VII. Cooperation & Competition

The Iterated Prisoner's Dilemma

The Prisoners' Dilemma

- Devised by Melvin Dresher & Merrill Flood in 1950 at RAND Corporation
- Further developed by mathematician Albert W. Tucker in 1950 presentation to psychologists
- It "has given rise to a vast body of literature in subjects as diverse as philosophy, ethics, biology, sociology, political science, economics, and, of course, game theory." — S.J. Hagenmayer
- "This example, which can be set out in one page, could be the most influential one page in the social sciences in the latter half of the twentieth century." — R.A. McCain

Prisoners' Dilemma: The Story

- · Two criminals have been caught
- · They cannot communicate with each other
- If both confess, they will each get 10 years
- If one confesses and accuses other:
 - confessor goes free
 - accused gets 20 years
- If neither confesses, they will both get 1 year on a lesser charge

Prisoners' Dilemma Payoff Matrix

	Bob		ob
		cooperate	defect
Ann	cooperate	-1,-1	-20,0
	defect	0, -20	-10, -10

- defect = confess, cooperate = don't
- payoffs < 0 because punishments (losses)

Ann's "Rational" Analysis (Dominant Strategy)

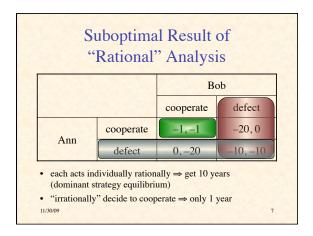
		Bob		
		cooperate	defect	
Ann	cooperate	-1, -1	-20,0	
	defect	0, –20	-10, -10	

- if cooperates, may get 20 years
- · if defects, may get 10 years
- .:., best to defect

Bob's "Rational" Analysis (Dominant Strategy)

		Bob		
		cooperate	defect	
	cooperate	-1,-1	-20,0	
Ann	defect	0, -20	[-10, -10]	

- if he cooperates, may get 20 years
- if he defects, may get 10 years
- :, best to defect



Summary

- Individually rational actions lead to a result that all agree is less desirable
- In such a situation you cannot act unilaterally in your own best interest
- Just one example of a (game-theoretic) dilemma
- Can there be a situation in which it would make sense to cooperate unilaterally?
 - Yes, if the players can expect to interact again in the future

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The Iterated Prisoners' Dilemma
and Robert Axelrod's Experiments

Assumptions

- No mechanism for enforceable threats or commitments
- · No way to foresee a player's move
- No way to eliminate other player or avoid interaction
- No way to change other player's payoffs
- Communication only through direct interaction

Axelrod's Experiments

- Intuitively, expectation of future encounters may affect rationality of defection
- Various programs compete for 200 rounds
 encounters each other and self
- Each program can remember:
 - its own past actions
 - its competitors' past actions
- 14 programs submitted for first experiment

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IPD Payoff Matrix

		В		
		cooperate	defect	
	cooperate	3,3	0,5	
A	defect	5,0	1,1	

N.B. Unless DC + CD < 2 CC (i.e. T + S < 2 R), can win by alternating defection/cooperation

Indefinite Number of Future Encounters

- Cooperation depends on expectation of indefinite number of future encounters
- Suppose a known finite number of encounters:
 - No reason to C on last encounter
 - Since expect D on last, no reason to C on next
 - And so forth: there is no reason to C at all

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Analysis of Some Simple Strategies

- Three simple strategies:
 - ALL-D: always defect
 - ALL-C: always cooperate
 - RAND: randomly cooperate/defect
- Effectiveness depends on environment
 - ALL-D optimizes local (individual) fitness
 - ALL-C optimizes global (population) fitness
 - RAND compromises

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Expected Scores

↓ playing ⇒	ALL-C	RAND	ALL-D	Average
ALL-C	3.0	1.5	0.0	1.5
RAND	4.0	2.25	0.5	2.25
ALL-D	5.0	3.0	1.0	3.0

