

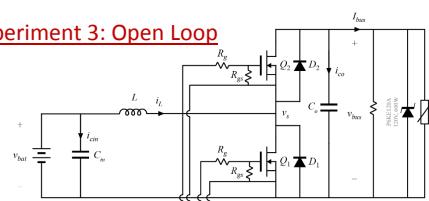
# Current Programmed Control

ECE 482 Lecture 6  
February 12, 2015

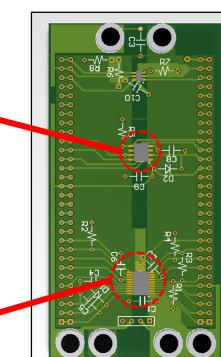
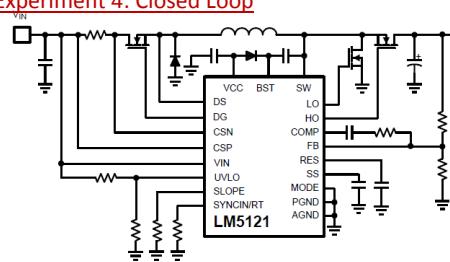


## Experiment 4: Closed-Loop Boost

### Experiment 3: Open Loop

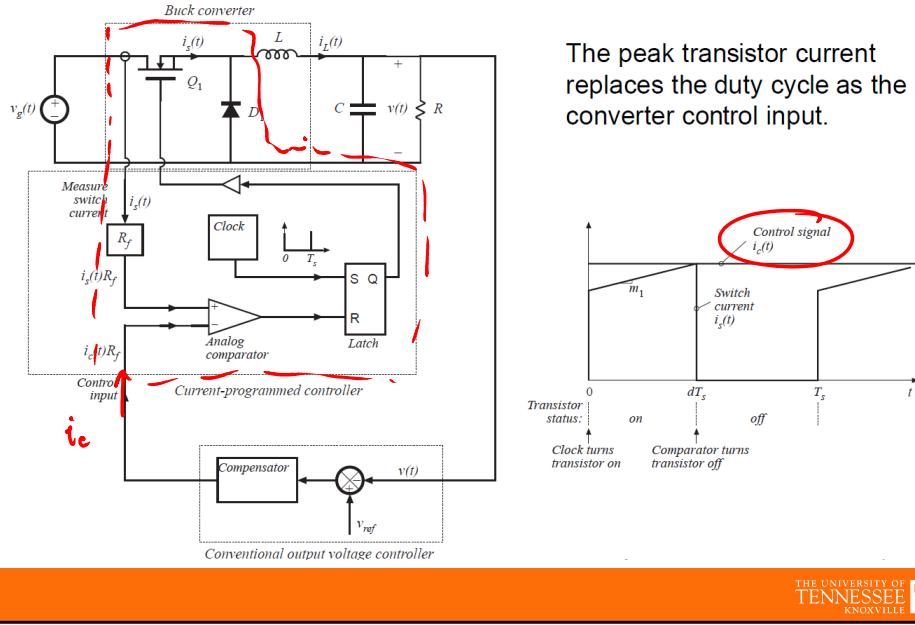


### Experiment 4: Closed Loop



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## Current Programmed Control (CPM)



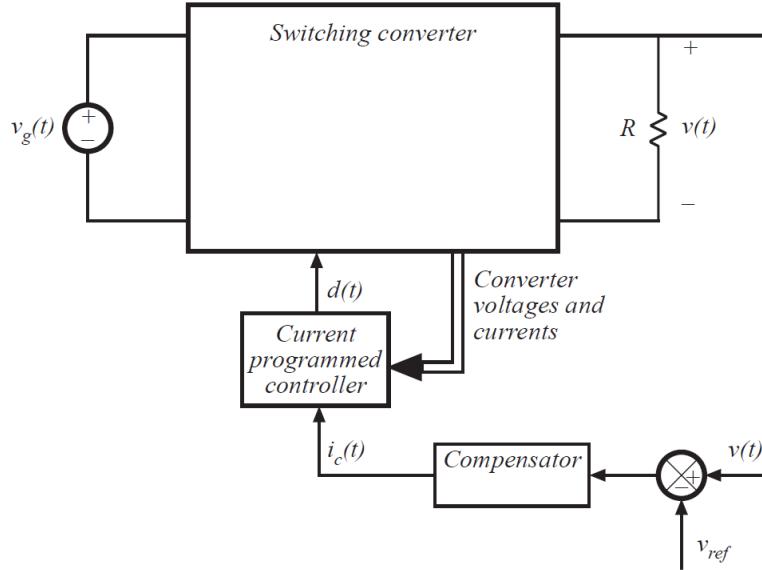
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## Current Programmed Control

