

# Overview of core loss prediction (and measurement techniques) for non-sinusoidal waveforms

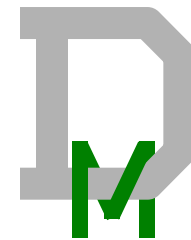
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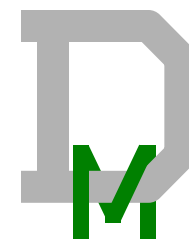
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# Outline

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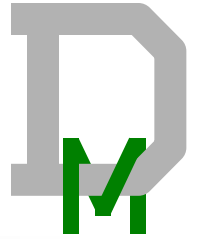
- Need for loss models for non-sinusoidal waveforms beyond the Steinmetz equation (SE).
- Models: MSE, GSE, NSE, EGSE, iGSE, i<sup>2</sup>GSE, WCSE, CWH and FHM (and in the addendum: the DNSE)
- How can they be used?
- Where to go from here?

*References are listed on the last slide*

# Existing models: Physically motivated



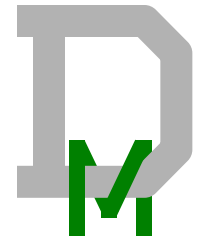
- Classical eddy current loss,  $P_{cl}$   
**Small part of loss in ferrites.**
- Detailed hysteresis models (e.g., Preisach, Jiles-Atherton).
  - Standard methods are **only static**; do not predict important frequency/rate dependence  
 $P = P_h + P_{cl} + P_{exc}$  (“excess loss”).
  - Addition of linear dynamics doesn’t capture nonlinearity in excess loss.
- Models based on eddy loss induced by domain wall motion:
  - $P_{exc} \propto (Bf)^\gamma$  ;  $\gamma = 1.5$  or  $2$
  - **Does not match empirical data for ferrites**  
(  $\alpha \neq \beta$  in Steinmetz equation).



# 20<sup>th</sup> C model for core loss

- Steinmetz equation (SE):
$$P = kf^\alpha \hat{B}^\beta$$
  - Sinusoidal only (but most power electronics waveforms are not sinusoidal!)
  - Loss is a nonlinear phenomenon: Fourier series does not apply.
  - Other notes:
    - One set of parameters only works for a limited frequency range.
    - Ignores the important effect of dc bias.
- Physically-based models: **Not available for ferrites.**
  - Possible recent exception: (Van den Bossche, Valchev, and Van de Sype, 2006)

# The first SE variation: Modified Steinmetz Equation (MSE)



(Albach ,Durbau and Brockmeyer, 1996;  
Reinert, Brockmeyer, and De Doncker, 1999).

- Modifies Steinmetz equation based on physical motivation that domain wall motion loss depends on  $dB/dt$ .
- Calculates an equivalent frequency from a weighted average of  $dB/dt$ :

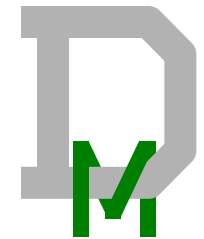
$$f_{eq} = \frac{2}{\Delta B^2 \pi^2} \int_0^T \left( \frac{dB}{dt} \right)^2 dt$$

- Use equivalent frequency and repetition rate  $f_r$  in Steinmetz Equation:

$$P = k f_{eq}^{\alpha-1} \hat{B}^{\beta} f_r$$

- **Limitation:** arbitrary assumption about type of averaging for equivalent frequency limits accuracy.

# Next: Generalized Steinmetz Equation (GSE) (Li, Abdallah, and Sullivan, 2001)



- Failed attempt—useful to see why.
- Hypothesis:  $p(t) = \text{fcn}(B(t), dB/dt)$   
(instantaneous power loss depends only on instantaneous  $B$ ,  $dB/dt$ )
- Combining the instantaneous dissipation hypothesis with the Steinmetz equation yields:
$$P(t) = k_1 \left| \frac{dB}{dt} \right|^a |B(t)|^b$$
- Tests show that it is not accurate—sometimes worse than MSE.

MSE  
1996, 1999

GSE  
2001



# Lesson from GSE failure

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- Losses depend on whole cycle, not just  $B(t)$ ,  $dB/dt$ .
- Our path forward: Try another hypothesis.

