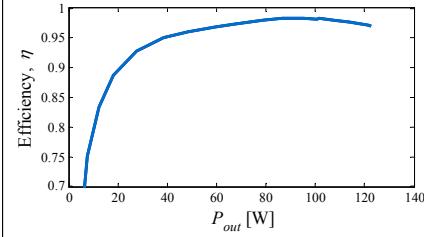
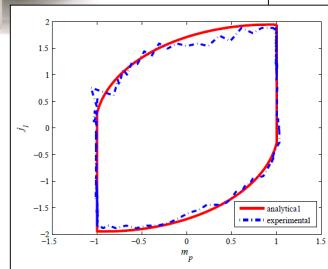
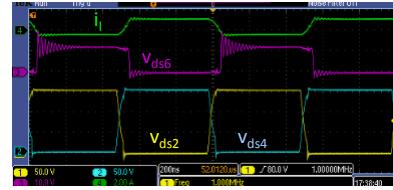
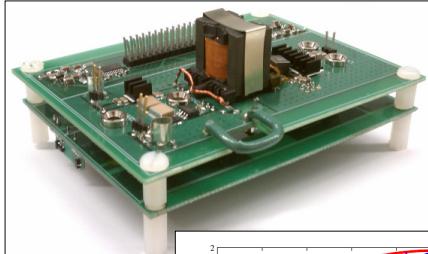


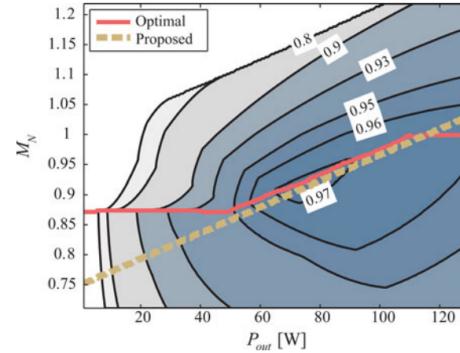
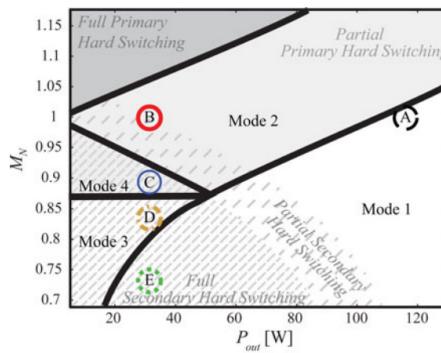
## DAB: Experimental Results



D. Costinett, D. Maksimovic, and R. Zane, "Design and control for high efficiency in high step-down dual active bridge converters operating at high switching frequency," IEEE Trans. Power Electron., vol. PP, no. 99, p. 1, 2012.

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## Soft Switching Range with Varying $V_{out}$



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## Application Example: Automotive

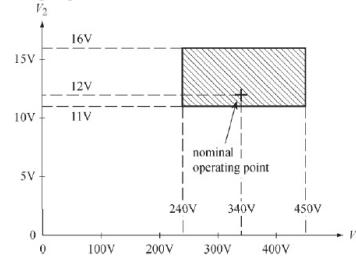


Fig. 1. Converter operating voltage ranges required for automotive application.

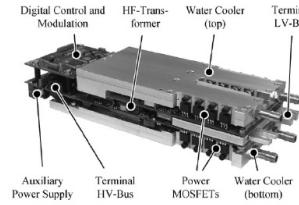
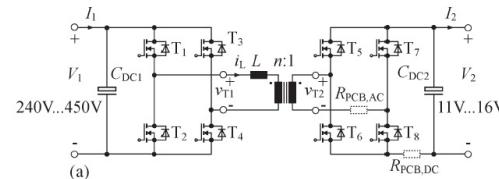


Fig. 3. Automotive DAB converter ( $273 \times 90 \times 53$  mm).



