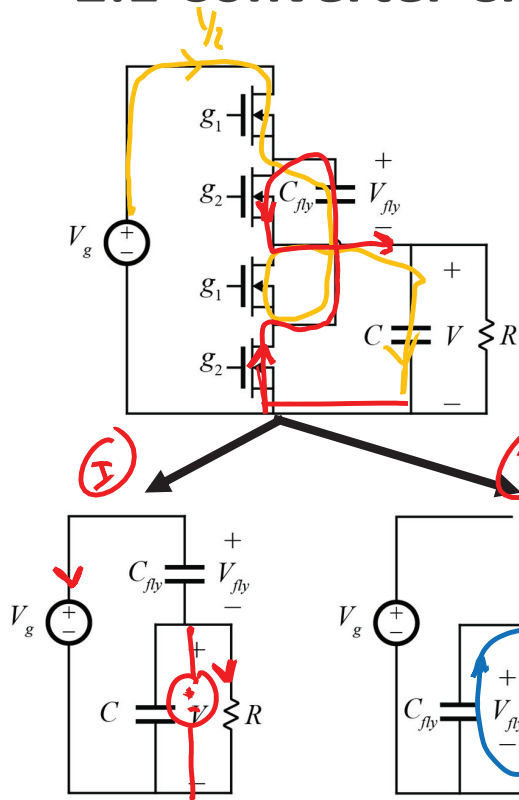


2:1 Converter Charge Vector Analysis



$$\bar{a}^I = [g_{in}^I, g_{fly}^I, g_{out}^I] / g_{out}$$

$$= [-1, 1, 1] / g_{out}$$

$$\bar{a}^I = [-1/2, 1/2, 1/2]$$

$$\bar{a}^{II} = [0, -1, 1] / g_{out}$$

$$\bar{a}^{II} = [0, -1/2, 1/2]$$

$$g_{out} = g_{out}^I + g_{out}^{II} = \underline{2}$$

$$\frac{g_{in}}{g_{out}} = \frac{g_{in}^I + g_{in}^{II}}{g_{out}} = -1/2$$

is a 2:1 converter

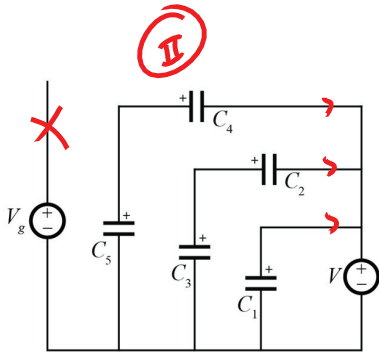
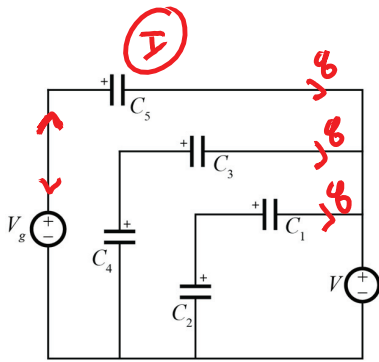
$$R_{o,ssl} = \sum_{\text{caps}} \frac{(a_{ci})^2}{C_i f_s} = \frac{1/4}{C_{fly} f_s} = \frac{1}{4C_{fly} f_s} \checkmark$$

$$\bar{a}_r = [g_{m1}, g_{m2}, g_{m3}, g_{m4}] / g_{out}$$

$$\bar{a}_r = [1/2, 1/2, -1/2, -1/2]$$

$$R_{o,Fsl} = \sum_{i \in \text{switches}} 2R_{on_i} (a_{ri})^2 = \underline{2R_{on}} \checkmark$$

Dickson Charge Vector Analysis



$$\bar{a}^I = [g_{C_5}^I, g_{C_3}^I, g_{C_2}^I, \dots, g_{C_1}^I, g_{out}^I] / g_{out}$$

$$= [-1, 1, -1, 1, -1, 1, 3] / g_{out}$$

$$\bar{a}^I = [-1/6, 1/6, -1/6, 1/6, -1/6, 1/6, 1/2]$$

$$\bar{a}^{II} = [0, -1, 1, -1, 1, -1, 3] / g_{out}$$

$$\bar{a}^{II} = [0, -1/6, \dots, -1/6, 1/2]$$

$$\frac{g_{in}}{g_{out}} = \frac{1}{6} \Rightarrow 6:1 \text{ converter}$$

$$P_{loss} = \sum_{i \in caps} \frac{(a_i)^2}{C_i f_s} = \frac{5}{36} \frac{1}{C_{eff} f_s}$$

$$\text{if } C_1 \dots C_5 = C_{eff}$$

Charge Vector Analysis in FSL

$$\bar{a}_r = \frac{\bar{g}_r}{g_{out}} \Rightarrow g_{r,i} = \text{charge that flows through switch } i \text{ when it is conducting}$$

