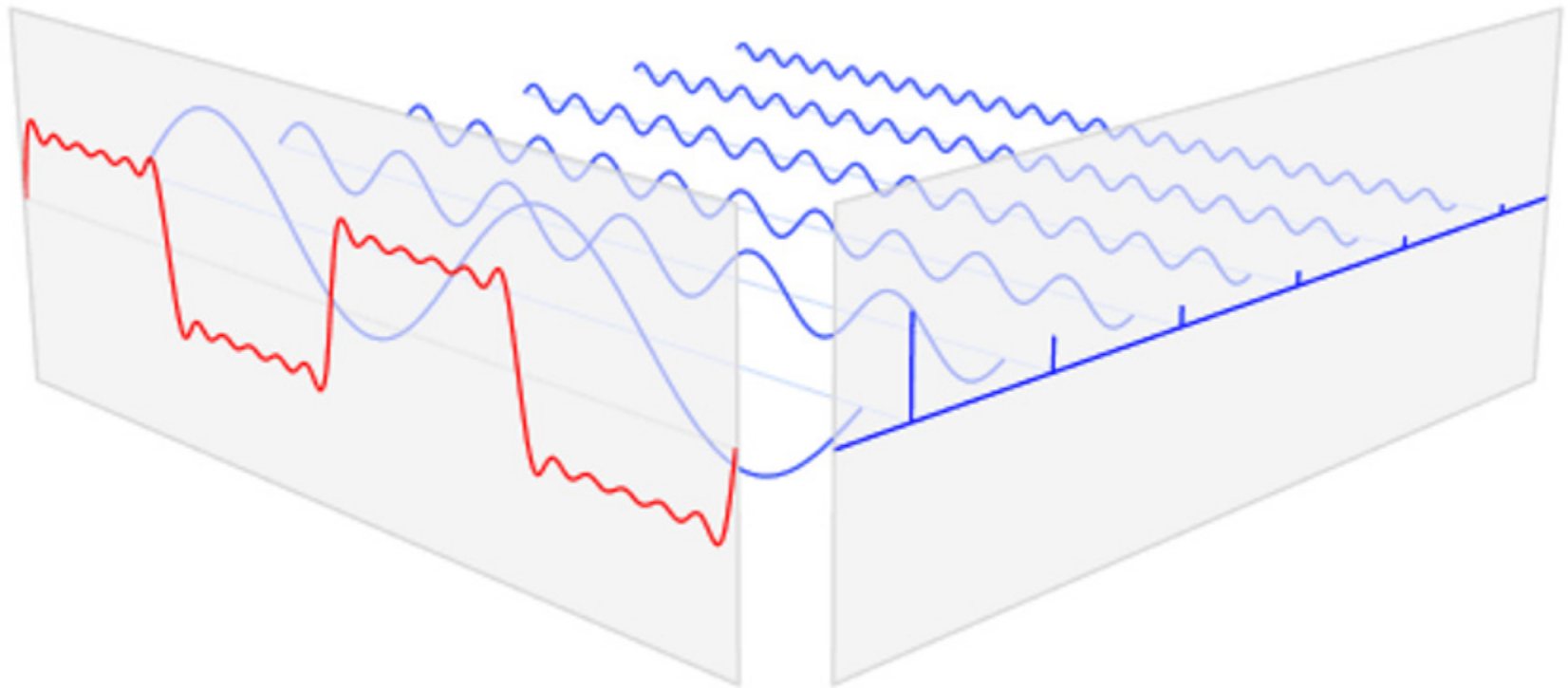


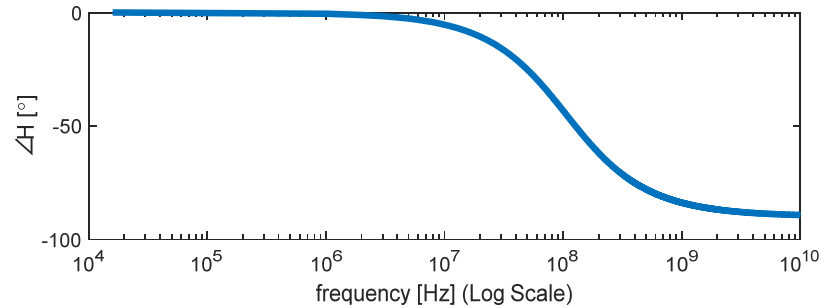
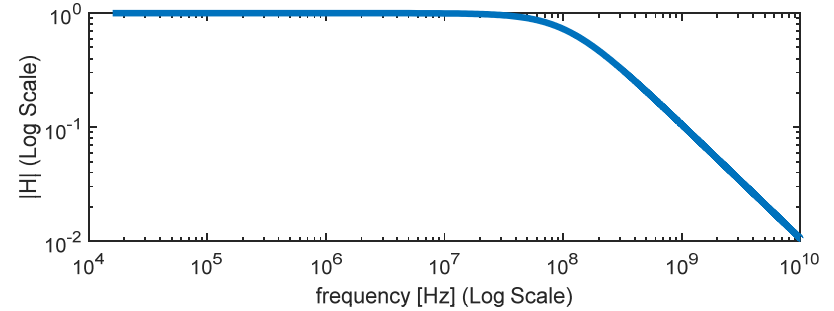
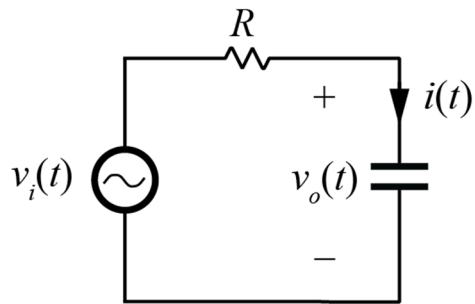
Fourier Series & Frequency Domain



