

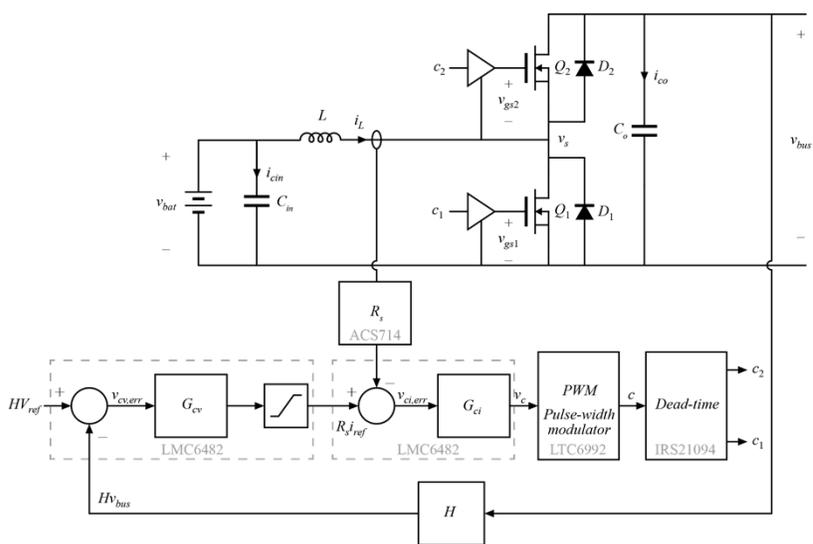


# Boost Controller Design

ECE 482 Lecture 7  
February 3, 2014

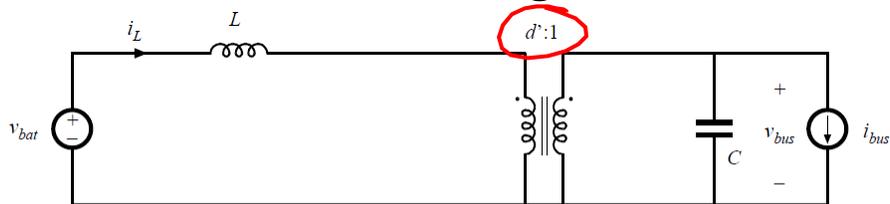


# Controller Implementation





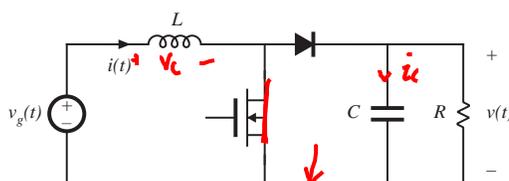
## Nonlinear, Averaged Circuit



$$\left. \begin{aligned} L \frac{d\langle i_L \rangle}{dt} &= \langle v_{bat} \rangle - (1-d)\langle v_{bus} \rangle \\ C \frac{d\langle v_{bus} \rangle}{dt} &= (1-d)\langle i_L \rangle - \langle i_{bus} \rangle \end{aligned} \right\}$$



## Nonlinear, Large-Signal Equations



$$\langle v_c \rangle = L \frac{d\langle i_c \rangle}{dt} = d(t) \langle v_g(t) \rangle + d'(t) (\langle v_g(t) \rangle - \langle v(t) \rangle)$$

$$\langle i_c \rangle = C \frac{d\langle v(t) \rangle}{dt} = -\frac{\langle v \rangle}{R} \frac{d(t)}{dt} + d'(t) (\langle i_c(t) \rangle - \frac{\langle v(t) \rangle}{R})$$

DC only

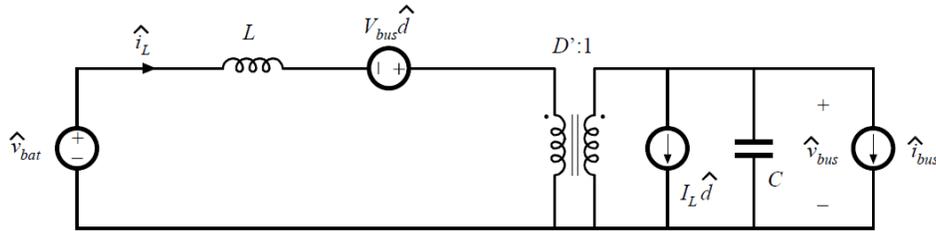
$$\begin{aligned} \phi &= V_g - D'V \\ \phi &= D'I_c - \frac{V}{R} \end{aligned}$$