- GSE was 
$$\overline{P(t)} = k_i \overline{B(t)^x \left| \frac{dB}{dt} \right|^y}$$

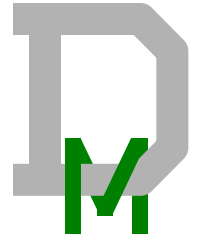
- Improved GSE (iGSE) hypothesis:

$$\overline{P(t)} = k_i (\Delta B)^w \overline{\left| \frac{dB}{dt} \right|^z}$$



# iGSE (improved Generalized SE)

(Venkatachalam, C. R. Sullivan, T. Abdallah, H. Tacca, 2002)



- Based on  $\overline{P(t)} = k_i (\Delta B)^w \left| \frac{dB}{dt} \right|^z$ , plus compatibility with Steinmetz equation for sine waves.
- Result:  $\overline{P(t)} = k_i (\Delta B)^{\beta - \alpha} \left| \frac{dB}{dt} \right|^\alpha$
- Two years later, independently discovered and named the Natural Steinmetz Extension (NSE) by Van den Bossche, Valchev and Georgiev, 2004

MSE  
1996, 1999

GSE  
2001

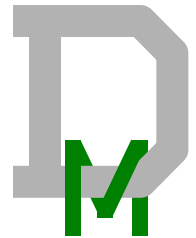
iGSE  
2002

=

aka NSE  
2004

# iGSE: formulas to use.

(Venkatachalam, C. R. Sullivan, T. Abdallah, H. Tacca, 2002)

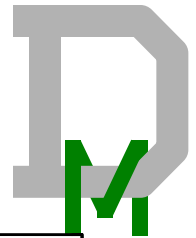


- General expression:  $\overline{P}(t) = k_i (\Delta B)^{\beta - \alpha} \left| \frac{dB}{dt} \right|^\alpha$
- Can obtain all parameters from sinusoidal data (i.e., from SE parameters)

$$k_i = \frac{k f^\alpha \left(\frac{1}{2}\right)^\beta}{(\Delta B)^{-\alpha} |\omega \cos(\omega t)|^\alpha} \quad k_i \cong \frac{k}{2^{\beta+1} \pi^{\alpha-1} \left(0.2761 + \frac{1.7061}{\alpha + 1.354}\right)}$$

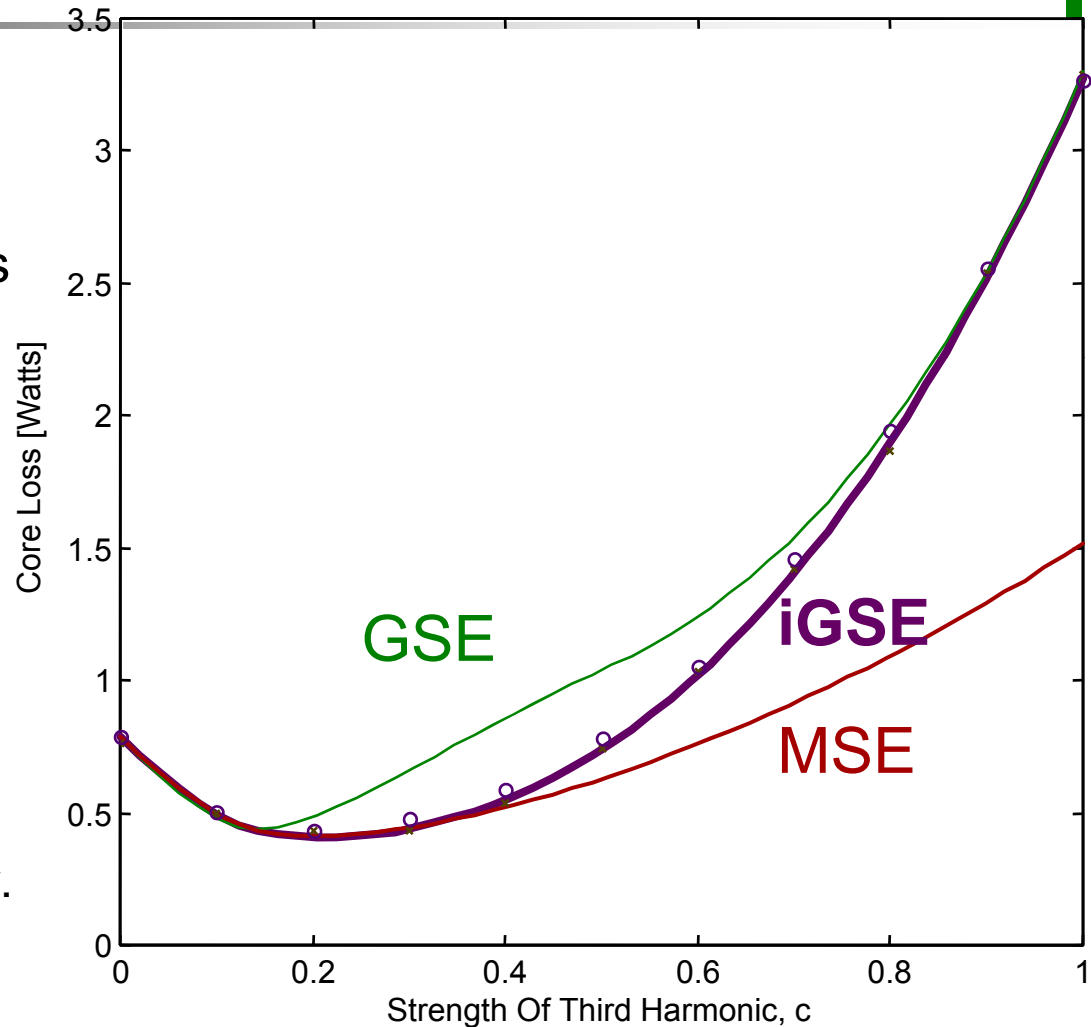
- Simple formula for piecewise-linear waveforms:

