

4
State Plane Analysis of DAB Converter
(1)
(II)

$$
\begin{aligned}
& \frac{\left(I_{1}+\Gamma_{1}\right)}{t_{2} \omega_{0}}=\frac{2 \sqrt{y_{y}}}{L_{1} \omega_{0}} \\
& \frac{(I+I)}{B}=\frac{2 V_{g}}{4 \cdot \sqrt{14 \theta}}=\frac{2 V_{g}}{R_{0}}
\end{aligned}
$$

(11)

$$
\begin{aligned}
& \begin{array}{l}
\left.J_{2}+J_{1}=2 \beta\right] 5 \\
\delta^{\prime}=\sin ^{-1}\left(\frac{2 n t}{J^{\prime}}\right) \\
J_{S}^{\prime}=\sqrt{(2 n t)^{2}+J_{2}^{\prime 2}} \quad \text { anolei }
\end{array}
\end{aligned}
$$

(1) $\rightarrow x$

$$
\begin{aligned}
& \text { Averaging Step } \\
& n_{t}\left\langle i_{\text {alt }}\right\rangle=\frac{2}{T_{s}} \int_{0}^{n_{s} / 2} i_{\omega \alpha}(t) d t=\frac{2}{T_{s}}\left[q_{1}+q_{2}+f_{3}+q_{4}\right] \\
& \frac{1}{I_{\text {er }}} \eta_{r}\left\langle L_{\text {ar }}\right\rangle=\frac{2}{T_{s}}\left[2 C_{p} V_{g}+t_{2} \frac{I_{1}-I_{2}}{2}+\phi+t_{4} I_{p}\right] \cdot \frac{1}{I_{\text {Base }}}
\end{aligned}
$$

$$
\begin{aligned}
& J=2 f_{5}\left[\frac{2}{\omega_{0}}+t_{2} \frac{s_{1}-s_{2}}{2}+t_{4} J_{p}\right] \cdot \frac{\omega_{0}}{\omega_{0}} \\
& J=\frac{1 f_{s}}{2 \pi f_{0}}\left[2+\beta \frac{s_{1}-s_{2}}{2}+\ell_{p}\right] \\
& J=\frac{F}{\pi}\left[2+\frac{\beta}{2}\left(J_{1}-J_{2}\right)+h_{\sim} J_{p}\right] \\
& \uparrow
\end{aligned}
$$

Output Plane

$$
\begin{aligned}
& J=\frac{n\left\langle i_{\text {out }}\right\rangle}{I_{\text {base }}}=\frac{F}{\pi}\left[2+\frac{1}{4}\left(J_{1}^{2}-J_{2}^{2}\right)+J_{p}\left(\frac{\pi}{F}-\alpha-\beta-\delta\right)\right] \leftharpoonup \downarrow \\
& F \equiv \frac{f_{s}}{f_{0}} \\
& F \rightarrow 1 \quad t_{0}=f_{s} U \\
& F \rightarrow 0 \text { fo } \gg f_{s} t \\
& \text { aus os very fast witt ts }
\end{aligned}
$$

## Selection of Tank Inductance

- State plane analysis gives equation of the form:

$$
P_{\text {out }}=f\left(C_{l}, C_{p}, C_{s}, f_{s}, U_{0}\right) \longleftarrow=f\left(\text { daish, } J_{p}\right)
$$

- If we select some minimum power $P_{\text {min }}$ for ZVS design to place ZVS boundary $\left(J_{p}=2\right)$, at $P_{\text {min }}$ $P_{\text {min }}=f\left(L_{l}\right.$, devices, $\left.f_{s}\right)$
- From resulting equation, $L_{I}$ determined from converter devices, application requirements, and placement of ZVS boundary
- Now select devices for minimum loss in converter