- Covered in Ch. 12 of *Fundamentals of Power Electronics*
- Advantages of current programmed control:
  - Simpler dynamics —inductor pole is moved to high frequency
  - Simple robust output voltage control, with large phase margin, can be obtained without use of compensator lead networks
  - It is always necessary to sense the transistor current, to protect against overcurrent failures. We may as well use the information during normal operation, to obtain better control
  - Transistor failures due to excessive current can be prevented simply by limiting  $i_c(t)$
  - Transformer saturation problems in bridge or push-pull converters can be mitigated
- A disadvantage: susceptibility to noise

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## A Simple First-Order Model



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## The First-Order Approximation

$$\langle i_L(t) \rangle_{T_s} = i_c(t)$$

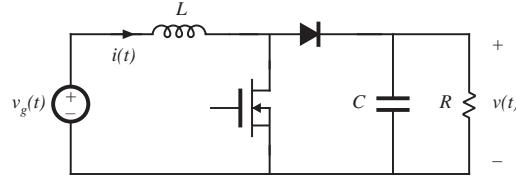
- Neglects switching ripple
- Yields physical insight and simple first-order model
- Accurate when converter operates well into CCM (so that switching ripple is small)
- Accurate when artificial ramp (discussed later) small
- Resulting small-signal relation:

$$i_L(s) \approx i_c(s)$$

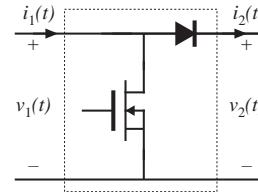
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## Boost Averaged Switch Modeling

Ideal boost converter example



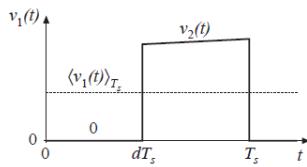
Boost-specific switch network



- Averaged switch model goal:
  - Express average of two waveforms ( $i_1(t)$ ,  $i_2(t)$ ,  $v_1(t)$ ,  $v_2(t)$ ) in terms of the other two



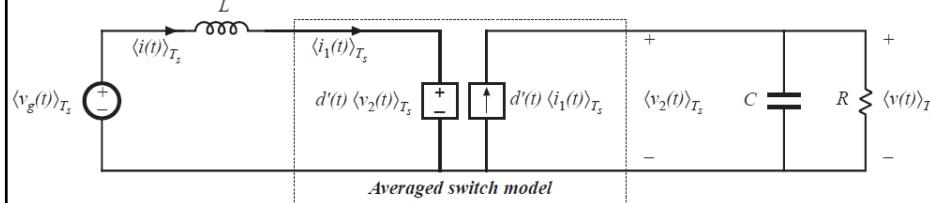
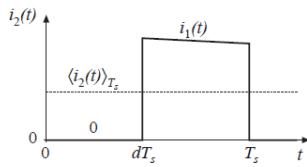
## Previous Definitions



Average the waveforms of the dependent sources:

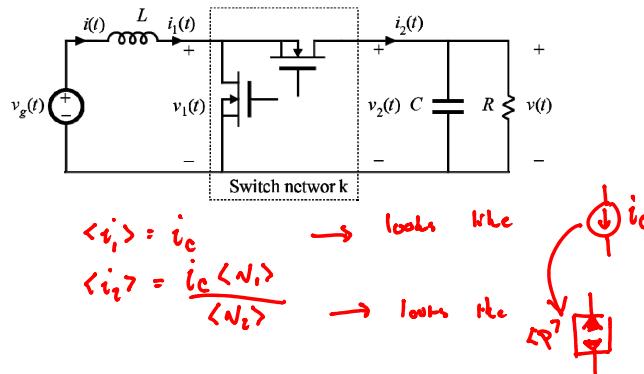
$$\langle v_1(t) \rangle_{T_s} = d'(t) \langle v_2(t) \rangle_{T_s}$$