(a)

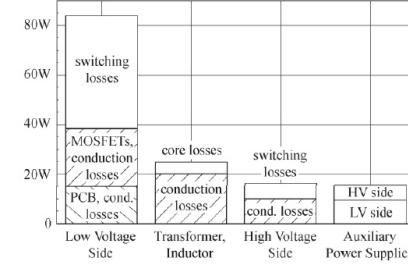
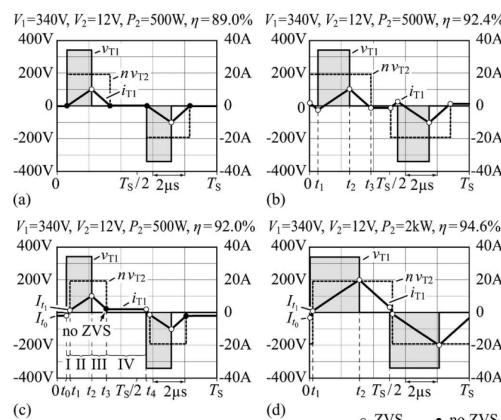
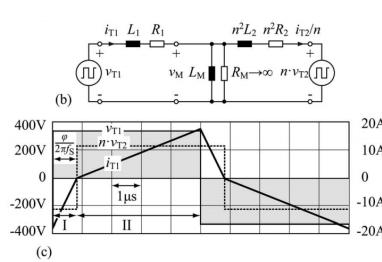


Fig. 13. Calculated distribution of the power losses for operation at  $V_1 = 340$  V,  $V_2 = 12$  V, and  $P_2 = 2$  kW.

\*F. Krismer, J.W.Kolar, "Accurate Power Loss Model Derivation of a High-Current Dual Active Bridge Converter for an Automotive Application, IEEE Trans. On Industrial Electronics, March 2010

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## Alternate Modulation Schemes



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## Efficiency Results

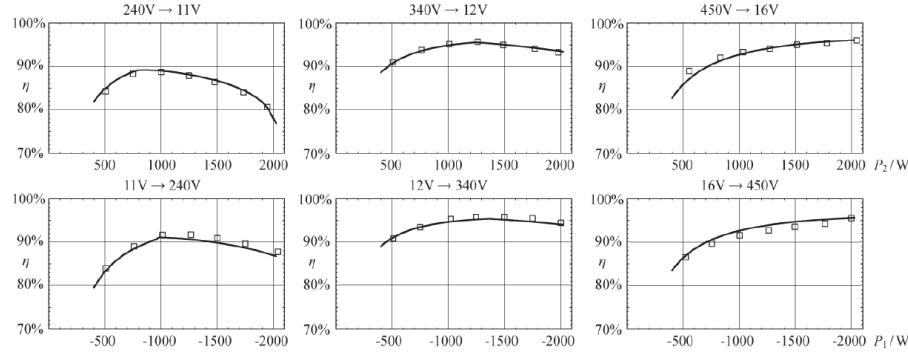
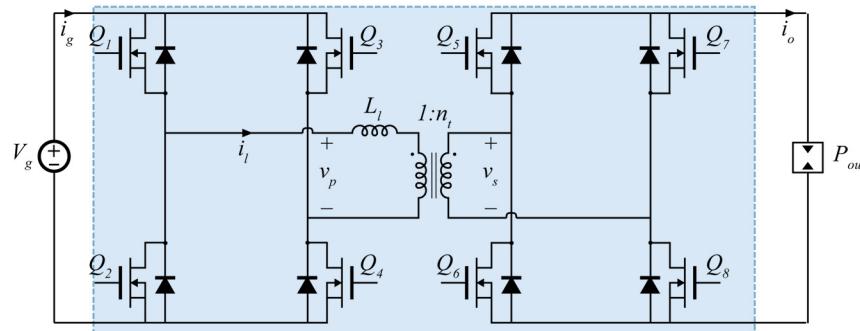


Fig. 12. (Solid lines) Predicted efficiencies and (□) measured efficiencies for different operating conditions. The efficiencies are calculated with the improved DAB loss model which includes all methods discussed in Section IV.

