

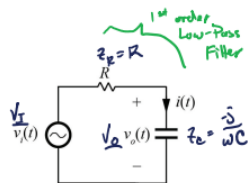
# Frequency Response

L18

## Frequency Response

$$V_o = V_s \frac{Z_c}{Z_R + Z_c} = V_s \frac{\frac{j\omega C}{j\omega C - \frac{1}{RC}}}{1 - \frac{j\omega RC}{1}} = V_s \frac{1}{j\omega RC + 1}$$

$$\frac{V_o}{V_s} = \frac{1}{j\omega RC + 1} \rightarrow \frac{V_o}{V_s} \equiv H(j\omega) = \text{Frequency Response}$$



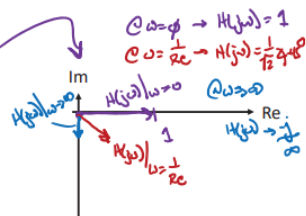
$H(j\omega)$  is the Frequency Response. It is some complex number with  $\omega$  as a variable that tells us the gain & phase shift of our output compared to the input

$$H(j\omega) = |H| \angle \angle H$$

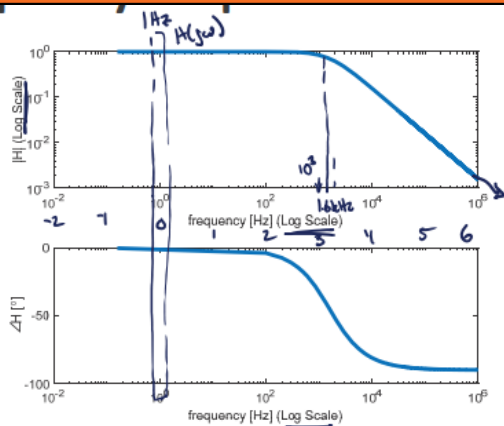
$$A(j\omega) = \frac{1}{j\omega RC + 1} = \frac{1}{\sqrt{1^2 + (\omega RC)^2}} \angle -\tan^{-1}(\omega RC)$$

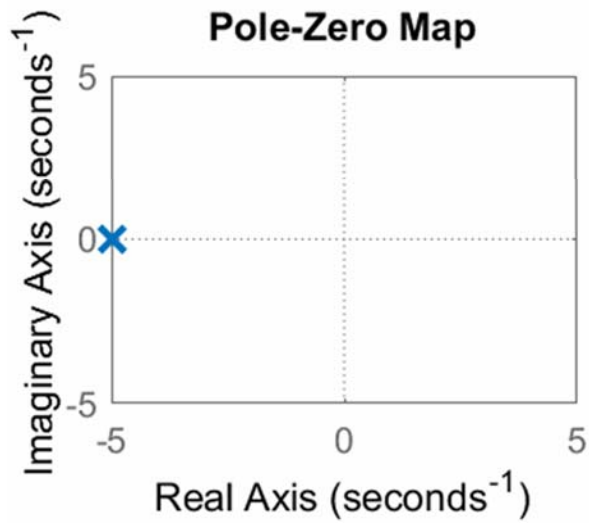
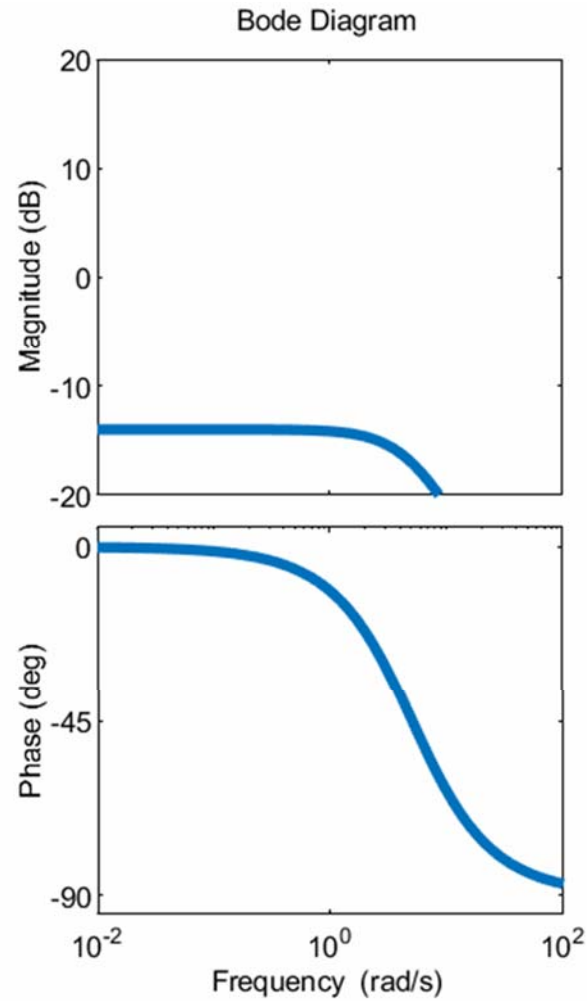
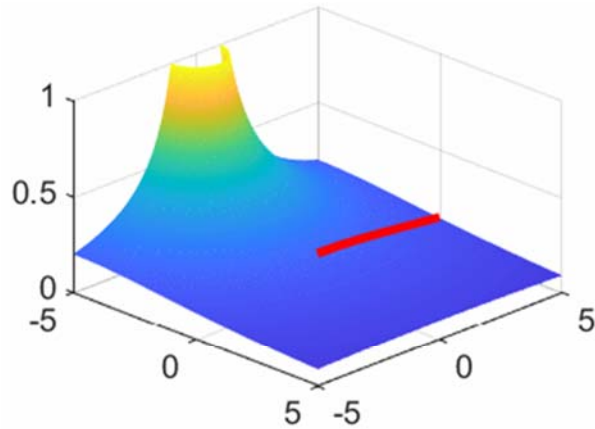
output is:

$$V_o = V_s A(j\omega) = \underbrace{|H|}_{\text{Magnitudes multiply}} \angle \underbrace{\angle H}_{\text{phases add}}$$

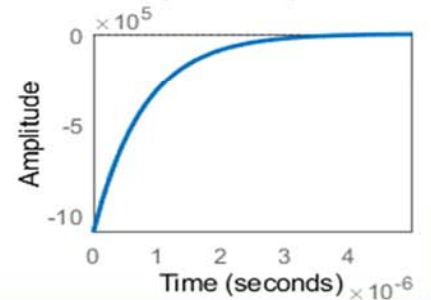
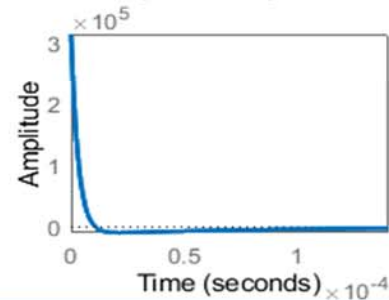
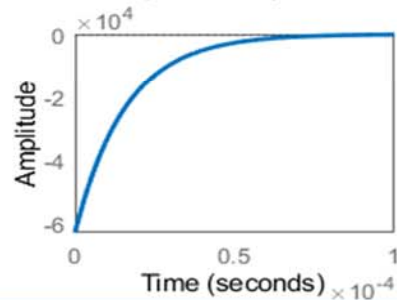