$$\langle i_2(t) \rangle_{T_s} = d'(t) \langle i_1(t) \rangle_{T_s}$$



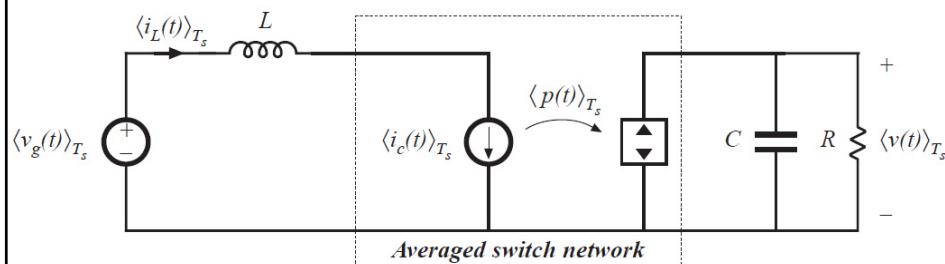
## A More Useful Approach

- Instead select  $i_1(t), i_2(t)$



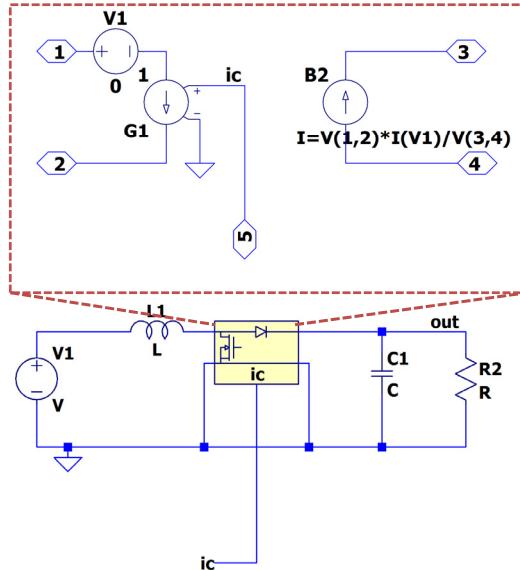
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## Large-Signal Nonlinear Model



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## Implementation in LTSpice



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## Perturb and Linearize

$$\begin{cases} \langle i_1 \rangle = I_c + \hat{i}_1 \\ \hat{i}_1 = \hat{i}_c \end{cases}$$

$$(1) \quad \langle i_1 \rangle = I_c$$

$$(2) \quad \langle i_2 \rangle = \frac{i_c \langle v_i \rangle}{\langle v_i \rangle}$$

$$(1) \quad I_c + \hat{i}_1 = I_c + \hat{i}_c \quad \text{DC: } \underline{I_c = I_c}$$

$$\text{ss AC: } \underline{\hat{i}_1 = \hat{i}_c}$$

$$(2) \quad (I_c + \hat{i}_1)(V_2 + \hat{v}_2) = (I_c + \hat{i}_c)(V_1 + \hat{v}_1)$$

$$\underline{I_c V_2 + \hat{i}_1 V_2 + \hat{i}_2 V_1 + I_c \hat{v}_2} = \underline{I_c V_1 + \hat{i}_c \hat{v}_1 + I_c \hat{v}_1 + V_1 \hat{v}_2}$$

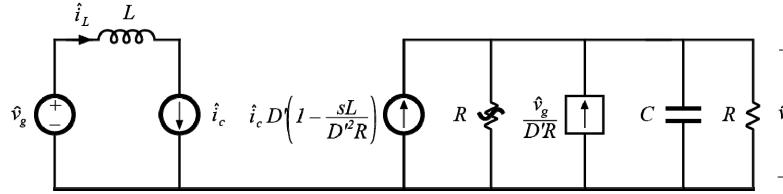
$$\text{DC: } I_c V_2 = I_c V_1$$

$$\text{AC: } \hat{i}_2 = \frac{I_c \hat{v}_1 + V_1 \hat{i}_c - I_c \hat{v}_2}{V_2}$$

Take DC solution for  $V_1, I_c$  &  $\underline{V_2 = V}$

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## Boost CCM CPM Small-Signal Model



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## CPM Transfer Functions

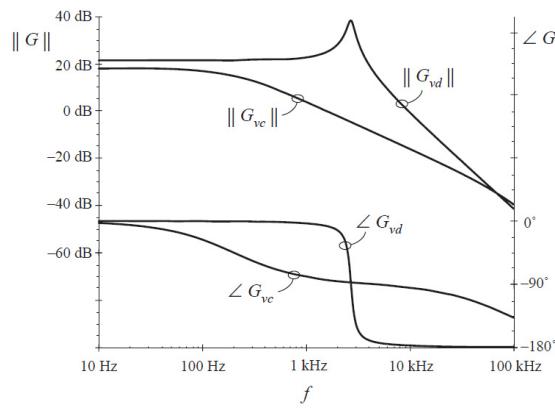
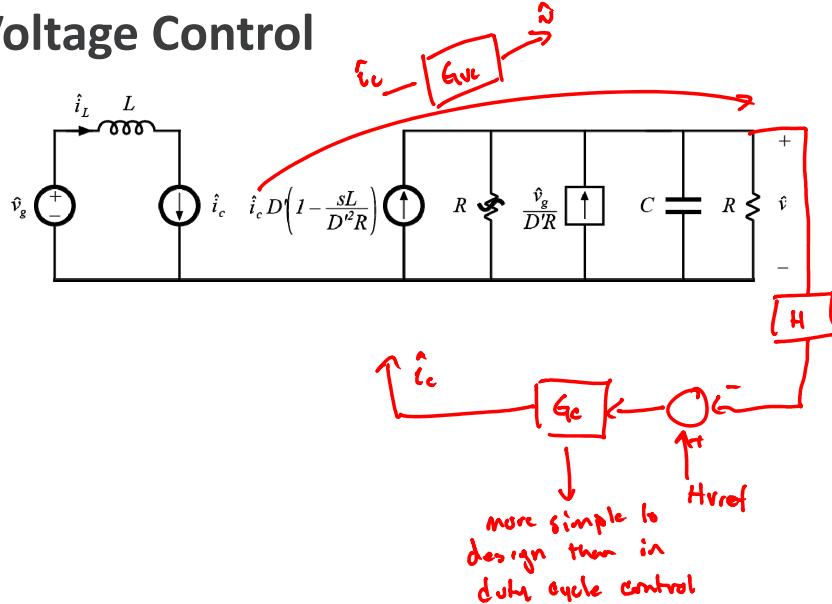