Result of Axelrod's Experiments

- Winner is Rapoport's **TFT** (Tit-for-Tat)
 - cooperate on first encounter
 - reply in kind on succeeding encounters
- Second experiment:
 - 62 programs
 - all know TFT was previous winner
 - TFT wins again

Expected Scores						
↓ playing ⇒	ALL-C	RAND	ALL-D	TFT	Avg	
ALL-C	3.0	1.5	0.0	3.0	1.875	
RAND	4.0	2.25	0.5	2.25	2.25	
ALL-D	5.0	3.0	1.0	1+4/N	2.5+	
TFT	3.0	2.25	1–1/ <i>N</i>	3.0	2.3125-	
TFT	3.0		1–1/N	3	.0	

Demonstration of Iterated Prisoners' Dilemma

Run NetLogo demonstration
PD N-Person Iterated.nlogo

Characteristics of Successful Strategies

- Don't be envious
 - at best TFT ties other strategies
- · Be nice
 - i.e. don't be first to defect
- Reciprocate
 - reward cooperation, punish defection
- · Don't be too clever
 - sophisticated strategies may be unpredictable & look random; be clear

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Tit-for-Two-Tats

- More forgiving than TFT
- Wait for two successive defections before punishing
- Beats TFT in a noisy environment
- E.g., an unintentional defection will lead **TFT**s into endless cycle of retaliation
- May be exploited by feigning accidental defection

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Effects of Many Kinds of Noise Have Been Studied

- Misimplementation noise
- Misperception noise
 - noisy channels
- Stochastic effects on payoffs
- General conclusions:
 - sufficiently little noise ⇒ generosity is best
 - greater noise ⇒ generosity avoids unnecessary conflict but invites exploitation

More Characteristics of Successful Strategies

- Should be a generalist (robust)
 - i.e. do sufficiently well in wide variety of environments
- · Should do well with its own kind
 - since successful strategies will propagate
- · Should be cognitively simple
- Should be evolutionary stable strategy
 - i.e. resistant to invasion by other strategies

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Kant's Categorical Imperative

"Act on maxims that can at the same time have for their object themselves as universal laws of nature."

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Ecological & Spatial Models

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Ecological Model

- What if more successful strategies spread in population at expense of less successful?
- Models success of programs as fraction of total population
- Fraction of strategy = probability random program obeys this strategy

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Variables

- $P_i(t)$ = probability = proportional population of strategy i at time t
- $S_i(t)$ = score achieved by strategy i
- R_{ij}(t) = relative score achieved by strategy i playing against strategy j over many rounds
 fixed (not time-varying) for now

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Computing Score of a Strategy

- Let n = number of strategies in ecosystem
- Compute score achieved by strategy *i*:

$$S_i(t) = \sum_{k=1}^n R_{ik}(t) P_k(t)$$

$$\mathbf{S}(t) = \mathbf{R}(t)\mathbf{P}(t)$$

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Updating Proportional Population

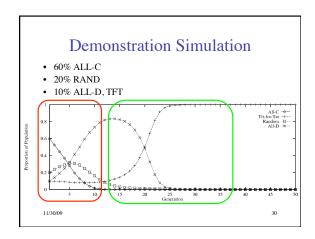
$$P_{i}(t+1) = \frac{P_{i}(t)S_{i}(t)}{\sum_{j=1}^{n} P_{j}(t)S_{j}(t)}$$

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Some Simulations

- Usual Axelrod payoff matrix
- 200 rounds per step

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NetLogo Demonstration of Ecological IPD

Run EIPD.nlogo

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Collectively Stable Strategy

- Let w = probability of future interactions
- Suppose cooperation based on reciprocity has been established
- Then no one can do better than **TFT** provided:

$$w \ge \max\left(\frac{T-R}{R-S}, \frac{T-R}{T-P}\right)$$

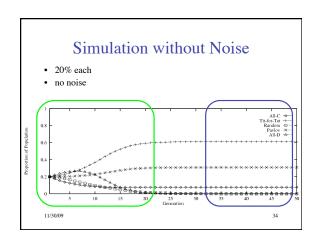
• The TFT users are in a Nash equilibrium