$$\overline{P}_v = \frac{k_i (\Delta B)^{\beta - \alpha}}{T} \sum_m \left| \frac{B_{m+1} - B_m}{t_{m+1} - t_m} \right|^\alpha (t_{m+1} - t_m)$$

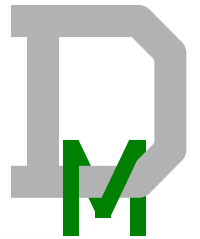


# Performance of iGSE

- Matched measurements much better than either previous method.
- Subsequent comparisons have consistently shown that it outperforms alternatives.
- Main limitations:
  - What if fundamental and harmonics are in different frequency ranges where Steinmetz parameters are different?
  - DC bias not accounted for.
  - Relaxation effects
  - For more on these, see (J. Muhlethaler, J. Biela, J.W. Kolar, A. Ecklebe, 2012a, 2012b)

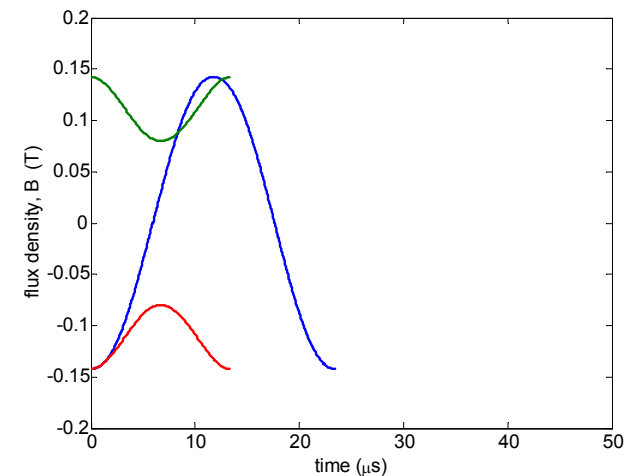
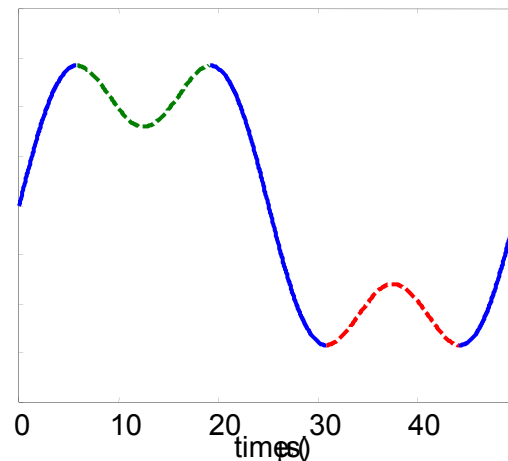
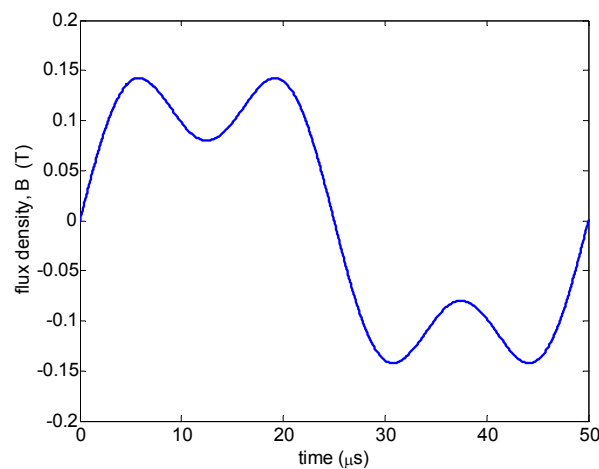