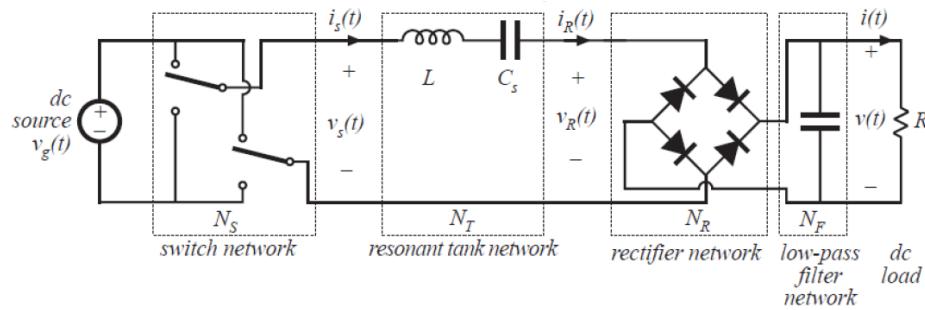
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## Transformer Saturation



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## Next: SRC

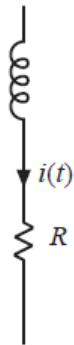


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## Magnetics Losses

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## Magnetics Winding Loss (DC)



- DC Resistance given by

$$R_{DC} = \rho \frac{l_b}{A_w}$$

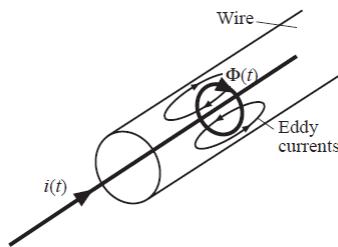
- At room temp,  $\rho = 1.724 \cdot 10^{-6} \Omega\text{-cm}$
- At  $100^\circ\text{C}$ ,  $\rho = 2.3 \cdot 10^{-6} \Omega\text{-cm}$
- Losses due to DC current:

$$P_{cu,DC} = I_{L,rms}^2 R_{DC}$$

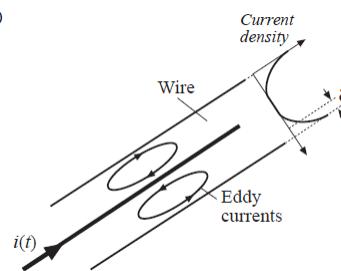


## Skin Effect in Copper Wire

(a)



(b)



- Current profile at high frequency is exponential function of distance from center with characteristic length  $\delta$



## Skin Depth

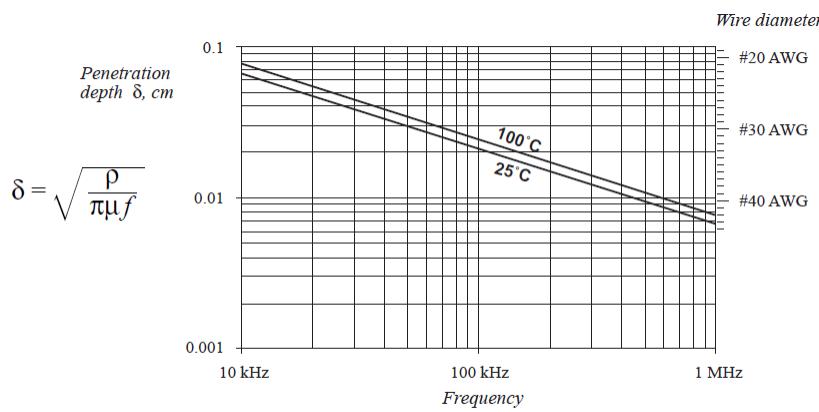
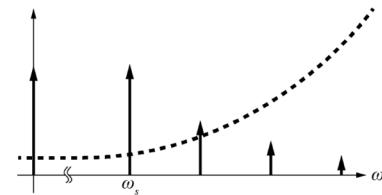


Fig. 13.23 Penetration depth  $\delta$ , as a function of frequency  $f$ , for copper wire.

