective pressure
- Estimate  $t^* \approx \ln n / \ln s$

#### Innovation Time

- Innovation time *t*<sub>i</sub> = average time to get a better individual through crossover & mutation
- Let  $p_i$  = probability a single crossover produces a better individual
- Number of individuals undergoing crossover =  $p_c n$
- Number of probable improvements =  $p_i p_c n$
- Estimate:  $t_i \approx 1 / (p_c p_i n)$

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## Other Algorithms Inspired by Genetics and Evolution

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#### • Evolutionary Programming

- natural representation, no crossover, time-varying continuous mutation
- Evolutionary Strategies - similar, but with a kind of recombination
- Genetic Programming
- like GA, but program trees instead of strings
- Classifier Systems
- GA + rules + bids/payments
- and many variants & combinations ...

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# Additional Bibliography

- 1. Goldberg, D.E. *The Design of Innovation: Lessons from and for Competent Genetic Algorithms*. Kluwer, 2002.
- 2. Milner, R. *The Encyclopedia of Evolution*. Facts on File, 1990.