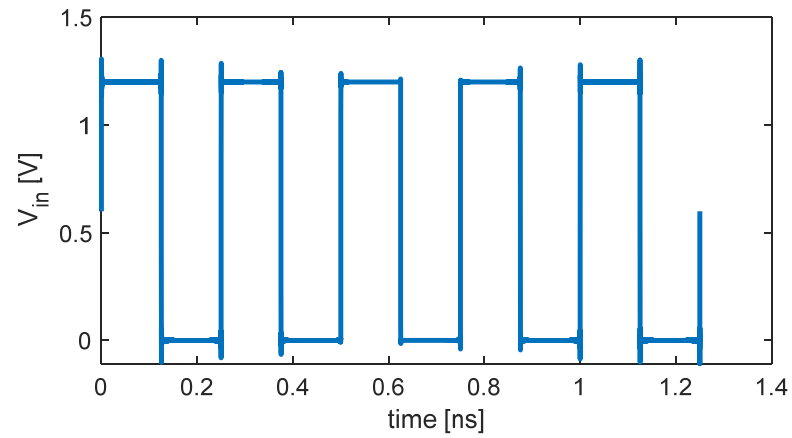
Input Spectrum



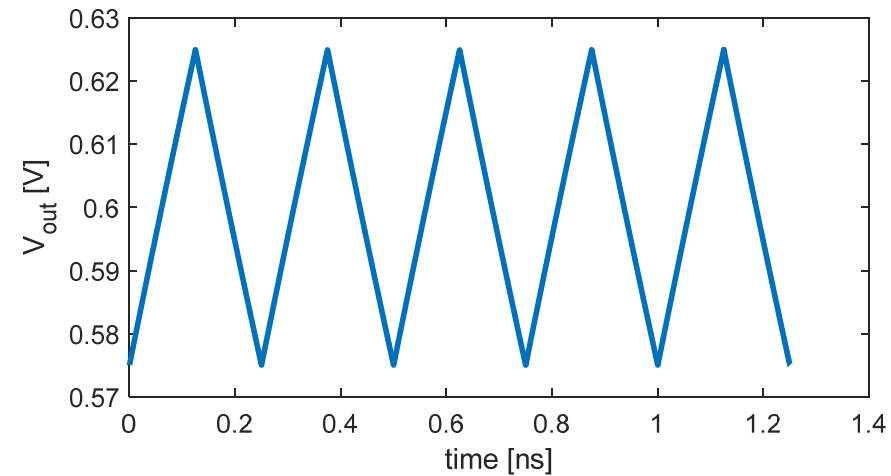
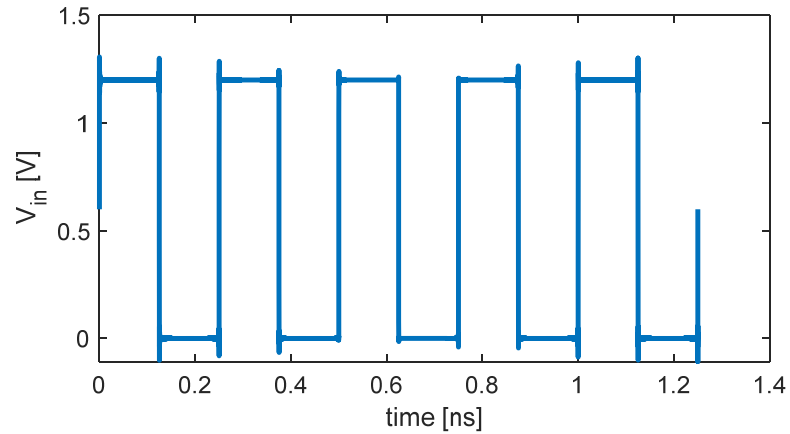
Application: Digital Communication



