



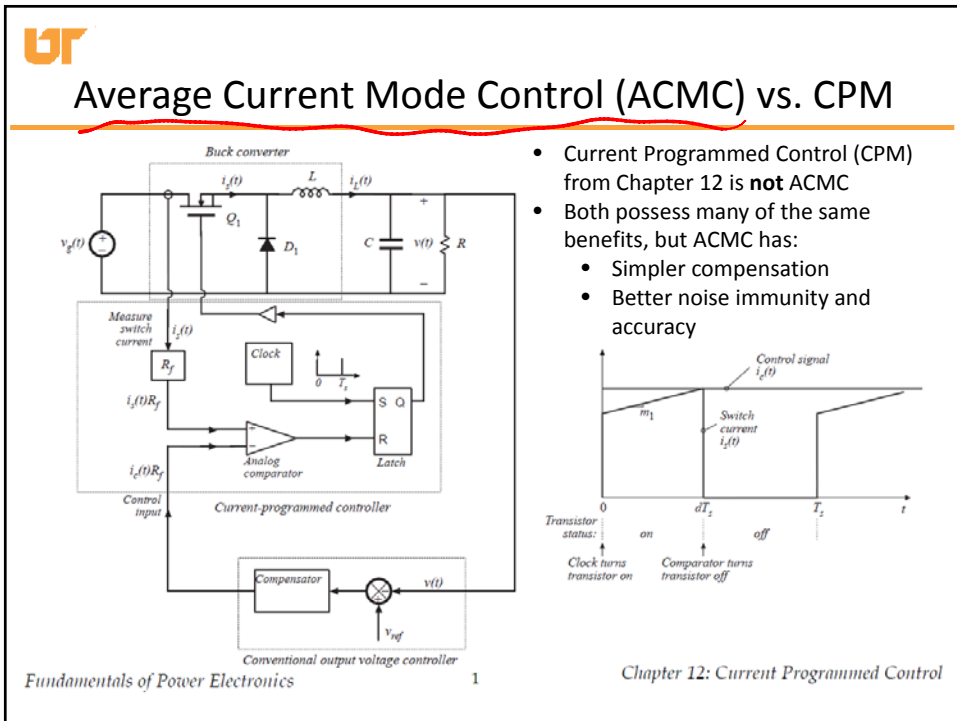
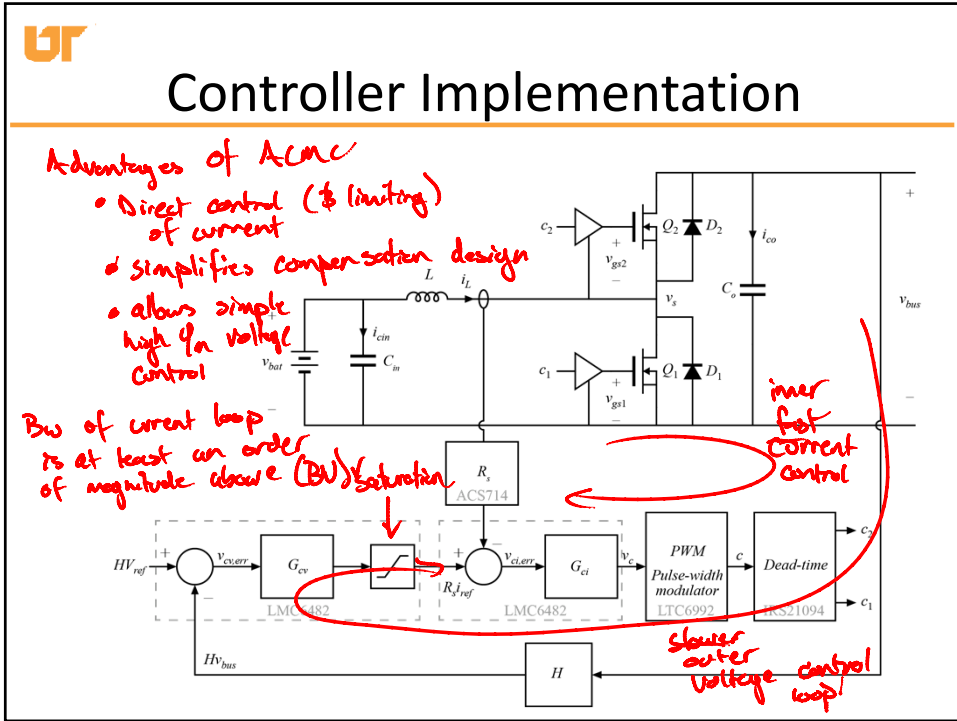
Boost Controller Design