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"Win-Stay, Lose-Shift" Strategy

- Win-stay, lose-shift strategy:
 - begin cooperating
 - if other cooperates, continue current behavior
 - if other defects, switch to opposite behavior
- Called **PAV** (because suggests Pavlovian learning)

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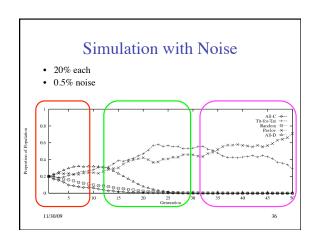


Effects of Noise

- Consider effects of noise or other sources of error in response
- TFT:
 - cycle of alternating defections (CD, DC)
 - broken only by another error
- · PAV
 - eventually self-corrects (CD, DC, DD, CC)
- can exploit ALL-C in noisy environment
- Noise added into computation of R_{ij}(t)

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Spatial Effects

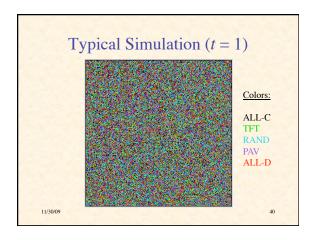
- Previous simulation assumes that each agent is equally likely to interact with each other
- So strategy interactions are proportional to fractions in population
- More realistically, interactions with "neighbors" are more likely
 - "Neighbor" can be defined in many ways
- Neighbors are more likely to use the same strategy

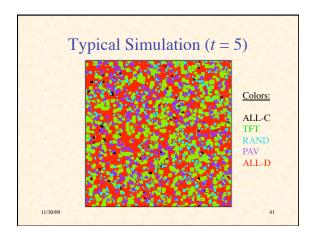
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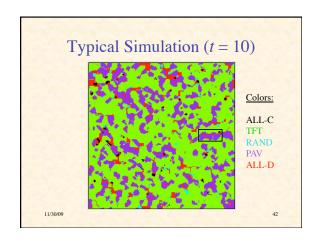
Spatial Simulation

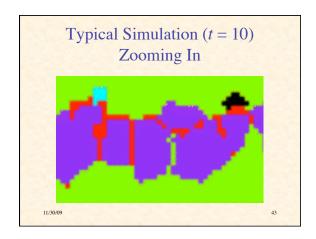
- Toroidal grid
- Agent interacts only with eight neighbors
- Agent adopts strategy of most successful neighbor
- · Ties favor current strategy

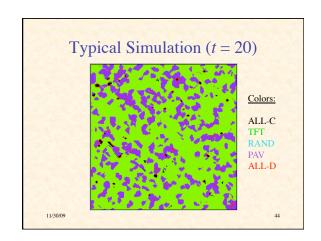
NetLogo Simulation of Spatial IPD Run SIPD.nlogo

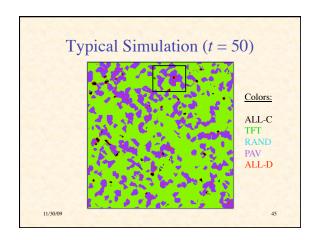


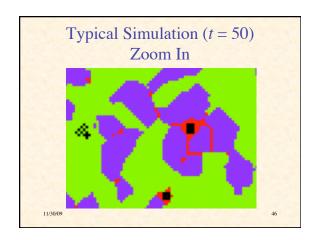


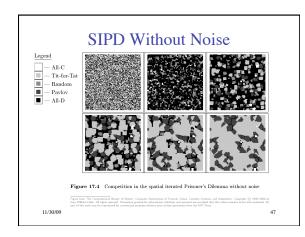












Conclusions: Spatial IPD • Small clusters of cooperators can exist in hostile environment • Parasitic agents can exist only in limited numbers • Stability of cooperation depends on expectation of future interaction • Adaptive cooperation/defection beats unilateral cooperation or defection

Additional Bibliography

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Part VIII