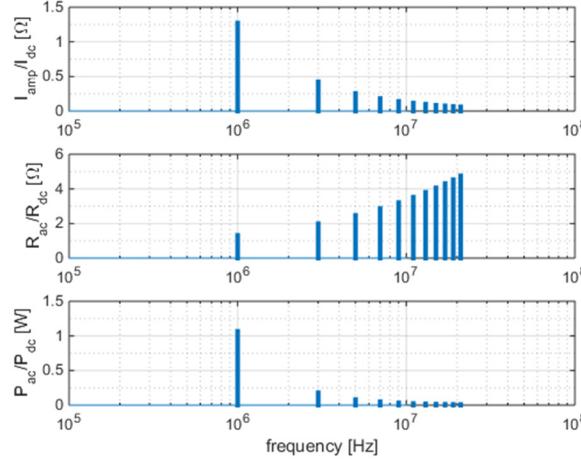
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## Skin Depth Calculations



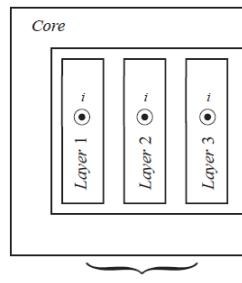
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## Example Calculation

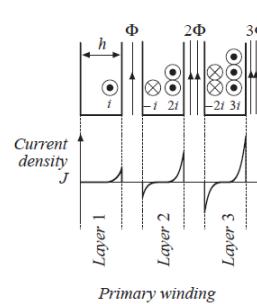


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(a)



(b)



## Proximity Effect

- In *foil* conductor closely spaced with  $h \gg \delta$ , flux between layers generates additional current according to Lentz's law.

$$P_1 = I_{L,rms}^2 R_{ac}$$

- Power loss in layer 2:

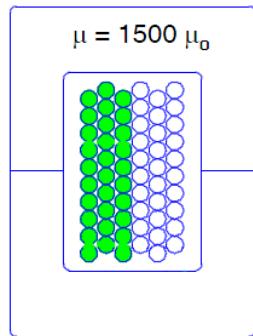
$$P_2 = I_{L,rms}^2 R_{ac} + (2I_{L,rms})^2 R_{ac}$$

$$P_2 = 5P_1$$

See *Fundamentals of Power Electronics*, Section 13.4

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## Simulation Example

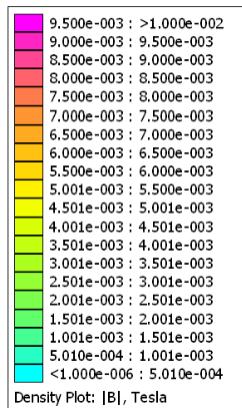


- AWG#30 copper wire
  - Diameter  $d = 0.294$  mm
  - $d = \delta$  at around 50 kHz
- 1:1 transformer
  - Primary and secondary are the same, 30 turns in 3 layers
- Sinusoidal currents,  
 $I_{1rms} = I_{2rms} = 1$  A

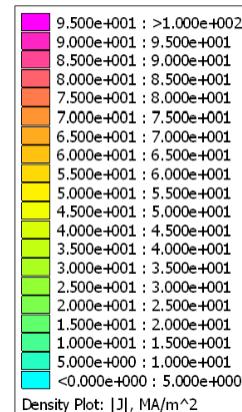
Numerical field and current density solutions using FEMM (Finite Element Method Magnetics), a free 2D solver,  
<http://www.femm.info/wiki/HomePage>