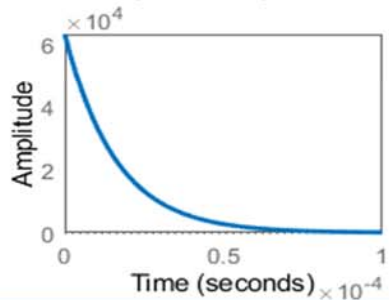
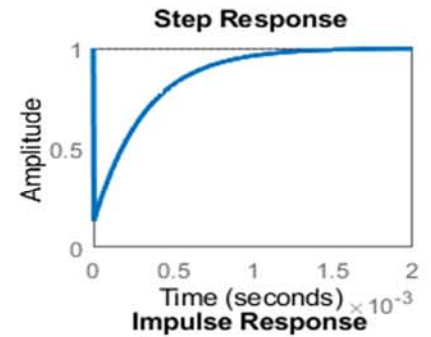
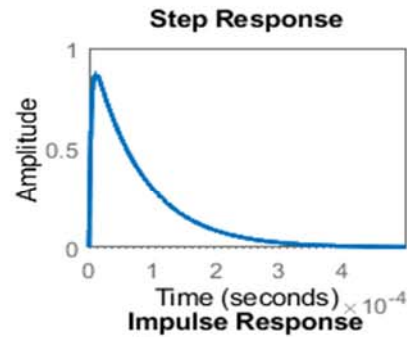
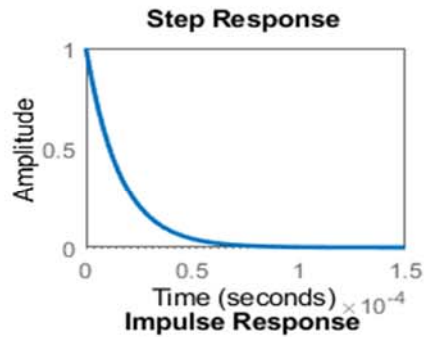
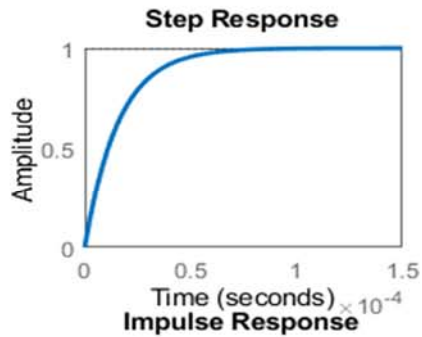
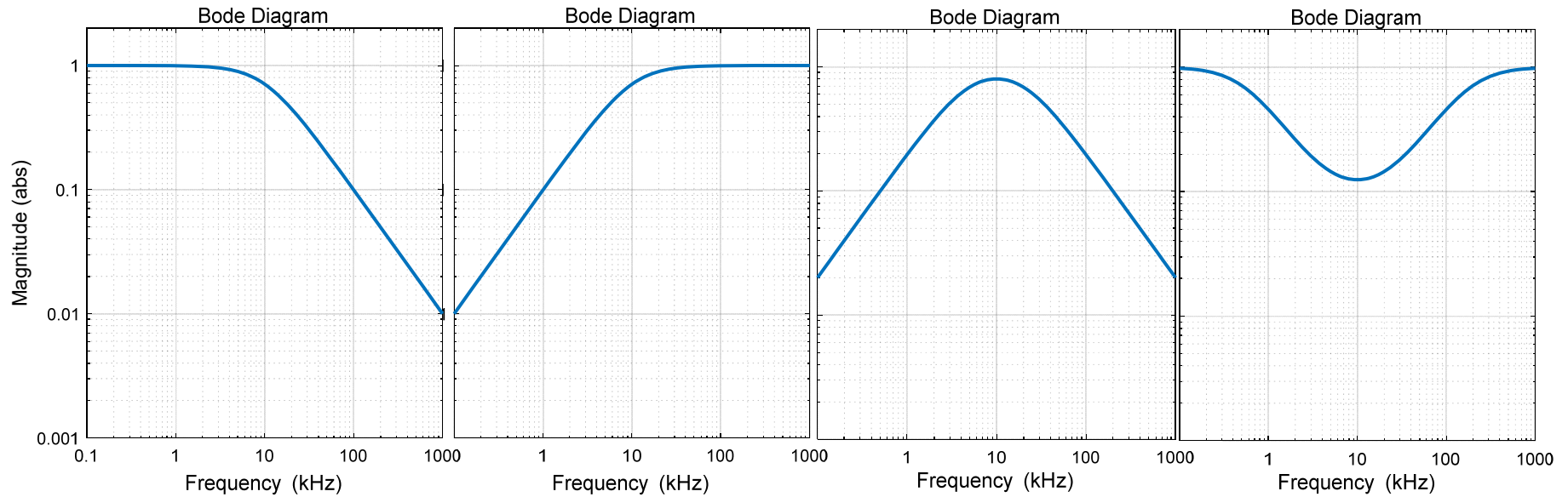