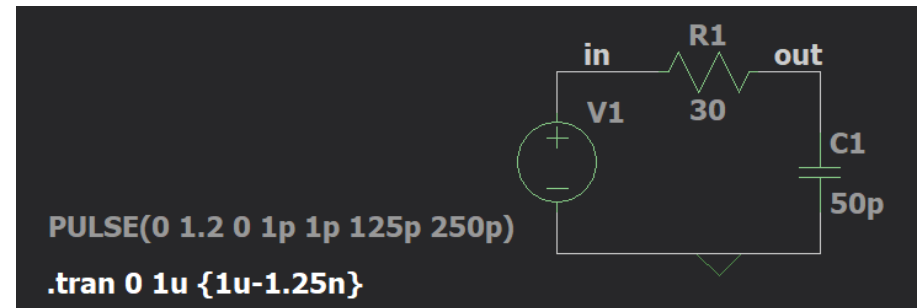
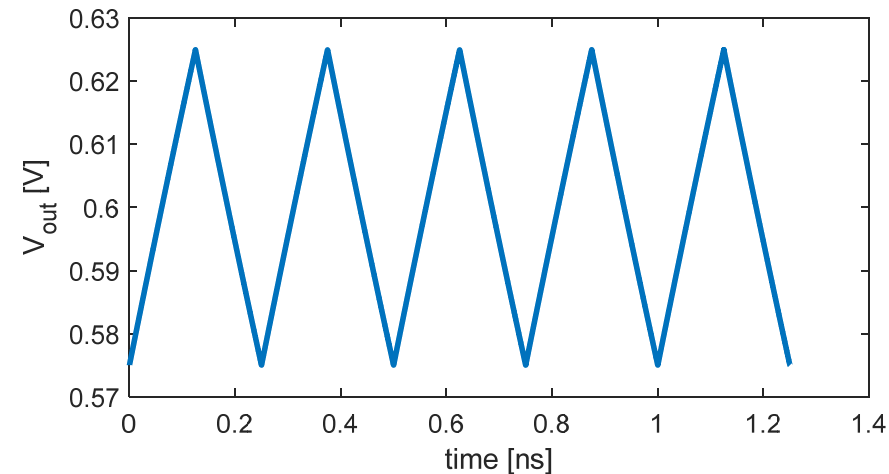
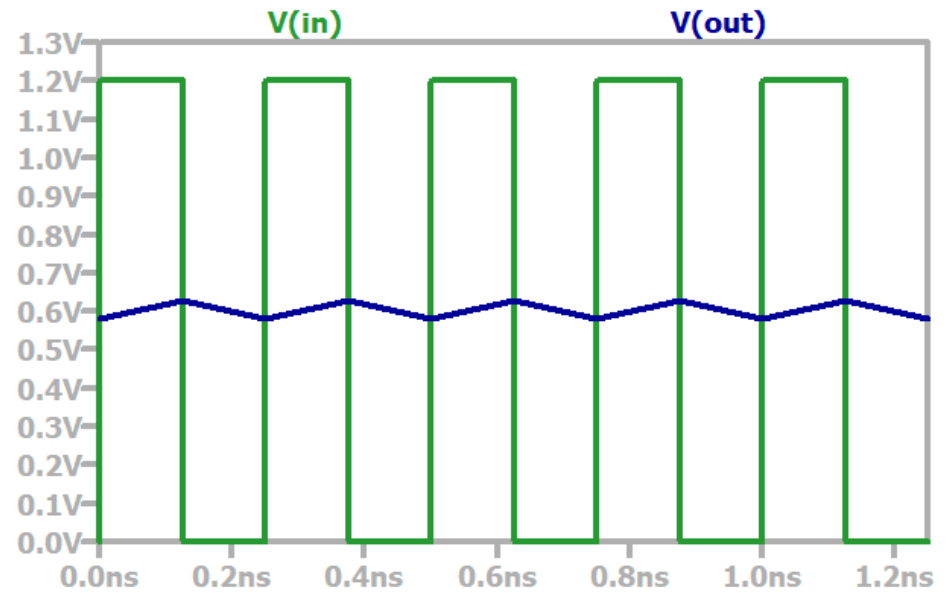
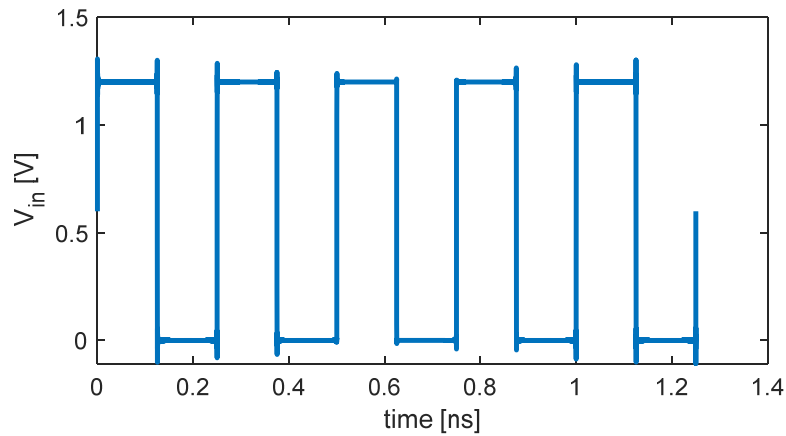
Applying Superposition