$$B(t) = A[(1-c)\sin\omega t + c \sin(3\omega t + \phi)]$$



# Minor loops

- Not present in simple waveforms.
- Addressed in 1<sup>st</sup> MSE paper (Albach, Durbau & Brockmeyer, 1996) and in iGSE paper (2002):
  - Algorithm for automatic separation of nested loops in iGSE paper (2002).





# Other SE methods

- WcSE: Waveform coefficient SE

(Shen, Wang, Boroyevich, Tipton, 2008)

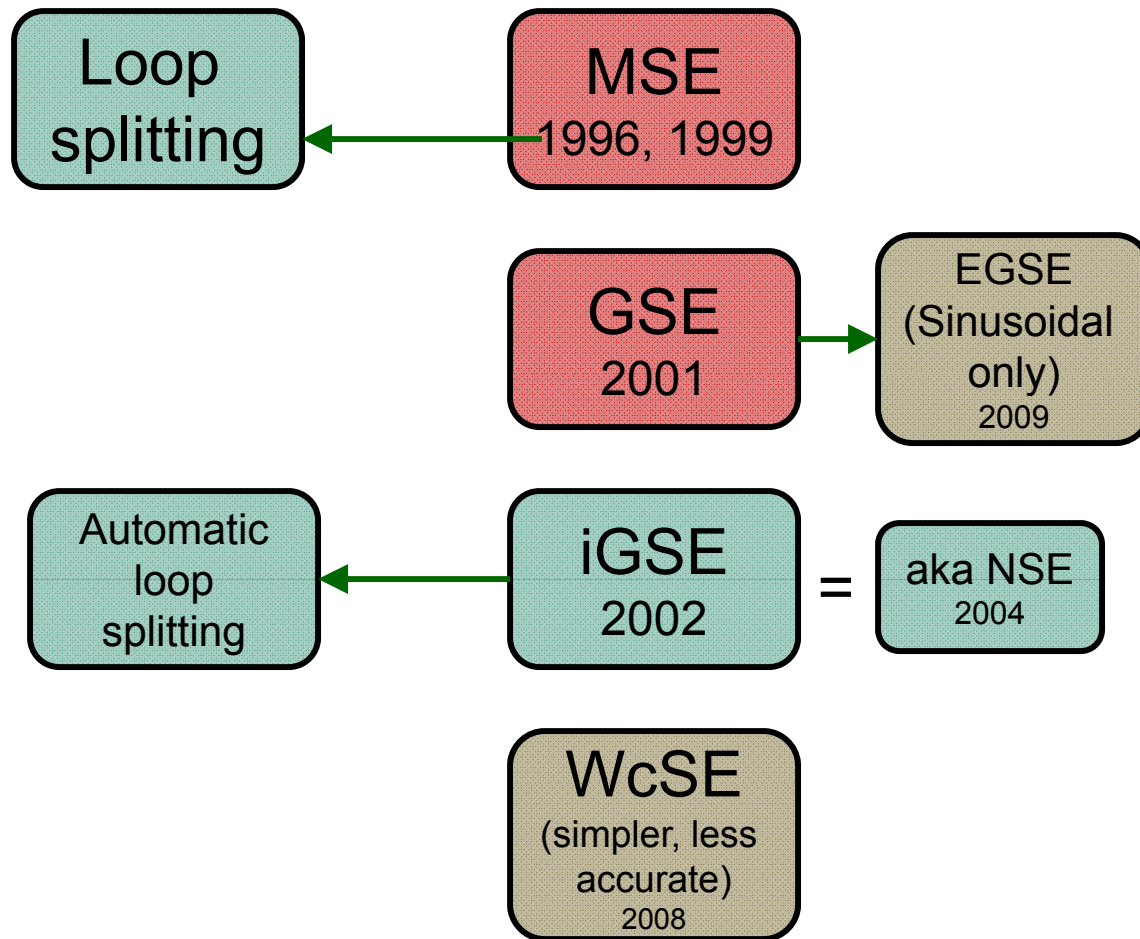
- Multiply SE result by a factor:
- Intended to be easier than iGSE; authors' results show similar accuracy to iGSE.
- Others' results show it's significantly less accurate for some situations (Villar, Viscarret, Etxeberria-Otadui and Rufer, 2009)

