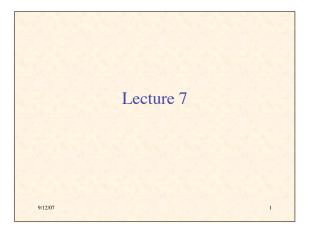
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### Modified Martiel & Goldbeter Model for Dicty Signalling

Variables (functions of x, y, t):

 $\beta$  = intracellular concentration of cAMP



 $\gamma$  = extracellular concentration of cAMP

 $\rho$  = fraction of receptors in active state

**Equations** 

$$\frac{d\beta(x,y,t)}{dt} = s\Phi(\rho,\gamma) \qquad -\beta k_{\rm i} \qquad -\beta k_{\rm t} \qquad [1]$$

Rate of change in intracellular [cAMP] = Production of cAMP

$$\frac{d\gamma(x,y,t)}{dt} = \frac{k_t}{h}\beta \qquad -k_c\gamma \qquad +D\nabla^2\gamma \quad [2]$$

Rate of change in extracellular [cAMP] = Secretion of cAMP

$$\frac{d\rho(x,y,t)}{dt} = f_2(\gamma)(1-\rho) \qquad -f_1(\gamma)\rho$$
 [3]

Positive Feedback Loop

- Extracellular cAMP increases (γ increases)
- ⇒ Rate of synthesis of intracellular cAMP increases

(Φ increases)

- ⇒ Intracellular cAMP increases (β increases)
- ⇒ Rate of secretion of cAMP increases
- (⇒ Extracellular cAMP increases)

See Equations

## Negative Feedback Loop

- · Extracellular cAMP increases (γ increases)
- ⇒ cAMP receptors desensitize  $(f_1 \text{ increases}, f_2 \text{ decreases}, \rho \text{ decreases})$
- ⇒ Rate of synthesis of intracellular cAMP
  - (Φ decreases)
- ⇒ Intracellular cAMP decreases
- ⇒ Rate of secretion of cAMP decreases
- ⇒ Extracellular cAMP decreases

(γ decreases)

See Equations

Dynamics of Model

- Unperturbed ⇒ cAMP concentration reaches steady state
- Small perturbation in extracellular cAMP ⇒ returns to steady state
- Perturbation > threshold ⇒ large transient in cAMP, then return to steady state
- Or oscillation (depending on model parameters)

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#### Circular & Spiral Waves Observed in:

- · Slime mold aggregation
- Chemical systems (e.g., BZ reaction)
- · Neural tissue
- · Retina of the eye
- · Heart muscle
- · Intracellular calcium flows
- · Mitochondrial activity in oocytes

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#### Cause of Concentric Circular Waves

- · Excitability is not enough
- But at certain developmental stages, cells can operate as pacemakers
- When stimulated by cAMP, they begin emitting regular pulses of cAMP

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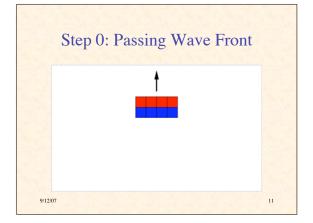
#### Spiral Waves

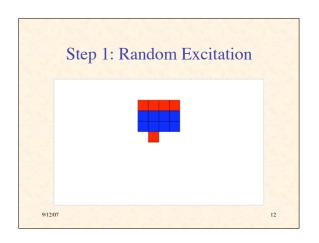
- Persistence & propagation of spiral waves explained analytically (Tyson & Murray,
- · Rotate around a small core of of nonexcitable cells
- Propagate at higher frequency than circular
- · Therefore they dominate circular in collisions
- But how do the spirals form initially?

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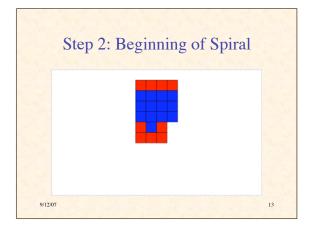
### Some Explanations of Spiral Formation

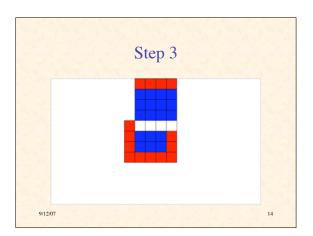
- "the origin of spiral waves remains obscure"
- · Traveling wave meets obstacle and is broken
- · Desynchronization of cells in their developmental path
- · Random pulse behind advancing wave front

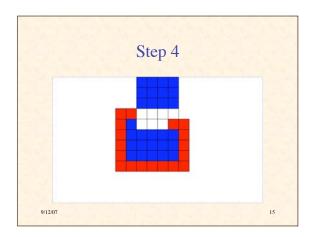


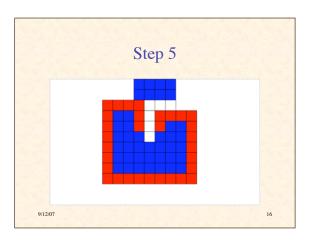


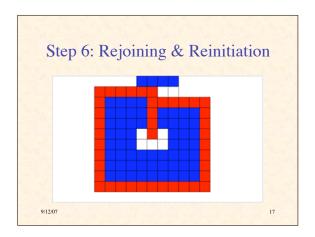
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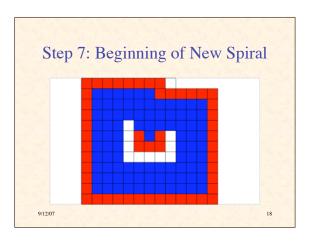




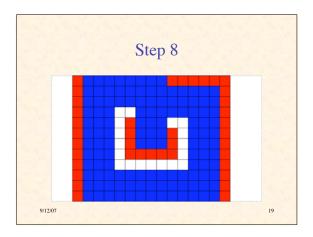


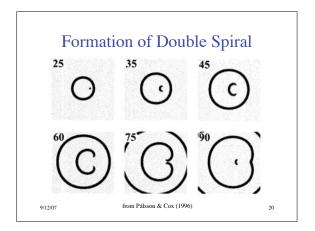






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#### NetLogo Simulation Of Spiral Formation

- Amoebas are immobile at timescale of wave movement
- A fraction of patches are inert (grey)
- A fraction of patches has initial concentration of cAMP
- At each time step:
  - chemical diffuses
  - each patch responds to local concentration

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#### Response of Patch

if patch is not refractory (brown) then
if local chemical > threshold then
set refractory period
produce pulse of chemical (red)

#### else

decrement refractory period degrade chemical in local area

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# Demonstration of NetLogo Simulation of Spiral Formation

Run SlimeSpiral.nlogo

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#### Observations

- Excitable media can support circular and spiral waves
- Spiral formation can be triggered in a variety of ways
- All seem to involve inhomogeneities (broken symmetries):
  - in space
  - in time
  - in activity
- · Amplification of random fluctuations
- Circles & spirals are to be expected

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## NetLogo Simulation of Streaming Aggregation

- 1. chemical diffuses
- 2. **if** cell is refractory (yellow)
- 3. then chemical degrades
- 4. **else** (it's excitable, colored white)
  - if chemical > movement threshold then
     take step up chemical gradient
  - else if chemical > relay threshold then produce more chemical (red) become refractory
  - 3. else wait

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Demonstration of NetLogo Simulation of Aggregation (Spiral & Streaming Phases)

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