↳ some linear combination of \bar{a}^I & \bar{a}^{II}

in FSL, currents constant within I & II

$i_{r,i}$ = current in switch i when conducting

$$i_{r,i} = g_{r,i} \frac{2}{f_s}$$

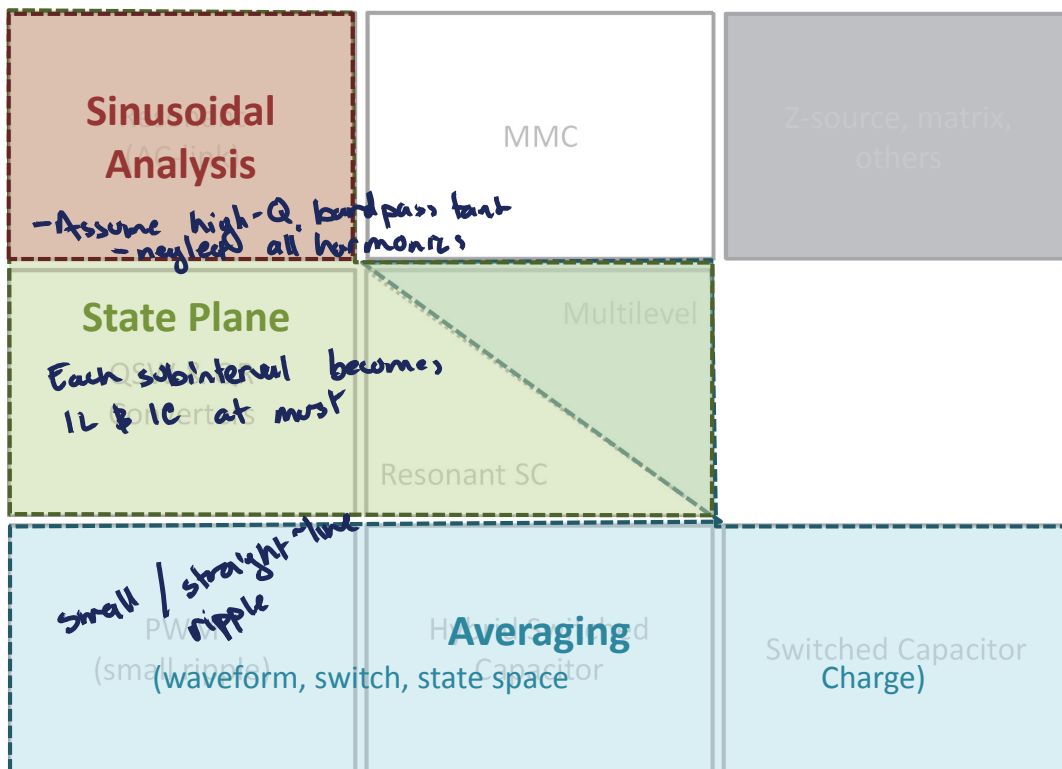
$$P_{r,i} = (i_{r,i})^2 R_{on,i} \cdot \frac{1}{2} = (g_{r,i} \frac{2}{f_s})^2 R_{on,i} \frac{1}{2} = g_{r,i}^2 f_s^2 \cdot 2 R_{on,i}$$

$$P_{r,i} = a_{r,i}^2 \underbrace{g_{out}^2}_{I_{out}^2} f_s^2 \cdot 2 R_{on,i}$$

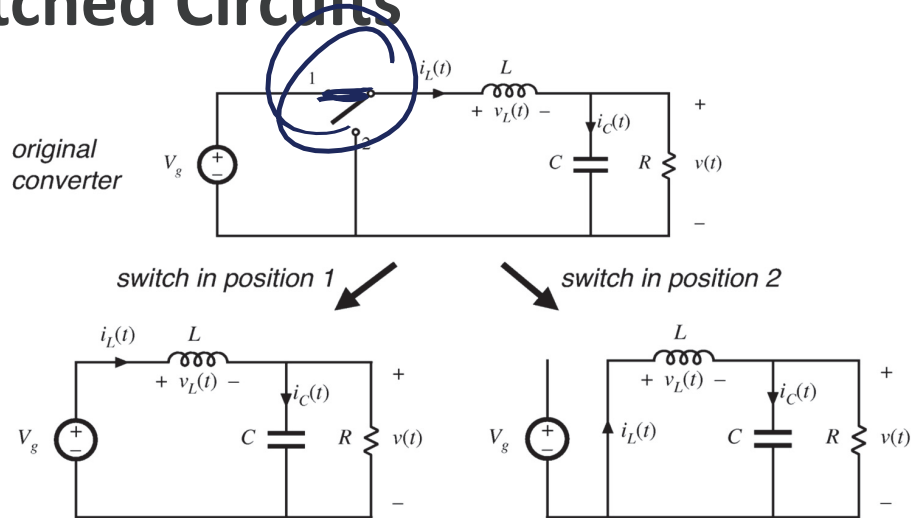
$$P_{r,FSL} = \sum_{i \in switches} 2 R_{on,i} (a_{r,i})^2$$

DISCRETE TIME MODELING

Converter Analysis



Switched Circuits



Historical Perspective



Robert D Middlebrook

PhD, Stanford, 1955

CalTech Professor, 1955-1998



Slobodan Cúk

PhD CalTech, 1976

CalTech Prof, 1977-1999

*Modelling, analysis, and design of
switching converters*

Model a switched system as an
averaged, time-invariant system with

$$\dot{x}(t) = Ax(t) + Bu(t)$$

where

$$A = DA_1 + D'A_2$$

$$B = DB_1 + D'B_2$$