$$L \frac{d\hat{i}_c}{dt} = \hat{v}_g - D'\hat{v} + \hat{v}d$$

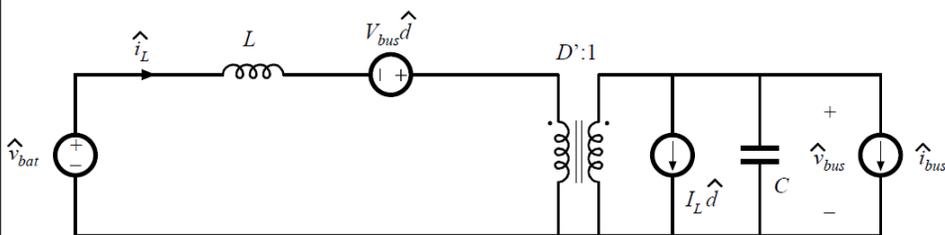
$$C \frac{d\hat{v}}{dt} = -\frac{\hat{v}}{R} + D'\hat{i}_c - I_c d$$



## Small-Signal AC Averaged Equic. Circuit Model



## Open-Loop Control-to-Current TF



Find  $G_{id}(s) = \left. \frac{\hat{i}_L}{\hat{d}} \right|_{\hat{v}_{bat}=0, \hat{i}_{bus}=0}$



## Open-Loop Control-to-Current TF



## Open-Loop Control-to-Current TF

$$G_{id}(s) = \left. \frac{\hat{i}_L}{\hat{d}} \right|_{\hat{v}_{bat}=0, \hat{i}_{bus}=0} = G_{ido} \frac{1 + \frac{s}{\omega_{zi}}}{1 + \frac{s}{\omega_o^2}}$$

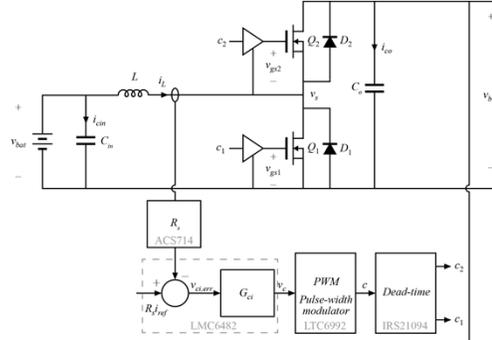
$$G_{ido} = \frac{I_L}{D'} = \frac{I_{bus}}{(D')^2}$$

$$f_{zi} = \frac{1}{2\pi} \frac{1}{C} \frac{I_{bus}}{V_{bus}}$$

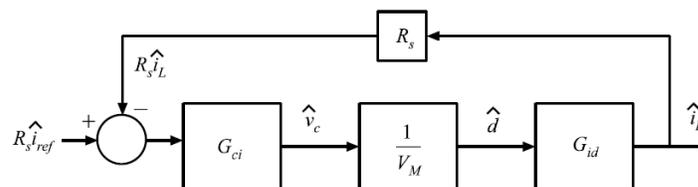
$$f_o = \frac{1}{2\pi} \frac{D'}{\sqrt{LC}}$$