## Selecting MOSFETs for DAB

| 150 V FETS 12 V FETS |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Device <br> Variant | Type | $\begin{gathered} r_{o n} \\ {[\mathrm{~m} \Omega]} \end{gathered}$ | $\begin{gathered} C_{\text {oss }} \\ {[\mathrm{pF}]} \end{gathered}$ | $\begin{gathered} Q_{g} \\ {[\mathrm{nC}]} \end{gathered}$ | Device Variant | Type | $\begin{gathered} r_{o n} \\ {[\mathrm{~m} \Omega]} \end{gathered}$ | $\begin{gathered} C_{\text {oss }} \\ {[\mathrm{pF}]} \end{gathered}$ | $\begin{gathered} Q_{g} \\ {[\mathrm{nC}]} \end{gathered}$ |
| EPC1012 | GaN 2 | 70 | 80 | 1.9 | EPC1014 | GaN | 12.0 | 150 | 3.0 |
| EPC1010 | GaN | 18 | 310 | 7.5 | EPC1015 | GaN | 3.2 | 575 | 11.6 |
| FDMS2672 | MOS 7 | 64 | 95 | 30 | CSD16325Q5C | MOS | 1.7 | 2190 | 18.0 |
| IPD320N | MOS | S. 35 | 135 | 12.0 | STD60N3LH5 | MOS | 8.8 | 265 | 8.8 |
| IRFS4020 | MOS | 85 | 91 | 18.0 | CSD16411Q3 | MOS | 12.0 | 330 | 2.9 |

- Representative sample of HV and LV devices, including Si and GaN devices
- Above $P_{\text {min }}$, all devices have no switching loss, so efficiency only depends on conduction losses

$$
P_{\text {cond }}=P_{\text {cond }, p}+P_{\text {cond }, s}=2 r_{\text {on }, p} i_{g, r m s}^{2}+2 r_{\text {on,s }} i_{\text {out,rms }}^{2}
$$

## Selecting MOSFETs for DAB

| 150 V FETS |  |  |  |  | 12V FETS |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Device <br> Variant | Type | $\begin{gathered} r_{o n} \\ {[\mathrm{~m} \Omega]} \end{gathered}$ | $\begin{gathered} C_{p} \\ {[\mathrm{pF}]} \\ \hline \end{gathered}$ | $\begin{gathered} Q_{g} \\ {[\mathrm{nC]}]} \\ \hline \end{gathered}$ | Device Variant | Type | $\begin{gathered} r_{o n} \\ {[\mathrm{~m} \Omega]} \end{gathered}$ | $\begin{gathered} C_{s} \\ {[\mathrm{pF}]} \\ \hline \end{gathered}$ | $\begin{gathered} Q_{g} \\ {[\mathrm{nC}]} \\ \hline \end{gathered}$ |
| EPC1012 | GaN | 70 | 8 | - 9 | EPC1014 | GaN | 12.0 | 241 |  |
| EPC1010 | GaN | 18 |  |  | EPC1015 | GaN | 3.2 | 000 |  |
| FDMS2672 | MOS | 64 | 177 | 30 | CSD16325Q5C | MOS | 7 | 3200 | 18.0 |
| IPD320N | MOS | 35 | 379 | 12.0 | STD60N3LH5 | MOS | 8.8 | 713 | 8.8 |
| IRFS4020 | MOS | 85 | 140 | 18.0 | CSD16411Q3 | MOS | 12.0 | 486 | 2.9 |

- Representative sample of HV and LV devices, including Si and GaN devices
- Above $P_{\text {min }}$, all devices have no switching loss, so efficiency only depends on conduction losses
- Initial conclusion is to select lowest $r_{o n}$ devices
- Can solve analytical loss model from state plane analysis


- Analysis predicts that optimal selection consists of lowest $C_{p}$ primary device and lowest $r_{\text {on }}$ secondary device


## $\square$ <br> Device Loss Comparison: 150-12 V



## DAB: Experimental Results




D. Costinett, H. Nguyen, R. Zane, and D. Maksimovic, "GaN-FET based dual active bridge DC-DC converter," in Proc. Appl. Power Electron. Conf. (APEC), march 2011, pp. 1425-1432.
D. Costinett, D. Maksimovic, and R. Zane, "Design and control for high efficiency in high step-down dual active bridge converters operating at high switching frequency," IEEE Trans. Power Electron., vol. PP, no. 99, p. 1, 2012.

## Linear Model Comparison to Simulation

- At high output power and low switching frequency, square wave model of DAB converter accurately predicts behavior of full circuit simulation




## High Frequency, Low Power Operation

- At low output power and high switching frequency, square wave model is poor fit to circuit behavior
- Effect of switching transitions need to be considered



Application Example: Automotive


## Efficiency Results








Fig. 12. (Solid lines) Predicted efficiencies and ( $\square$ ) measured efficiencies for different operating conditions. The efficiencies are calculated with the improved DAB loss model which includes all methods discussed in Section IV.

## Alternate Modulation Schemes