ECE 482 Lecture 7
February 3, 2014



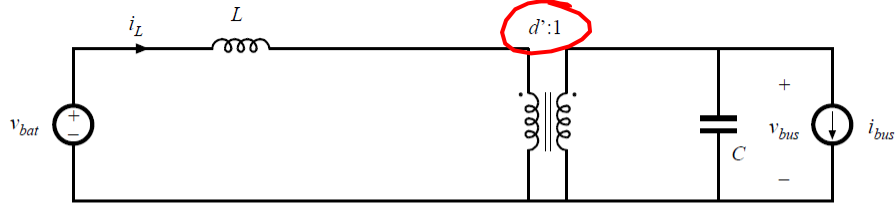
Announcements

- Experiment 1 Reports
 - Give all parameters needed to repeat
 - Reference *specific* features in figures/tables from text
- Experiment 2 Report due Friday
 - Demo full power in lab Wednesday
- Exp.3 prelab moved to Wednesday 2/12





Nonlinear, Averaged Circuit

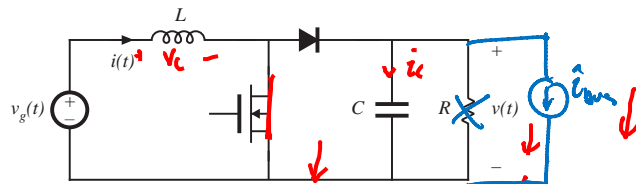


$$\left. \begin{aligned} L \frac{d\langle i_L \rangle}{dt} &= \langle v_{bat} \rangle - (1-d)\langle v_{bus} \rangle \\ C \frac{d\langle v_{bus} \rangle}{dt} &= (1-d)\langle i_L \rangle - \langle i_{bus} \rangle \end{aligned} \right\}$$

Suitable for simulation



Nonlinear, Large-Signal Equations



$$\begin{aligned} \langle v_L \rangle &= L \frac{d\langle i(t) \rangle}{dt} = d(t)\langle v_g(t) \rangle + d'(t)\langle v_g(t) \rangle - \langle v(t) \rangle \\ \langle i_C \rangle &= C \frac{d\langle v_C \rangle}{dt} = -\frac{\langle v \rangle}{R} \frac{d(t)}{dt} + d'(t)\langle i_p(t) \rangle - \frac{\langle v(t) \rangle}{R} \end{aligned}$$

DC only

$$\begin{aligned} \phi &= V_g - D'V \\ \phi &= D'I_L - \frac{V}{R} \end{aligned}$$

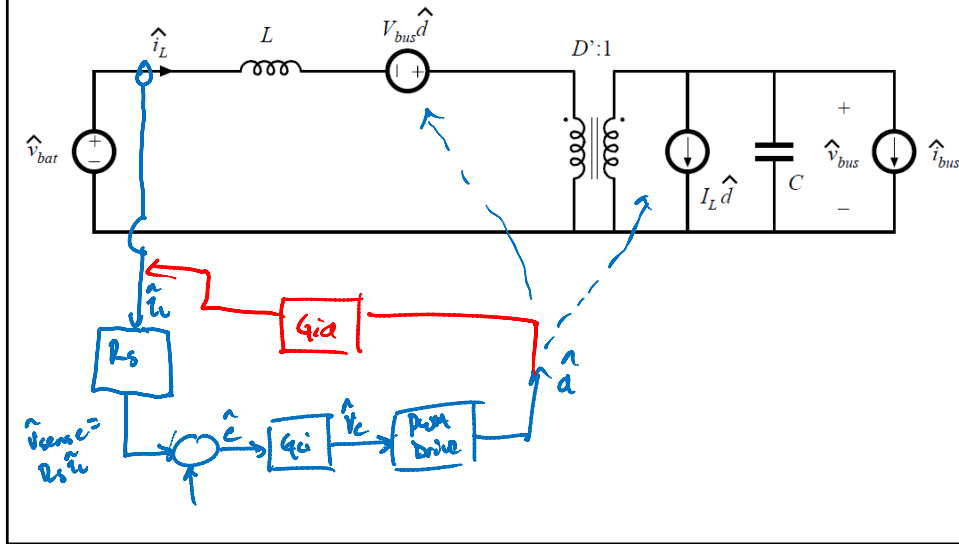
equiv. circuit model

$$\begin{cases} L \frac{d\hat{i}_L}{dt} = \hat{v}_g - D'\hat{v} + \hat{v}_d \\ C \frac{d\hat{v}_C}{dt} = -\frac{\hat{v}}{R} + D'\hat{i}_L - I_L d \end{cases}$$