$$\frac{\int_0^{T/2} |B(t)| dt}{\int_0^{T/2} \hat{B} \sin(\omega t) dt}$$

- EGSE: Expanded GSE (Chen, 2009)

- For LF sine waves in steel; captures frequency dependence better.

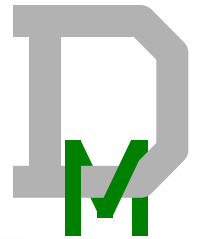
$$P(t) = k_2 \left| \frac{dB}{dt} \right|^m \left| \frac{dB}{dt} \right|^e |B(t)|^n$$



# FHM

## (Field-extrema Hysteresis Model)

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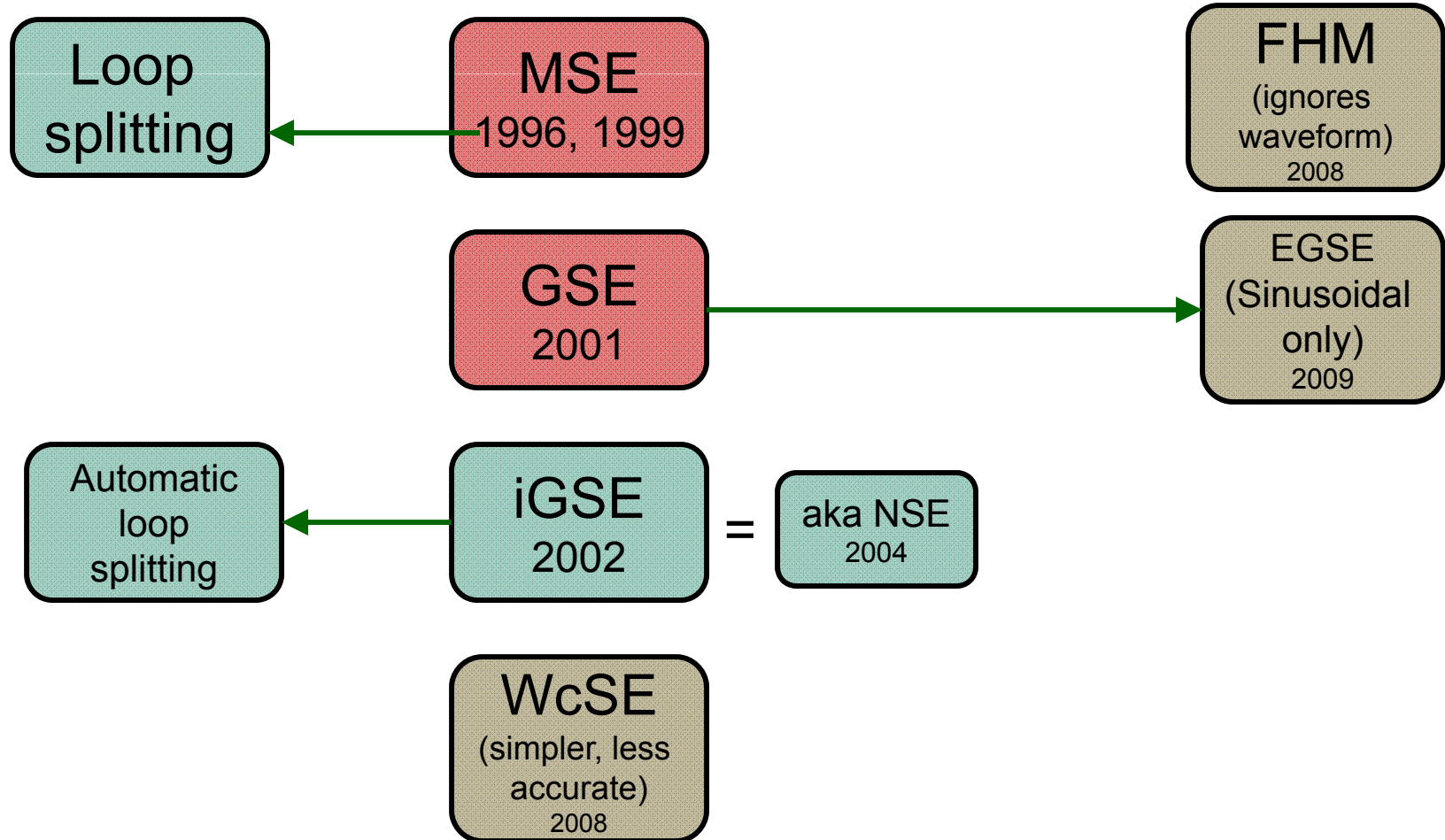


