## CS 580 Homework 8

October 25 4:10 PM, 2023

1) Prove or disprove: If $S$ is a finite set of recursively enumerable languages that partition $\sum^{*}$, then every $L \in S$ is recursive.
2) Prove or disprove: If $L$ is an infinite recursively enumerable language, then there exists some $L^{\prime} \subseteq L$ such that $L^{\prime}$ is infinite and recursive.

3 ) In decimal, what is the index of the string 0101 ?
4) In human terms, what strings are in $L\left(M_{1056772669305988391}\right)$ ?
5) In binary, what is the smallest $i$ such that $L\left(M_{i}\right)=\emptyset$ ?
6) In binary, what is the smallest $i$ such that $L\left(M_{i}\right) \neq \emptyset$ ?
7) In binary, what is the smallest $i$ such that $L\left(M_{i}\right)=\{\lambda\}$ ?
8) In binary, what is the smallest $i$ such that $L\left(M_{i}\right)$ is infinite?
9) In binary, what is the smallest $i$ such that $L\left(M_{i}\right)=\sum^{*}$ ?
10) In binary, what is the smallest $i$ such that the encoding of $M_{i}$ is in $L\left(M_{i}\right)$ ?