Fig. 12.28 Comparison of CPM control with duty-cycle control, for the control-to-output frequency response of the buck converter example.

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## Voltage Control



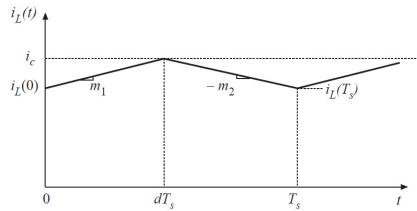
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## CPM Oscillations for $D > 0.5$

- The current programmed controller is inherently unstable for  $D > 0.5$ , regardless of the converter topology
- Controller can be stabilized by addition of an artificial ramp

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## Inductor Current Waveform in CCM



Inductor current slopes  $m_1$  and  $-m_2$

buck converter

$$m_1 = \frac{v_g - v}{L} \quad -m_2 = -\frac{v}{L}$$

boost converter

$$m_1 = \frac{v_g}{L} \quad -m_2 = \frac{v_g - v}{L}$$

buck-boost converter

$$m_1 = \frac{v_g}{L} \quad -m_2 = \frac{v}{L}$$



## Volt-Second Balancing

First interval:

$$i_L(dT_s) = i_c = i_L(0) + m_1 dT_s$$

Solve for  $d$ :

$$d = \frac{i_c - i_L(0)}{m_1 T_s}$$

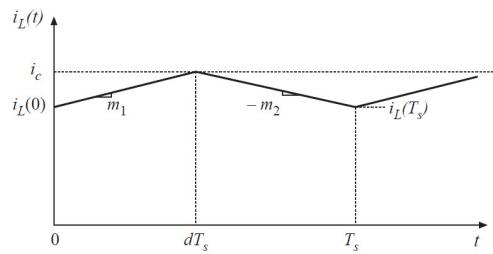
Second interval:

$$\begin{aligned} i_L(T_s) &= i_L(dT_s) - m_2 d T_s \\ &= i_L(0) + m_1 d T_s - m_2 d T_s \end{aligned}$$

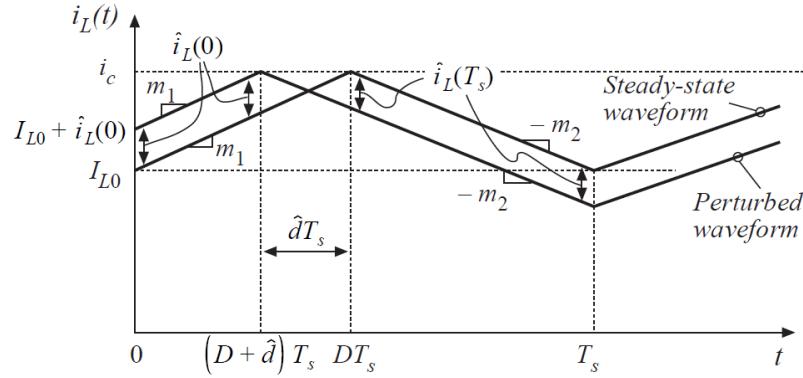
In steady state:

$$0 = M_1 D T_s - M_2 D' T_s$$

$$\frac{M_2}{M_1} = \frac{D}{D'}$$

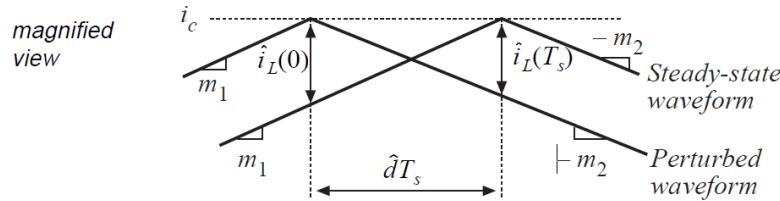


## Introducing a Perturbation



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## Change in Inductor Current Over $T_s$



$$\hat{i}_L(0) = -m_1 \hat{d}T_s$$

$$\hat{i}_L(T_s) = m_2 \hat{d}T_s$$

$$\hat{i}_L(T_s) = \hat{i}_L(0) \left( -\frac{D}{D'} \right)$$

$$\hat{i}_L(T_s) = \hat{i}_L(0) \left( -\frac{m_2}{m_1} \right)$$

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## Final Value of Inductor Current

$$\hat{i}_L(T_s) = \hat{i}_L(0) \left( -\frac{D}{D'} \right)$$

$$\hat{i}_L(2T_s) = \hat{i}_L(T_s) \left( -\frac{D}{D'} \right) = \hat{i}_L(0) \left( -\frac{D}{D'} \right)^2$$

$$\hat{i}_L(nT_s) = \hat{i}_L((n-1)T_s) \left( -\frac{D}{D'} \right) = \hat{i}_L(0) \left( -\frac{D}{D'} \right)^n$$