(Cale, Sudhoff, and Chan, 2008)

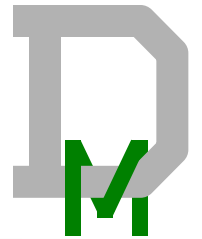
- By definition, this assumes that the shape of the waveform doesn't matter and only looks at peaks.
  - Does not capture effect of waveform.
- Starts by assuming that a frequency-dependent Jiles-Atherton model is correct—aims to duplicate its behavior.
  - Does capture DC bias effect as in JA model.



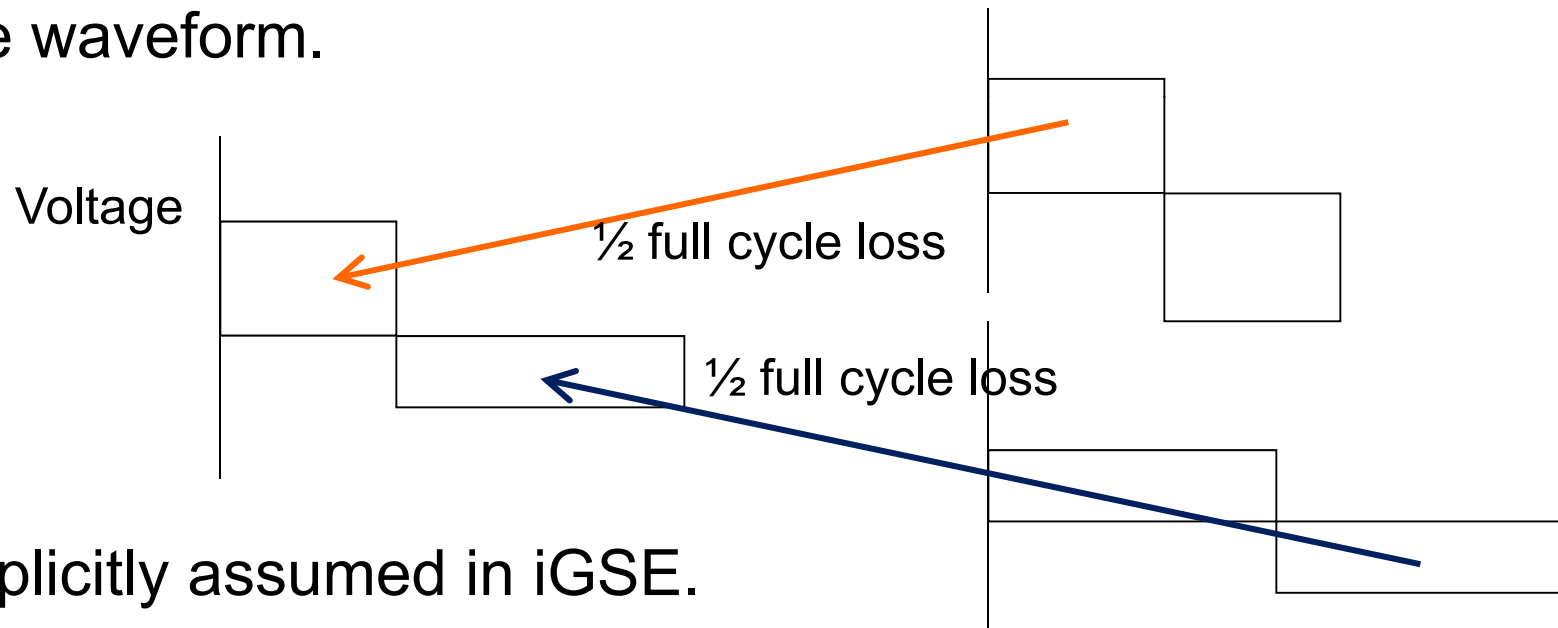