Flux density magnitude

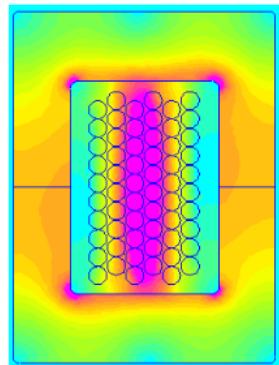


Current density magnitude

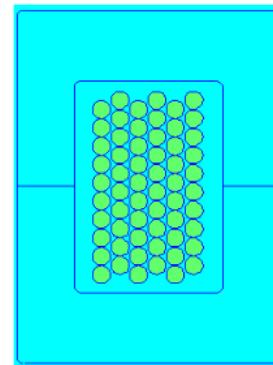


## Frequency: 1 kHz

Flux density

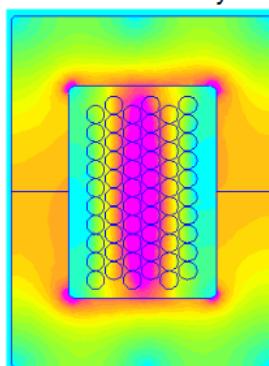


Current Density

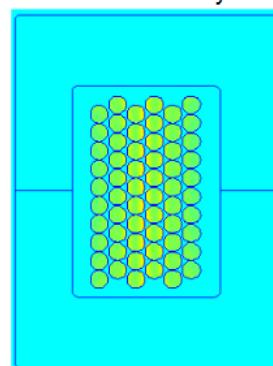


## Frequency: 100 kHz

Flux density



Current Density

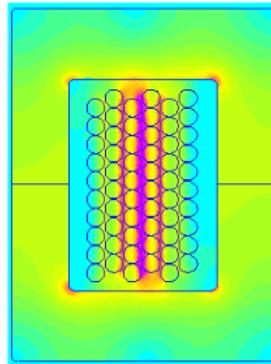


Total copper losses 1.8 larger than at 1 kHz

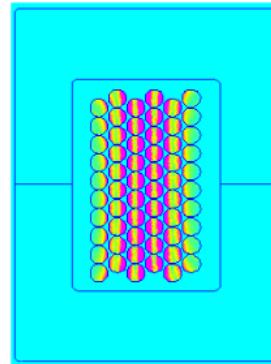


## Frequency: 1 MHz

Flux density



Current Density

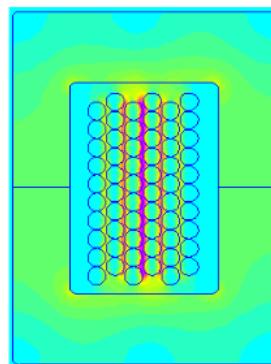


Total copper losses 20 times larger than at 1 kHz

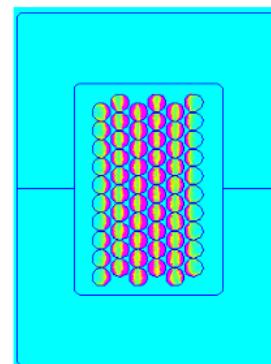


## Frequency: 10 MHz

Flux density



Current Density

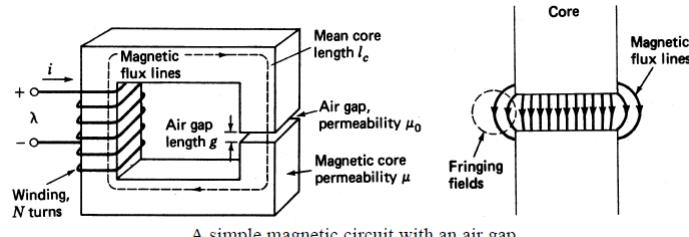


Very significant proximity effect

Total copper losses = 65 times larger than at 1 KHz



## Fringing

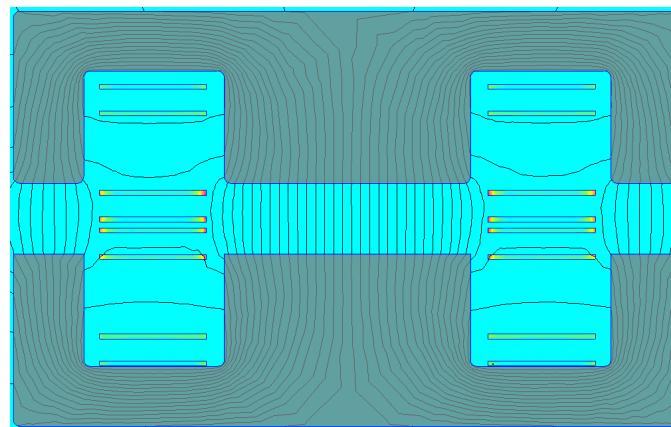


A simple magnetic circuit with an air gap

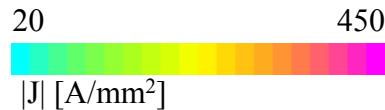
- Near air gap, flux may bow out significantly, causing additional eddy current losses in nearby conductors