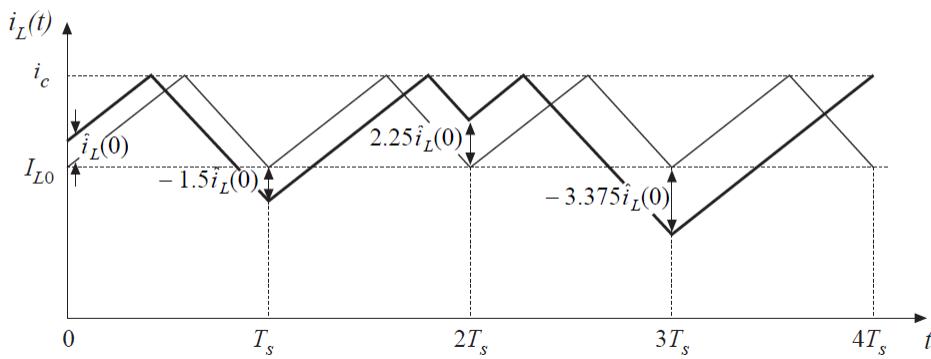
$$\left| \hat{i}_L(nT_s) \right| \rightarrow \begin{cases} 0 & \text{when } \left| -\frac{D}{D'} \right| < 1 \\ \infty & \text{when } \left| -\frac{D}{D'} \right| > 1 \end{cases}$$

For stability:  $D < 0.5$



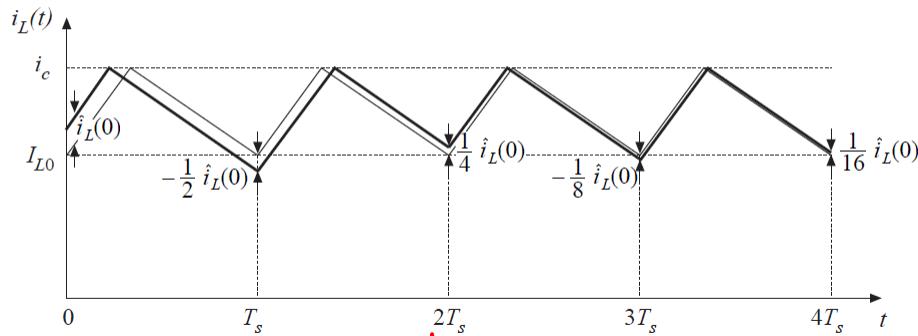
## Example: Unstable operation for $D=0.6$

$$\alpha = -\frac{D}{D'} = \left( -\frac{0.6}{0.4} \right) = -1.5$$



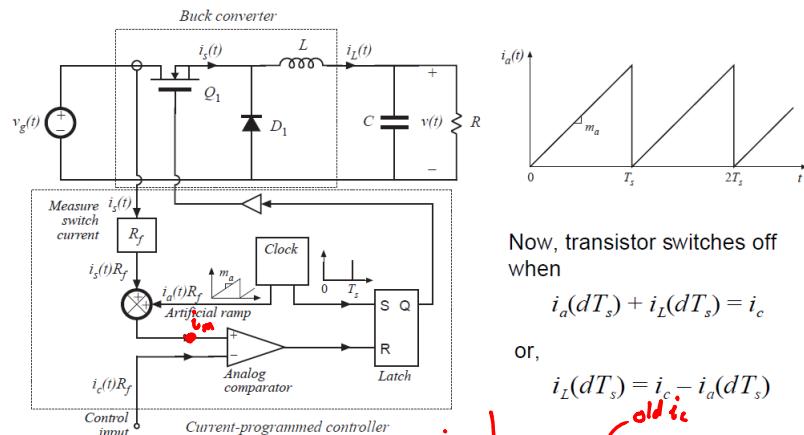
## Example: Stable operation for $D=1/3$

$$\alpha = -\frac{D}{D'} = \left(-\frac{1/3}{2/3}\right) = -0.5$$



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## Stabilization Through Artificial Ramp



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## Final Value of Inductor Current