## Other purpose



# Composite Waveform Hypothesis

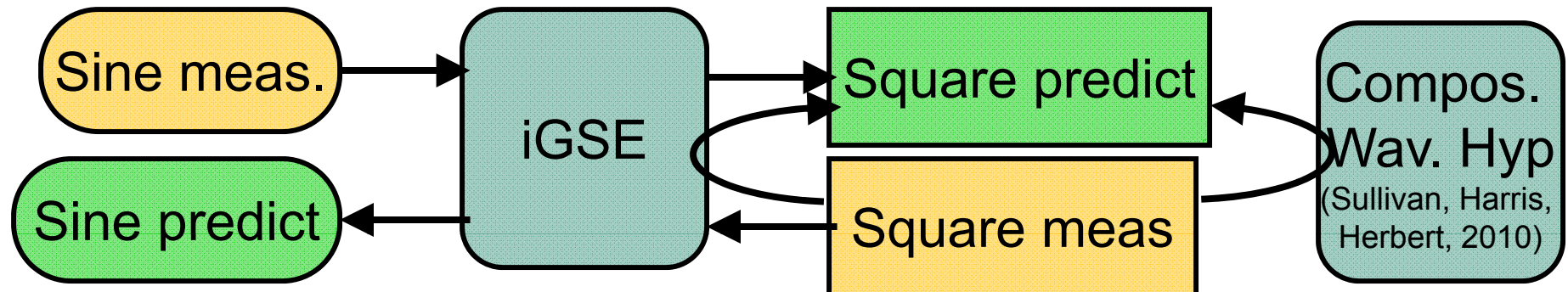
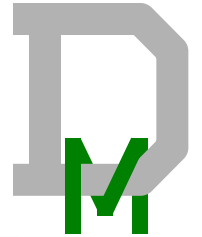


- Idea that total energy lost in a cycle can be calculated by summing the loss that occurs during each segment of the waveform.



- Implicitly assumed in iGSE.
- Explicitly stated and tested in (Sullivan, Harris and Herbert, 2010)
  - Results mixed—see next talk.

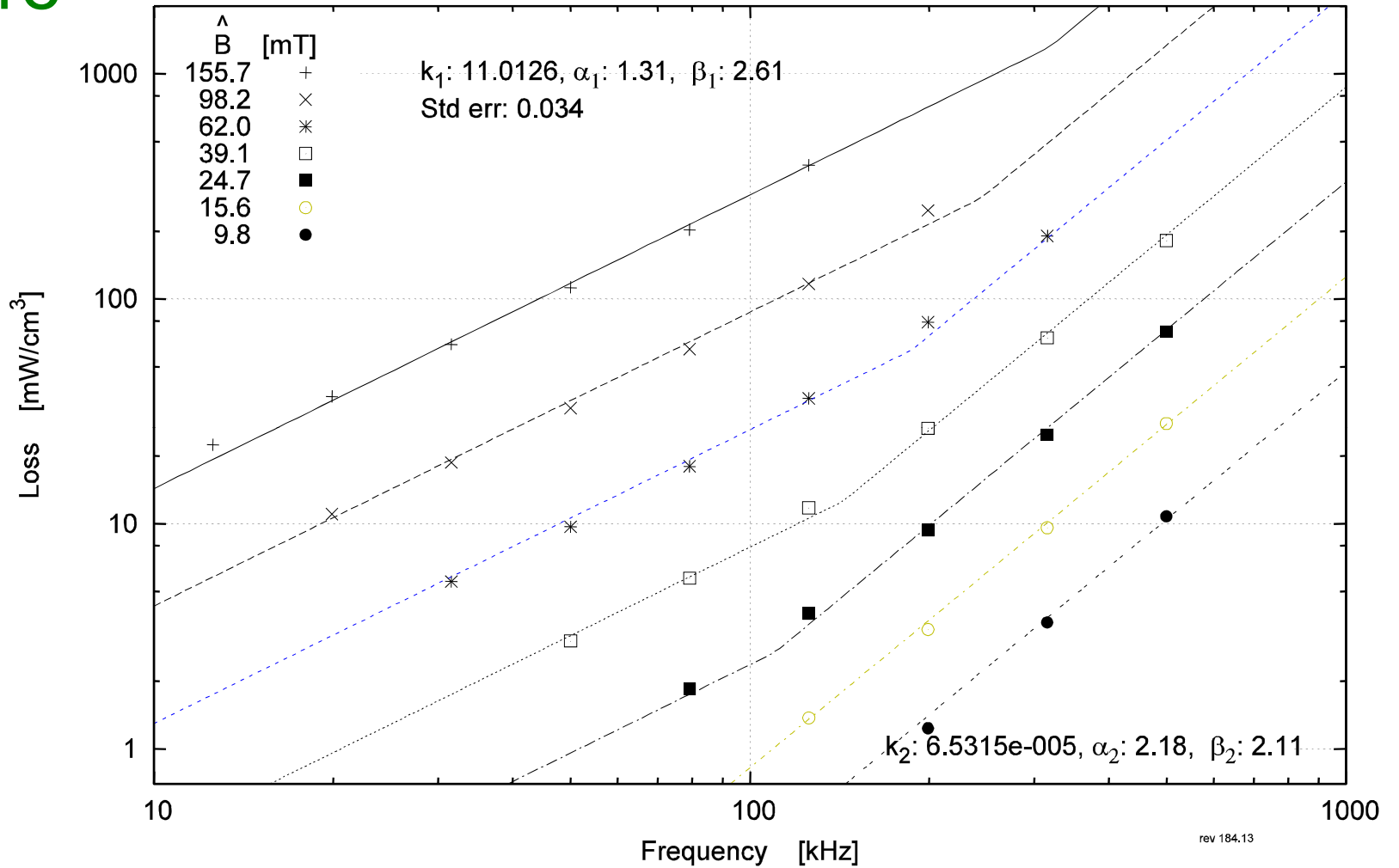
# Measuring with sine waves vs. measuring square-wave voltage?