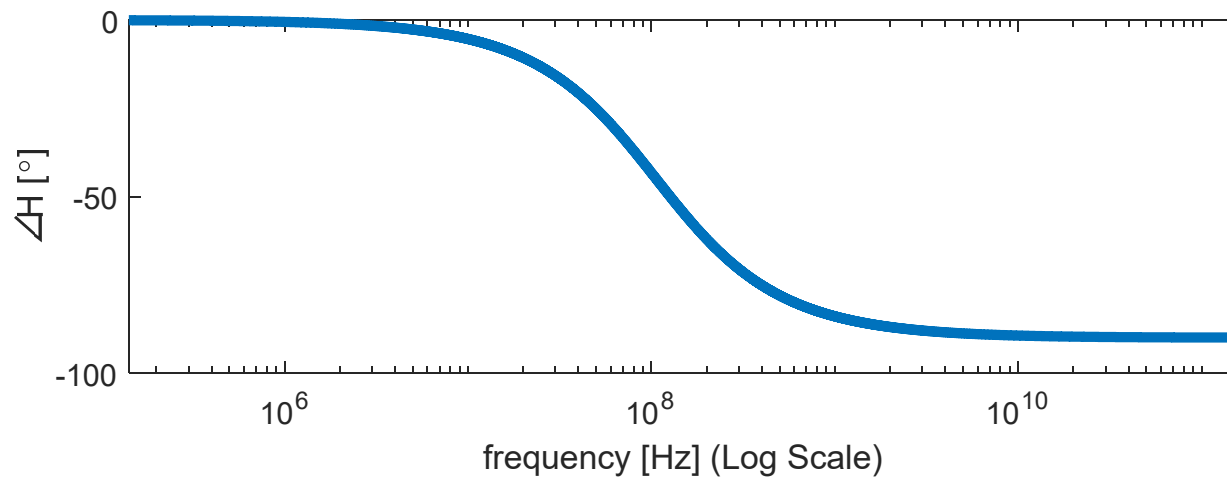
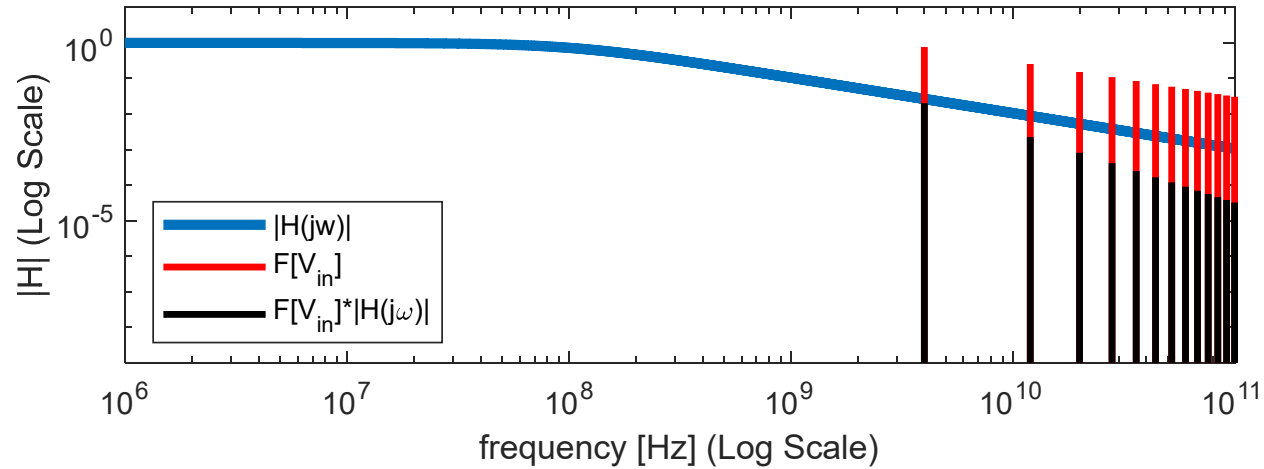
Calculated Output Voltage