THE UNIVERSITY OF TENNESSEE KNOXVILLE

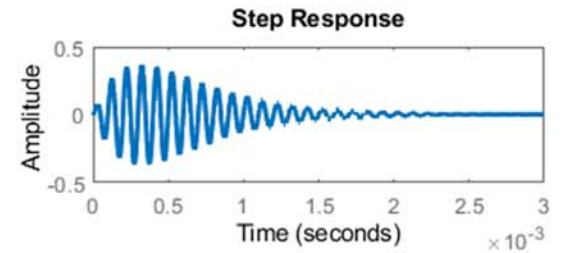
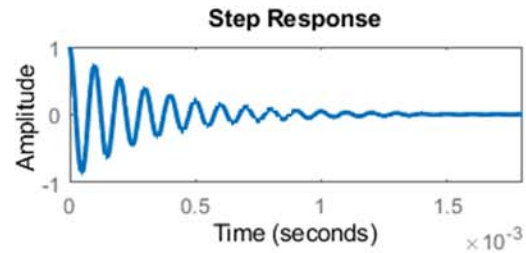
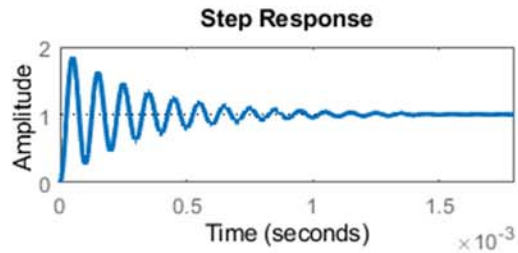
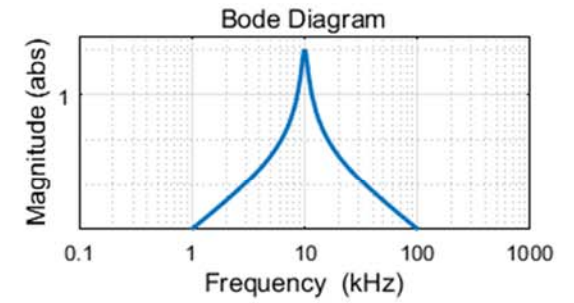
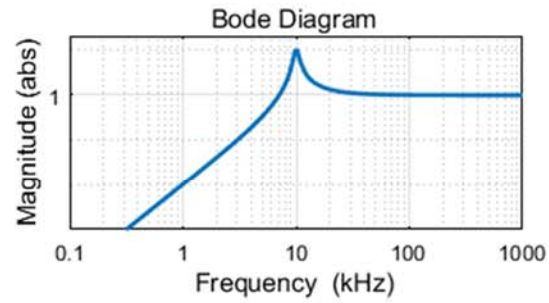
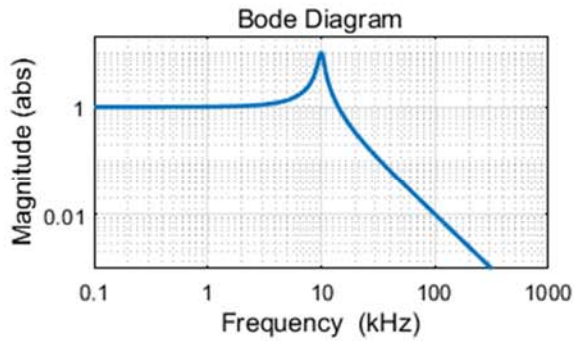




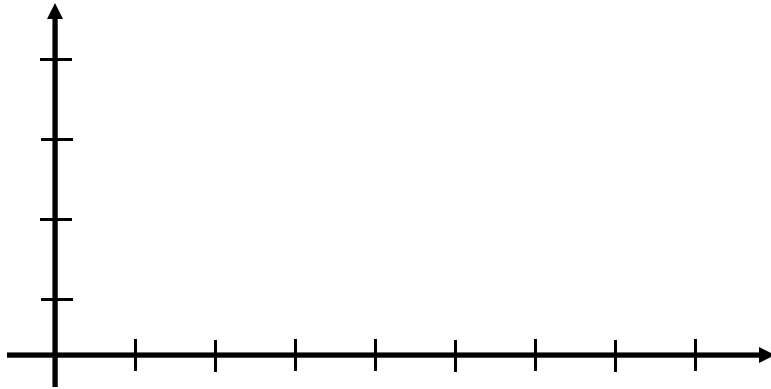
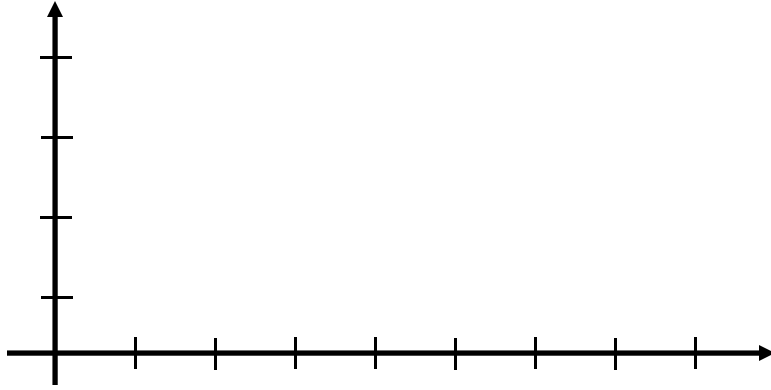
# Frequency Response and Circuit Behavior