First subinterval:

$$\hat{i}_L(0) = -\hat{d}T_s(m_1 + m_a)$$

Second subinterval:

$$\hat{i}_L(T_s) = -\hat{d}T_s(m_a - m_2)$$

Net change over one switching period:

$$\hat{i}_L(T_s) = \hat{i}_L(0) \left( -\frac{m_2 - m_a}{m_1 + m_a} \right)$$

After  $n$  switching periods:

$$\hat{i}_L(nT_s) = \hat{i}_L((n-1)T_s) \left( -\frac{m_2 - m_a}{m_1 + m_a} \right) = \hat{i}_L(0) \left( -\frac{m_2 - m_a}{m_1 + m_a} \right)^n = \hat{i}_L(0) \alpha^n$$

Characteristic value:

$$\alpha = -\frac{m_2 - m_a}{m_1 + m_a}$$

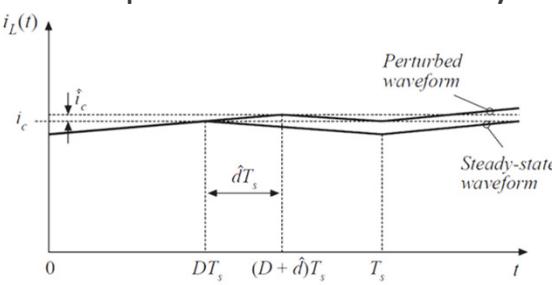
$$|\hat{i}_L(nT_s)| \rightarrow \begin{cases} 0 & \text{when } |\alpha| < 1 \\ \infty & \text{when } |\alpha| > 1 \end{cases}$$



## Artificial Ramp: Additional Notes

- For stability, require  $|\alpha| < 1$
- Common choices:
  - $m_a = 0.5 m_2$
  - $m_a = m_2$
- Artificial ramp decreases sensitivity to noise

$$\alpha = -\frac{1 - \frac{m_a}{m_2}}{\frac{D'}{D} + \frac{m_a}{m_2}}$$

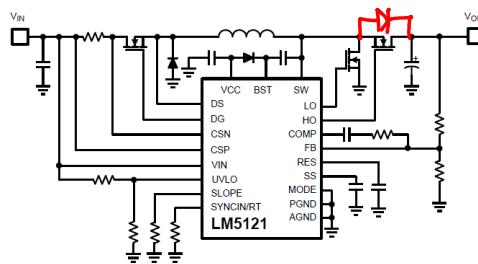


## More Accurate Models

- The simple models of the previous section yield insight into the low- frequency behavior of CPM converters
- Unfortunately, they do not always predict everything that we need to know:
  - Line-to-output transfer function of the buck converter
  - Dynamics at frequencies approaching  $f_s$
- More accurate model accounts for nonideal operation of current mode controller built-in feedback loop
- Converter duty-cycle-controlled model, plus block diagram that accurately models equations of current mode controller
- See Section 12.3 for additional info