## Current Control Loop

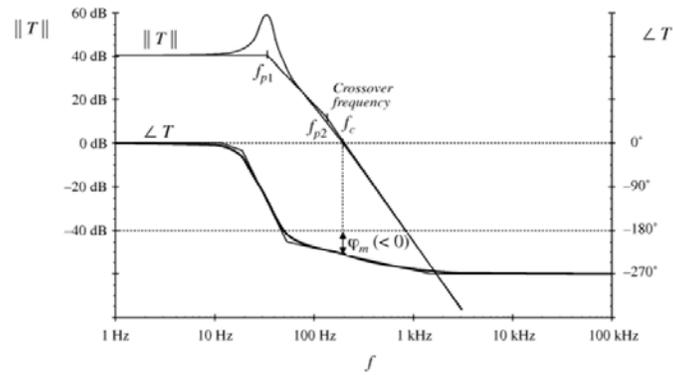


## Current Loop Gain





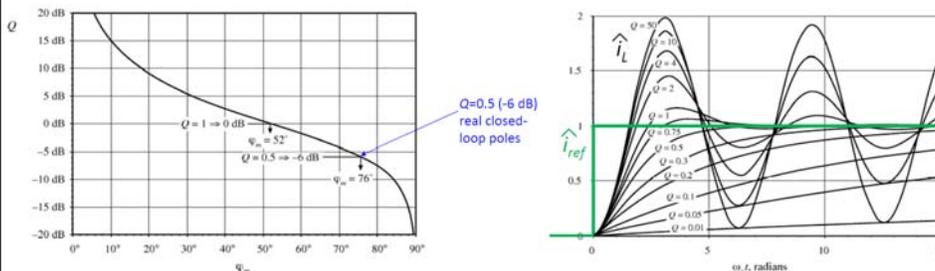
## Loop Gain & Stability



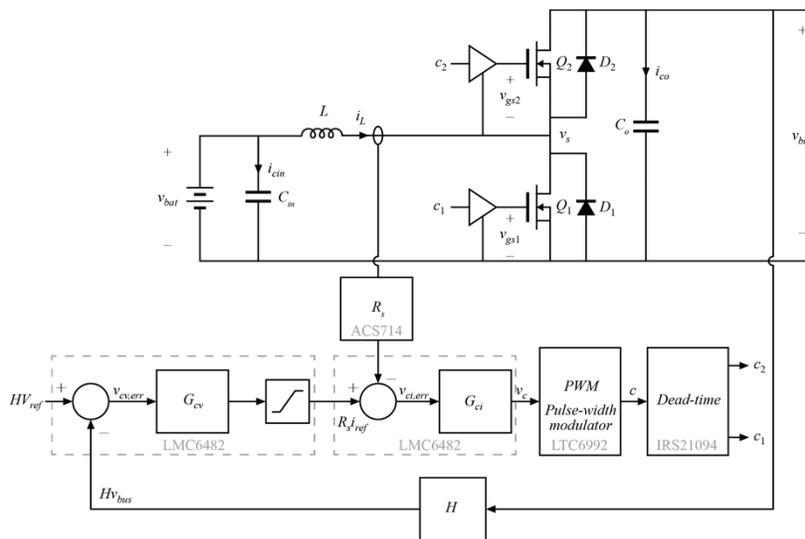
## Phase Margin Test



# Closed-Loop Response

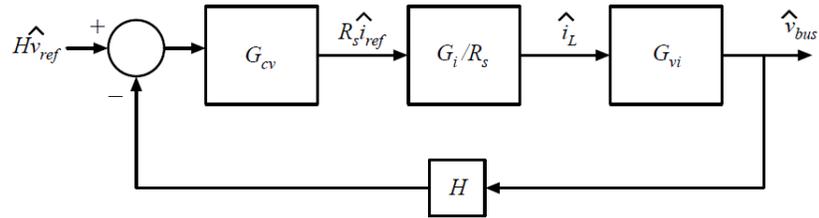


# Voltage Loop

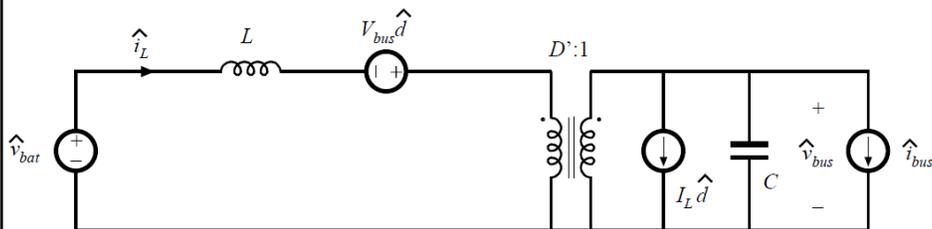




## Voltage Loop Gain



## Solving $G_{vi}$



$$G_{vi} = \frac{\hat{v}_{bus}}{\hat{i}_L} \Big|_{\hat{v}_{bat}=0, \hat{i}_{bus}=0}$$



## Solving $G_{vi}$



## Solving $G_{vi}$

$$G_{vi} = \left. \frac{\hat{v}_{bus}}{\hat{i}_L} \right|_{\hat{v}_{bar}=0, \hat{i}_{bus}=0} = G_{vio} \frac{1 - \frac{s}{\omega_z}}{1 + \frac{s}{\omega_{zi}}}$$

$$G_{vio} = D' \frac{V_{bus}}{I_{bus}}$$

$$f_z = \frac{1}{2\pi} \frac{D'^2 V_{bus}}{L I_{bus}}$$

$$f_{zi} = \frac{1}{2\pi} \frac{1}{C} \frac{I_{bus}}{V_{bus}}$$