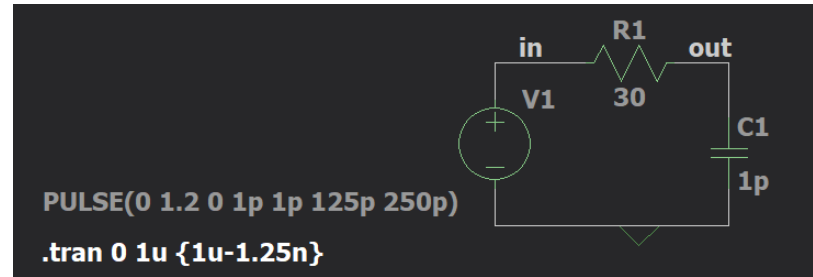
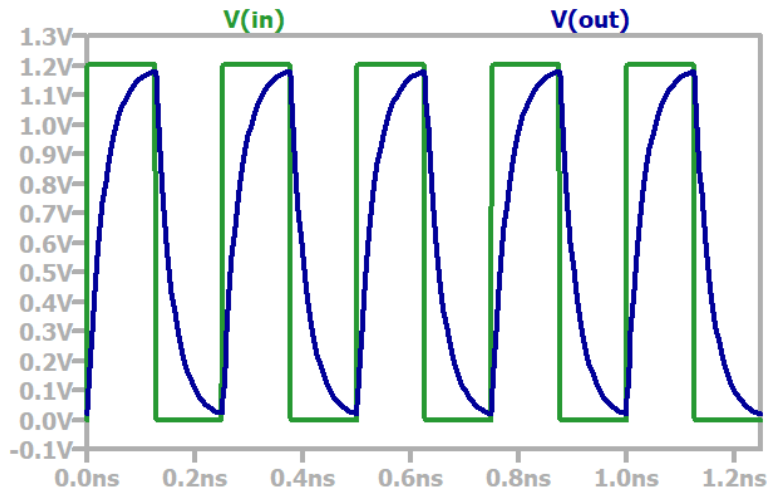


Simulation Verification



Frequency Domain Interpretation





Complex Form of Fourier Series

Fourier Series Representation

Assume we have some function $f(t)$ which is periodic with period $T_0 = \frac{2\pi}{\omega_0}$

$$f(t) = a_0 + \sum_{k=1}^{\infty} a_k \cos(k\omega_0 t) + b_k \sin(k\omega_0 t)$$

$$a_k = \frac{2}{T_0} \int_{t_0}^{t_0+T_0} f(t) \cos(k\omega_0 t) dt$$

$$b_k = \frac{2}{T_0} \int_{t_0}^{t_0+T_0} f(t) \sin(k\omega_0 t) dt$$

$f(t)$ can be expressed this way if

1. $f(t)$ is single-valued
2. $\int_{t_0}^{t_0+T_0} |f(t)| dt$ exists
3. $f(t)$ had finite discontinuities and max/min per period

Alternate forms

$$f(t) = a_0 + \sum_{k=1}^{\infty} A_k \cos(k\omega_0 t + \varphi_k) \quad \left\{ \begin{array}{l} A_k = \sqrt{a_k^2 + b_k^2} \\ \varphi_k = \tan^{-1} \left(\frac{b_k}{a_k} \right) \end{array} \right.$$

$$f(t) = \sum_{k=-\infty}^{\infty} c_k e^{jk\omega_0 t} \quad \left\{ \begin{array}{l} c_k = \frac{1}{2} (a_k - jb_k) \\ c_{-k} = \frac{1}{2} (a_k + jb_k) \\ c_0 = a_0 \end{array} \right.$$

$$c_k = \frac{1}{T_0} \int_{t_0}^{t_0+T_0} f(t) e^{-jk\omega_0 t} dt$$

Non-periodic Waveforms: Fourier Transform