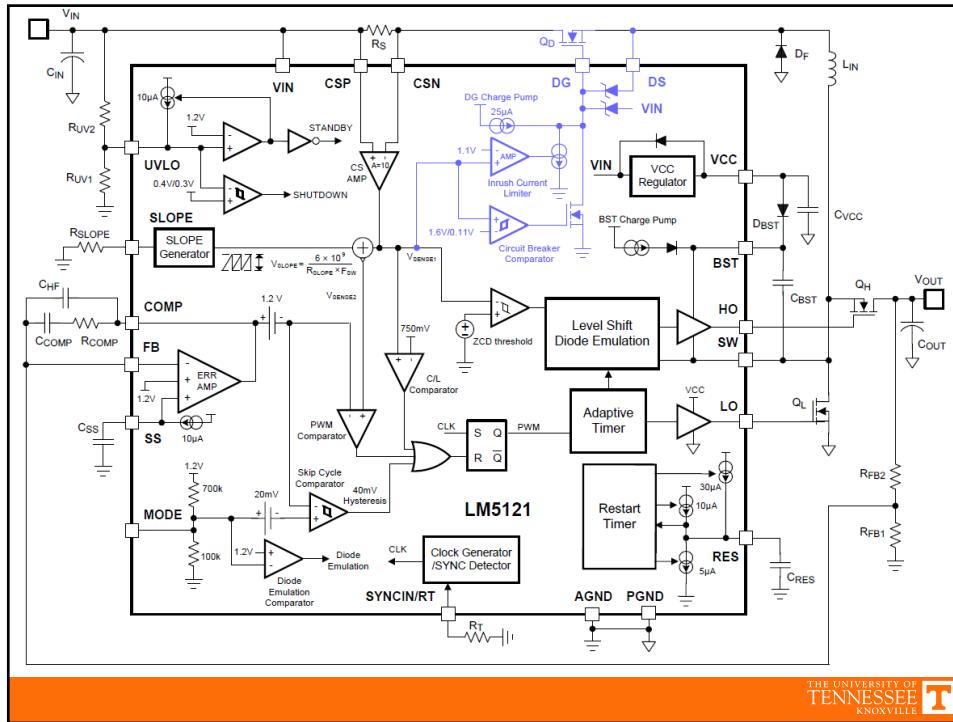
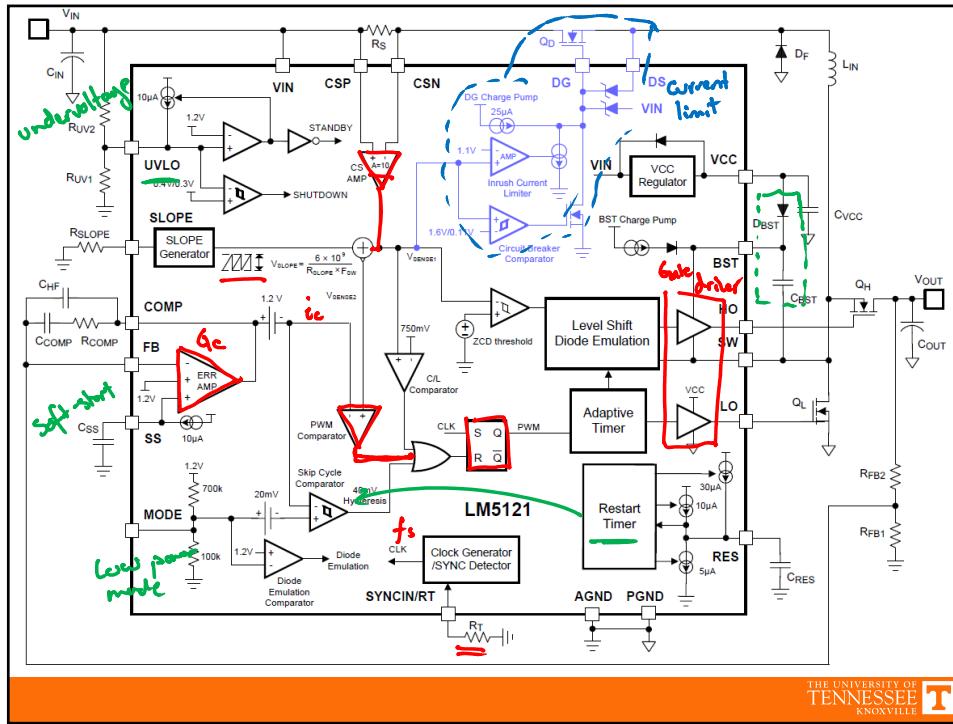