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## Finite Element Simulation



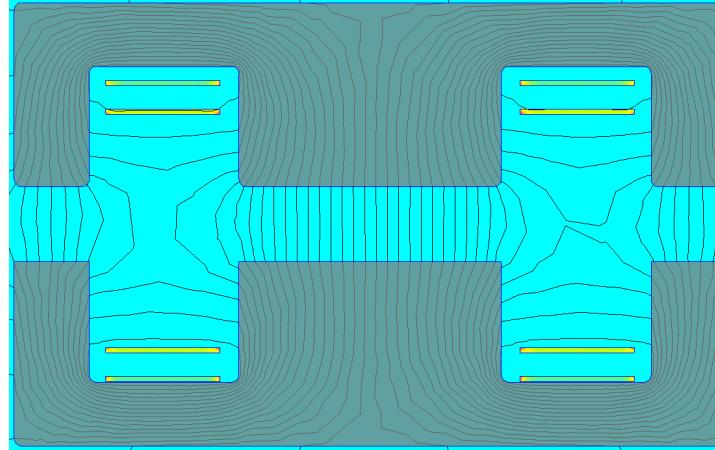
$$P_{cond} = 330 \text{ W}$$



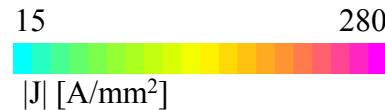
<http://www.femm.info/wiki/HomePage>

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## Removing Copper From Fringing Field



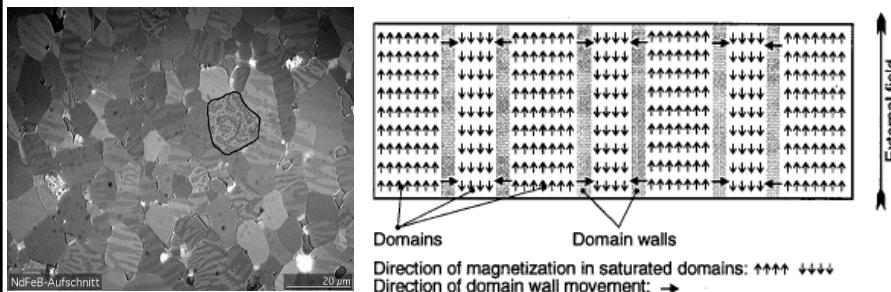
$$P_{cond} = 180 \text{ W}$$



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## Physical Origin of Core Loss

- Magnetic material is divided into “domains” of saturated material
- Both Hysteresis and Eddy Current losses occur from domain wall shifting



Reinert, J.; Brockmeyer, A.; De Doncker, R.W.; "Calculation of losses in ferro- and ferrimagnetic materials based on the modified Steinmetz equation,"

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## Inductor Core Loss

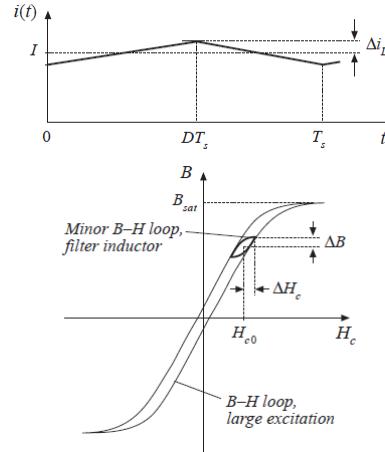
- Governed by Steinmetz Equation:

$$P_v = K_{fe} f_s^\alpha (\Delta B)^\beta \quad [\text{mW/cm}^3]$$

- Parameters  $K_{fe}$ ,  $\alpha$ , and  $\beta$  extracted from manufacturer data

$$P_{fe} = P_v A_c l_m \quad [\text{mW}]$$

- Only valid for sinusoidal waveforms



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## Steinmetz Parameter Extraction

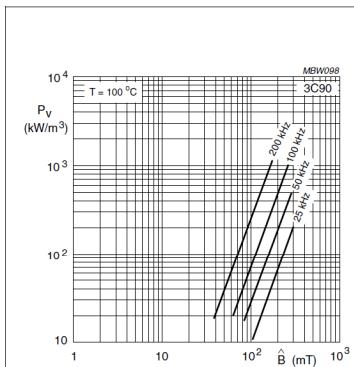


Fig.6 Specific power loss as a function of peak flux density with frequency as a parameter.