- Predicting square with square data: Comp. Wav. Hyp. and iGSE give exactly the same results.
- Making predictions with the same class of waveforms is more accurate. Because:
  - Steinmetz parameters are different for different frequencies.
  - Square wave includes harmonics—can span two ranges.

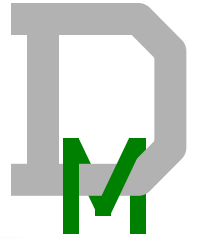
# Square-wave data

Core Loss vs. Frequency with Two-plane Steinmetz Fit,  
Run Set fx003: Ferroxcube 3C81 Material



- Can fit with “two-plane Steinmetz” equation (Sullivan & Harris, 2011)

$$P_v = \max\left(K_1 f^{\alpha_1} \hat{B}^{\beta_1}, K_2 f^{\alpha_2} \hat{B}^{\beta_2}\right)$$



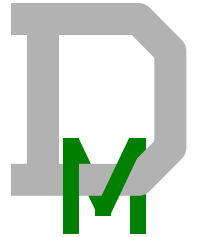
# Conclusions

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- iGSE:
  - Works surprisingly well; better than most alternatives.
  - Allows the use of square or sine data for square or sign predictions.
  - Is equivalent to the composite waveform hypothesis for square predictions with square waveforms.
  - Is simple to use for PWL waveforms without minor loops, and minor loop separation can be used for waveforms with minor loops.

But

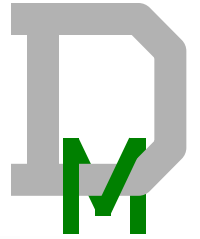
- Does not account for dc bias effect or “relaxation effects.”
- Square-wave data is a better basis for predicting loss with square voltage applications.
  - Can fit with two-plane Steinmetz equation.



# Moving forward

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- Square-wave data from manufacturers.
  - Including dc and temperature effects
    - Automated data collection!
    - Standardized database format.
- Research topics:
  - Reduce data collection needed for dc, temperature, and relaxation effects based on underlying mechanisms.
  - Nonlinear dynamic model that matches behavior and captures loss accurately.
    - Constrain model development to match known loss behavior, as in development of iGSE.



# Addendum

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- One more method omitted from the original presentation: the DNSE. (A.P. Van den Bossche, D.M. Van de Sype, V.C. Valchev, 2005)
- Uses iGSE (aka NSE) with the sum of two Steinmetz equations, one for pure hysteresis and one for anomalous losses.
- This is one solution to the problem of needing different frequency ranges in a Steinmetz fit.

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