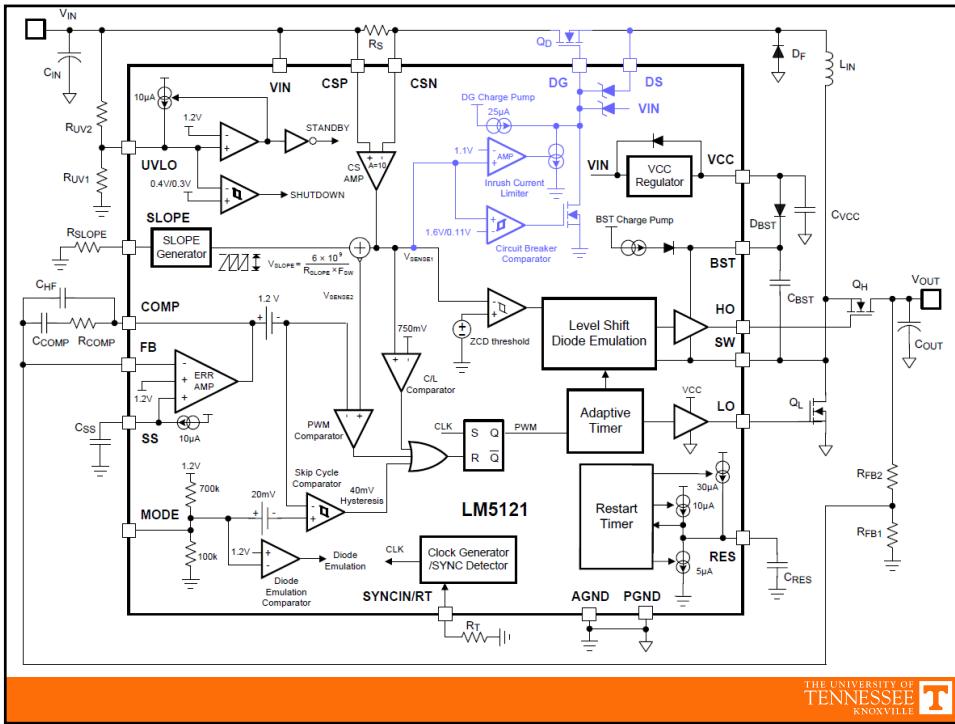
## Application to Experiment 4



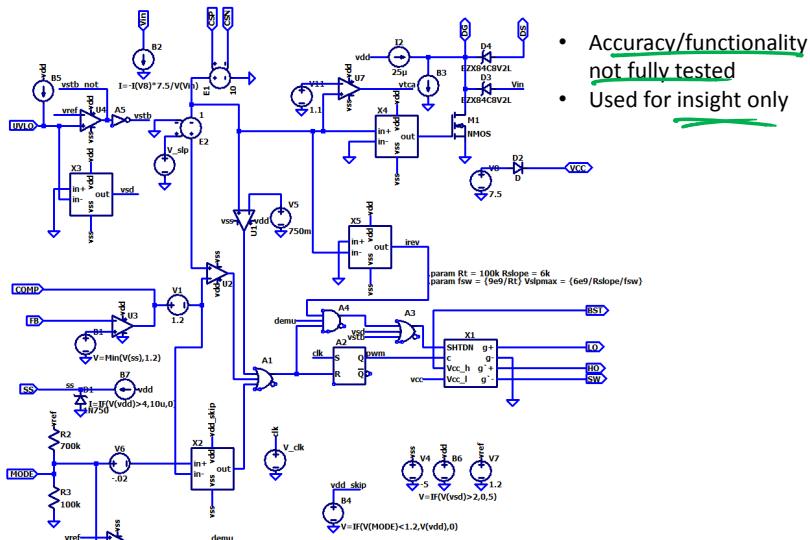
- Complex switching controller
- Read the datasheet first





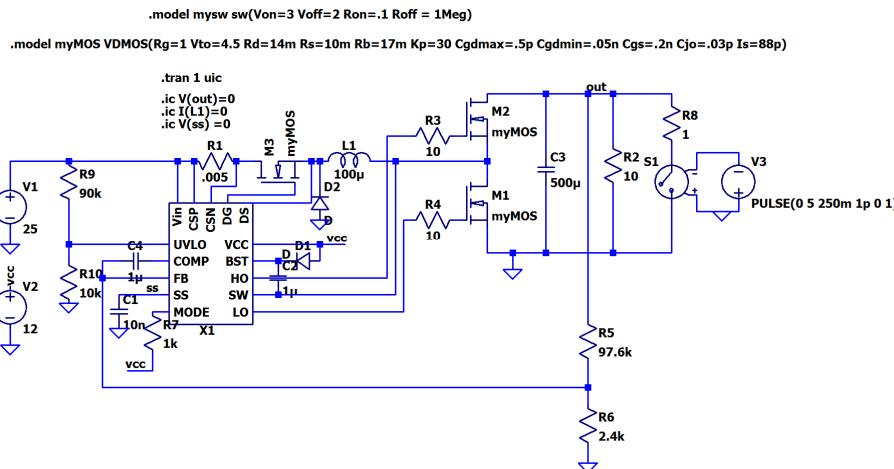


## Internal Functional Model in LTSpice



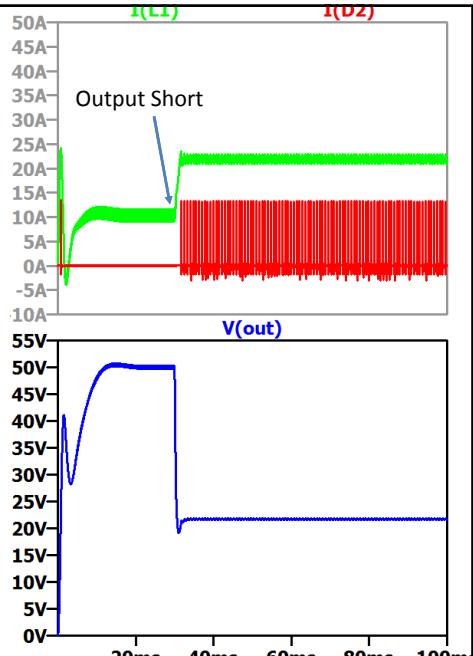
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## In-Circuit Simulation



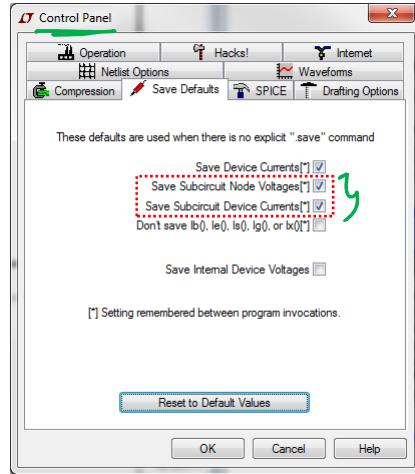
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## Sim Results



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## A Tip: Debug Internal of Subcircuit



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