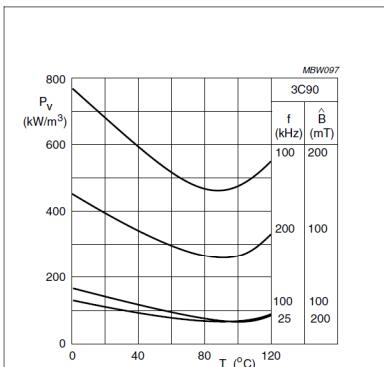


Fig.7 Specific power loss for several frequency/flux density combinations as a function of temperature.

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## Non-Sinusoidal Waveforms

- Modified Steinmetz Equation (MSE)
  - “Guess” that losses depend on  $dB/dt$
  - Calculate  $\langle dB/dt \rangle$  and find frequency of equivalent sinusoid

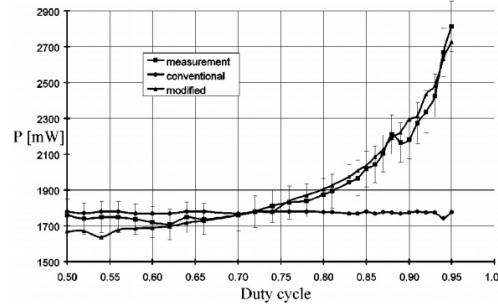


Fig. 8. Comparison between measurement and calculation as a function of duty cycle.

Albach ,Durbau and Brockmeyer, 1996  
Reinert, Brockmeyer, and Doncker, 1999



## NSE/iGSE

$$P_{NSE} = \left( \frac{\Delta B}{2} \right)^{\beta-\alpha} \frac{k_N}{T} \int_0^T \left| \frac{dB}{dt} \right|^{\alpha} dt$$

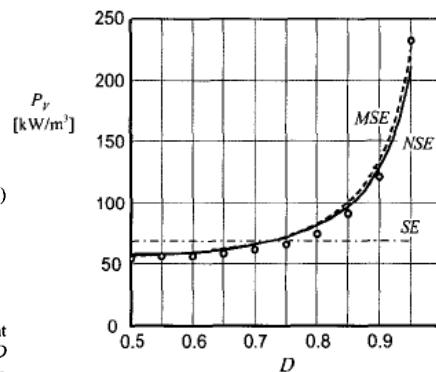
$$k_N = \frac{k}{(2\pi)^{\alpha-1} \int_0^{2\pi} |\cos \theta|^{\alpha} d\theta}$$

**Simple Formula for Square-wave voltages:**

$$P_{NSE} = k_N (2f)^{\alpha} (\Delta B)^{\beta} (D^{1-\alpha} + (1-D)^{1-\alpha}) \quad (10)$$

where  $f$  is the operating frequency;  
 $\Delta B / 2$  is the peak induction;  
 $D$  is the duty ratio of the square wave voltage.

*Note:* The second and third harmonics are dominant at moderate values of duty ratio  $D$ . For extreme values of  $D$  (95%), a higher value of  $\alpha$  could give better matching to the actual losses.



Van den Bossche, A.; Valchev, V.C.; Georgiev, G.B.; "Measurement and loss model of ferrites with non-sinusoidal waveforms," K. Venkatachalam; C. R. Sullivan; T. Abdallah; H. Tacca, "Accurate prediction of ferrite core loss with nonsinusoidal waveforms using only Steinmetz parameters"



## Additional Approaches

- History of Core Loss Approximation Techniques:

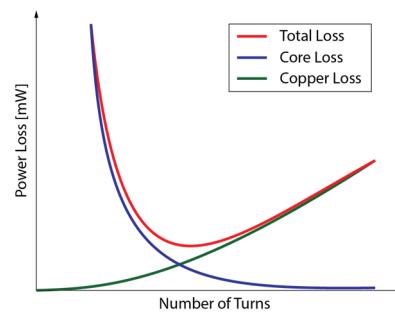
[https://engineering.dartmouth.edu/inductor/Sullivan\\_APEC\\_2012\\_core\\_loss\\_overview\\_with\\_references.pdf](https://engineering.dartmouth.edu/inductor/Sullivan_APEC_2012_core_loss_overview_with_references.pdf)

- Seminar on magnetic loss modeling:

[https://www.pes.ee.ethz.ch/uploads/tx\\_ethpublications/APEC2012\\_MagneticTutorial.pdf](https://www.pes.ee.ethz.ch/uploads/tx_ethpublications/APEC2012_MagneticTutorial.pdf)



## Minimization of Losses



## Spreadsheet Design

|    | A | B        | C         | D | E        | F        | G | H          | I   | J | K | L | M |
|----|---|----------|-----------|---|----------|----------|---|------------|-----|---|---|---|---|
| 1  |   | Vg [V]   | 25        |   | Pmax [W] | 250      |   | Vd [V]     | 12  |   |   |   |   |
| 2  |   | Vout [V] | 50        |   | L [uH]   | 2.00E+01 |   | dV [V]     | 250 |   |   |   |   |
| 3  |   | dV [V]   | 2         |   | f [Hz]   |          |   | dt [ns]    | 500 |   |   |   |   |
| 4  |   | i0 [A]   | 1.257E-06 |   | fs [Hz]  |          |   | Pg_on [W]  | 10  |   |   |   |   |
| 5  |   | Ta [C]   | 160E-06   |   |          |          |   | Pg_off [W] | 2   |   |   |   |   |
| 6  |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 7  |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 8  |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 9  |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 10 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 11 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 12 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 13 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 14 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 15 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 16 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 17 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 18 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 19 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 20 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 21 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 22 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 23 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 24 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 25 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 26 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 27 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 28 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 29 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 30 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 31 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 32 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 33 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 34 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 35 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 36 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 37 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 38 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 39 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 40 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 41 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 42 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 43 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 44 |   |          |           |   |          |          |   |            |     |   |   |   |   |
| 45 |   |          |           |   |          |          |   |            |     |   |   |   |   |

- Use of spreadsheet permits simple iteration of design
- Can easily change core, switching frequency, loss constraints, etc.



## Matlab (Programmatic) Design

```

1 function [n, lg, Pg1, Pg2, Pl, eta, Cmin ] = TestBoostDesign(Pmax, fs, L, dt, core_geom, core_mat, MOSFET)
2 %TestBoostDesign calculate boost converter efficiency and temperature rise
3 %for various designs
4 % fs = switching frequency (in Hz)
5 % L = inductance (in Henries)
6 % n = number of turns on inductor
7 % dt = switching dead time (in seconds)
8 % core_geom = core geometry, chosen from 'EFD25', 'ETD291', 'ETD391', 'ETD441', or 'ETD491'
9 % core_mat = core material, chosen from '3F3', '3C90', or '3F4'
10 % MOSFET = MOSFET selection, chosen from 'AOT1', 'FDP1', 'IPP21', 'IRF',
11 % 'CSD' or 'IPPO'
12
13 - Vg = 25;
14 - Vout = 50;
15 - Iout = Pmax/Vout;
16 - Ts = 1/fs;
17 - D = 1-Vg/Vout;
18 - dVout = 2;
19 - Vdr = 12;
20
21 - Rgon = 10;
22 - Rgoff = 2;
23
24 - rho = 1.724e-6; %ohms*cm
25 - u0 = 4*pi*1e-7;
26
27 %% Inductor Datasheet Parameters
28 - switch core_geom
29 - case 'EFD25'
30 -     MLT = 46.4; %mm
31 -     Ac = 58; %mm^2
32 -     Vs = 3300; %mm^3
33 -     Wa = 40.2; %mm^2

```

- Matlab, or similar, permits more powerful iteration and plotting/insight into design variation