# Complex Poles



# Bode Plots



# dB Scale

## Decibels

$$\|G\|_{\text{dB}} = 20 \log_{10}(\|G\|)$$

*Decibels of quantities having units (impedance example): normalize before taking log*

$$\|Z\|_{\text{dB}} = 20 \log_{10}\left(\frac{\|Z\|}{R_{\text{base}}}\right)$$

Table 8.1. Expressing magnitudes in decibels

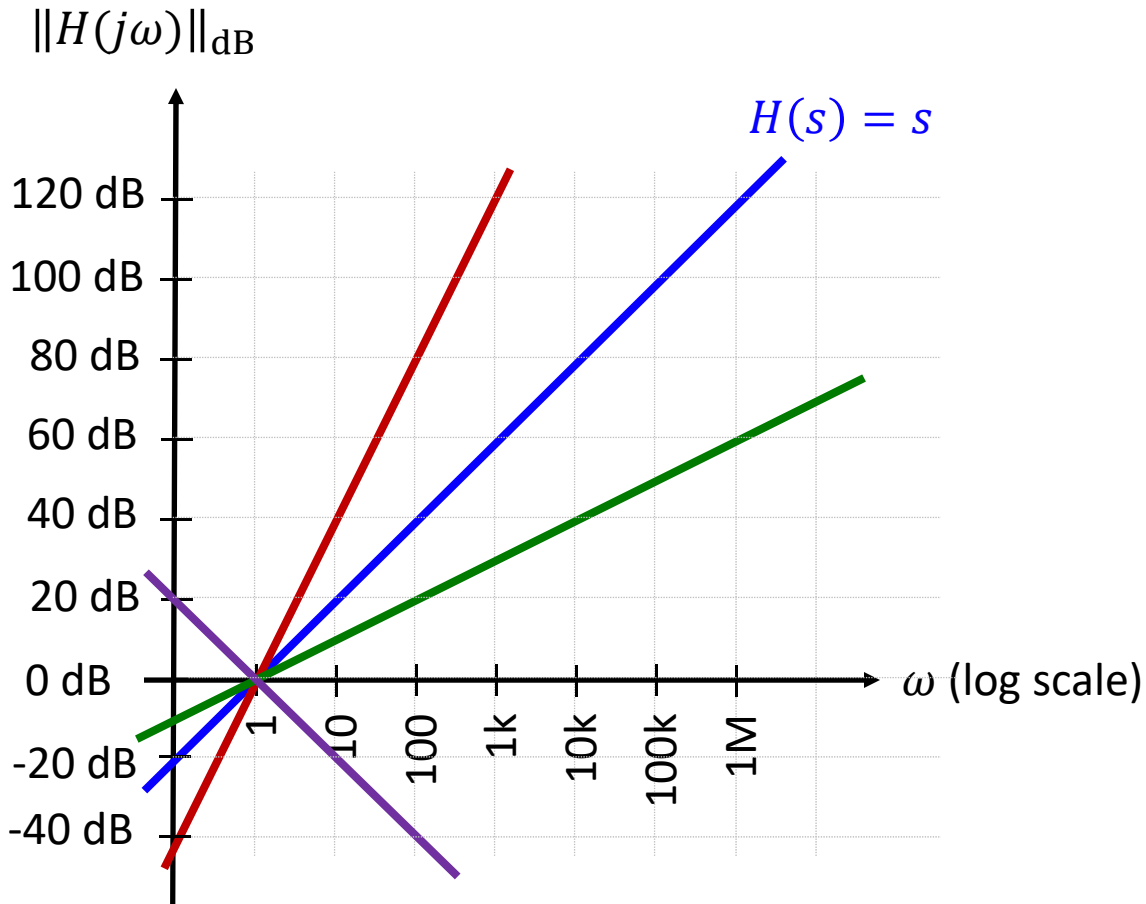
Actual magnitude	Magnitude in dB
1/2	- 6dB
1	0 dB
2	6 dB
5 = 10/2	20 dB - 6 dB = 14 dB
10	20dB
1000 = 10 <sup>3</sup>	3 · 20dB = 60 dB

5Ω is equivalent to 14dB with respect to a base impedance of  $R_{\text{base}} = 1\Omega$ , also known as 14dBΩ.

60dBμA is a current 60dB greater than a base current of 1μA, or 1mA.

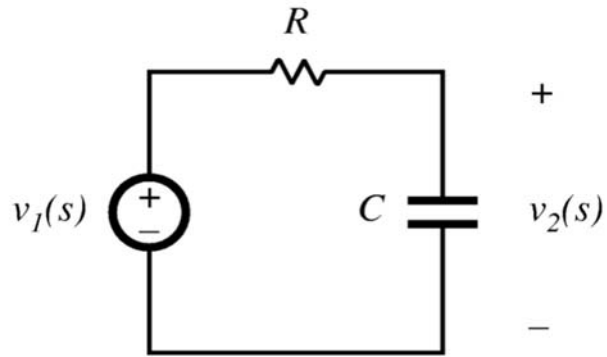
# Logarithm Review

# Plotting on Logarithmic Axes





# Single Pole Response



# Magnitude of Single Pole Response

# Asymptotic Behavior