$\uparrow \frac{\hat{v}}{R} = \hat{i}_{bus}$



Small-Signal AC Averaged Equiv. Circuit Model



Open-Loop Control-to-Current TF

Find $G_{id}(s) = \frac{\hat{i}_L}{\hat{d}} \Big|_{\hat{v}_{bat}=0, \hat{v}_{bus}=0}$

$$\hat{v}_c = \frac{1}{s} \hat{v}_c = \frac{1}{sL} (V_{bus} \hat{d} + \frac{D'I_c}{s} \hat{d} - \hat{c} \frac{D'I_c}{s^2 LC})$$

$$\hat{v}_c (1 + \frac{D'I_c}{s^2 LC}) = \hat{d} (\frac{V_{bus}}{s} + \frac{D'I_c}{s^2 LC})$$

$$G_{id} = \frac{\frac{V_{bus}}{s} + \frac{D'I_c}{s^2 LC}}{(1 + \frac{D'I_c}{s^2 LC})} = \frac{(1 + \frac{C V_{bus}}{D'I_c} s)}{(\frac{s^2 LC}{D'I_c} + \frac{D'I_c}{I_c})}$$



Open-Loop Control-to-Current TF

$$G_{id} = \frac{I_L}{D'} \frac{\left(1 + s \frac{CV_{bus}}{D'I_L}\right)}{\left(1 + s^2 \frac{LC}{D'L}\right)}$$

$$= G_{ido} \frac{\left(1 + \frac{s}{\omega_{zi}}\right)}{\left(1 + \frac{s^2}{\omega_o^2}\right)}$$

DC solution:

$$D'I_L = I_{bus}$$

$$\omega_{zi} = \frac{I_{bus}}{CV_{bus}}$$



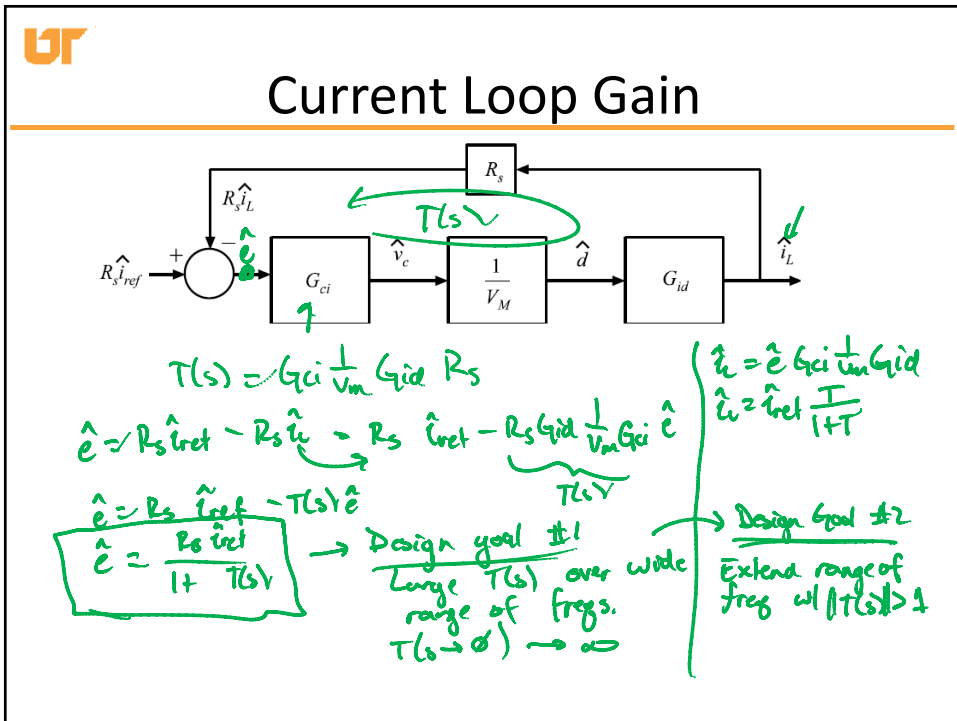
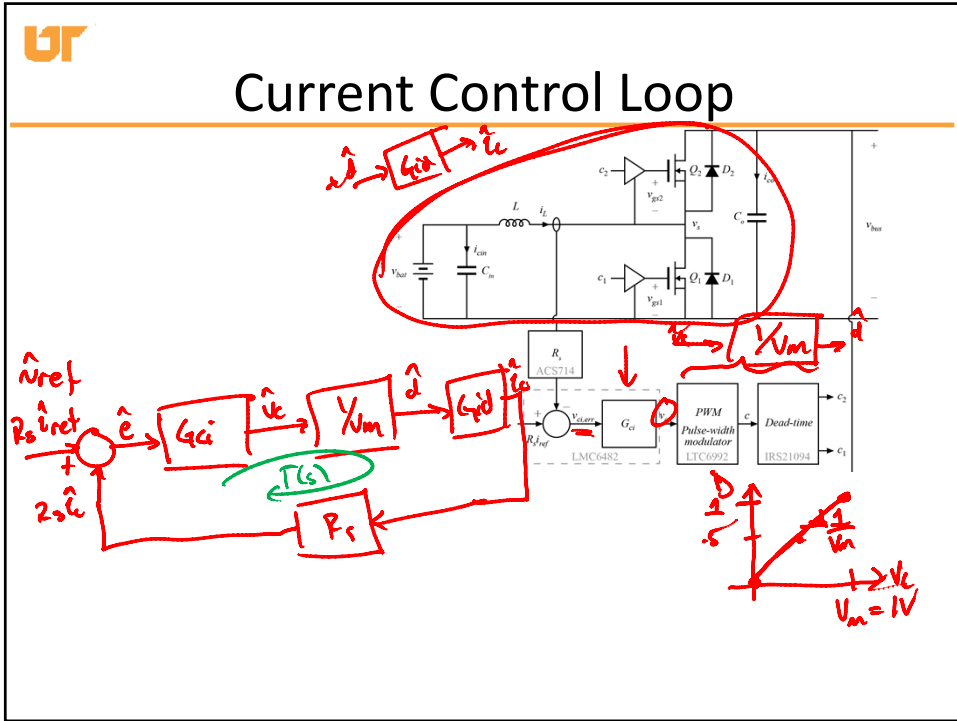
Open-Loop Control-to-Current TF

$$G_{id}(s) = \frac{\hat{i}_L}{\hat{d}} \Big|_{\hat{v}_{bat}=0, \hat{i}_{bus}=0} = G_{ido} \frac{1 + \frac{s}{\omega_{zi}}}{1 + \frac{s^2}{\omega_o^2}}$$

$$G_{ido} = \frac{I_L}{D'} = \frac{I_{bus}}{(D')^2}$$

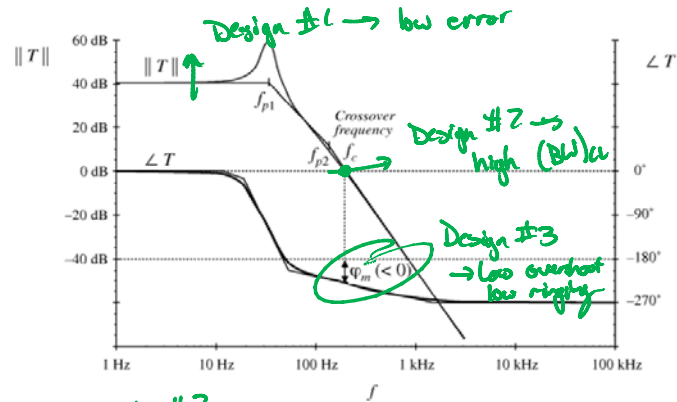
$$f_{zi} = \frac{1}{2\pi} \frac{1}{C} \frac{I_{bus}}{V_{bus}} \leftarrow$$

$$f_o = \frac{1}{2\pi} \frac{D'}{\sqrt{LC}}$$





Loop Gain & Stability



Design Goal #3
 system well stabilized
 → large PM



Phase Margin Test

System stable if

$$\phi_m = 180^\circ + \angle T(j\omega_c) \geq 0^\circ$$

$$(\omega_c \Rightarrow \|T(j\omega_c)\| = 1 = 0 \text{ dB})$$



Closed-Loop Response

