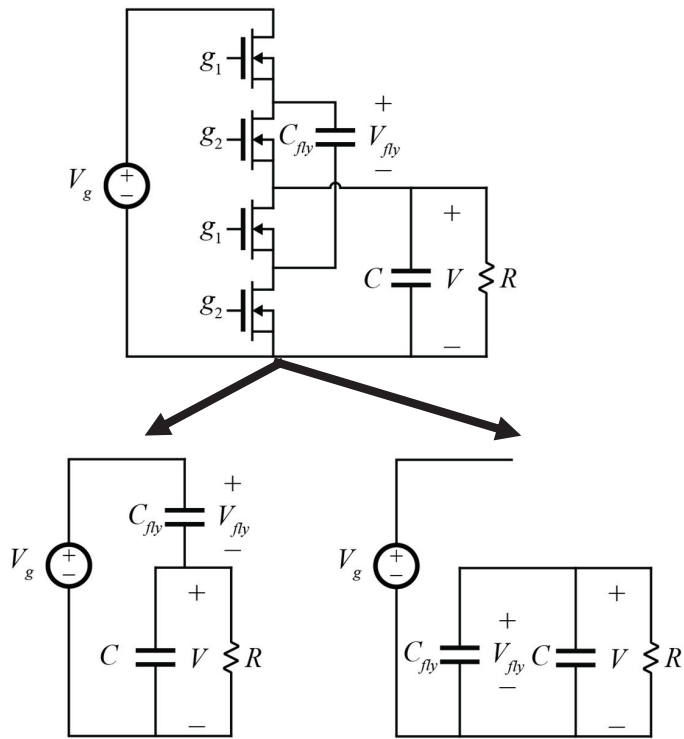
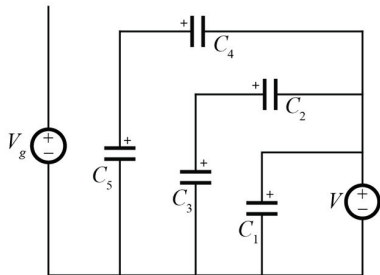
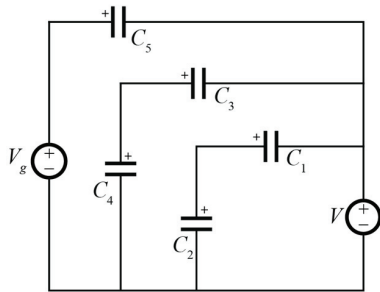


# 2:1 Converter Charge Vector Analysis



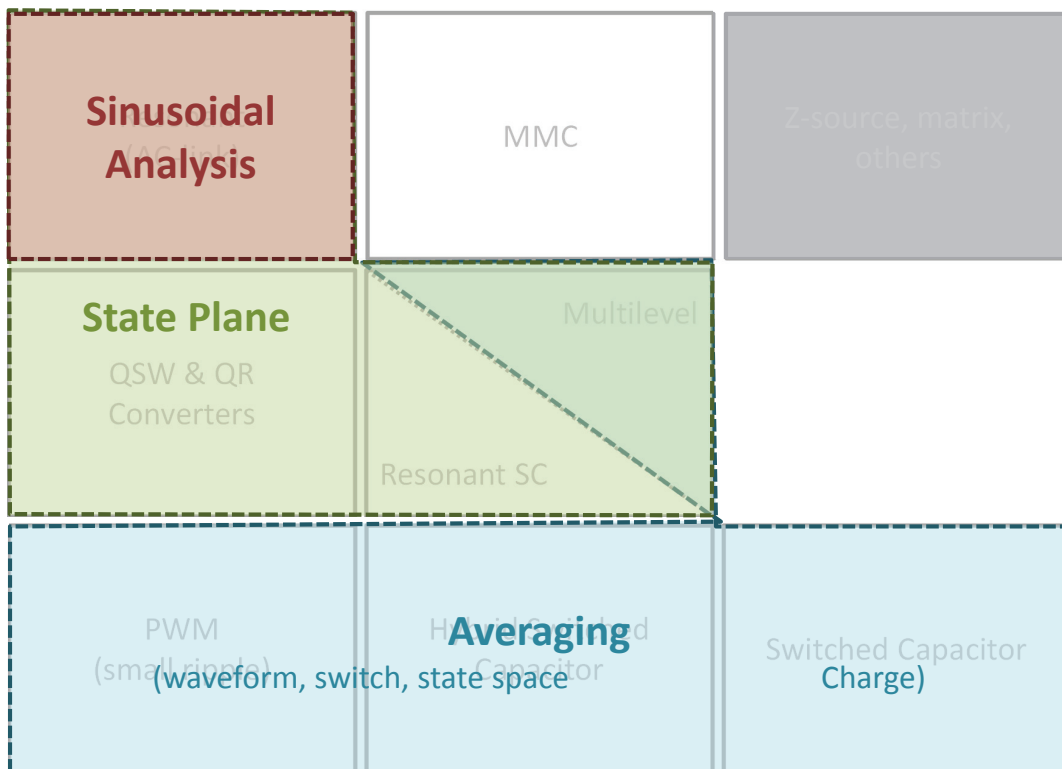
# Dickson Charge Vector Analysis



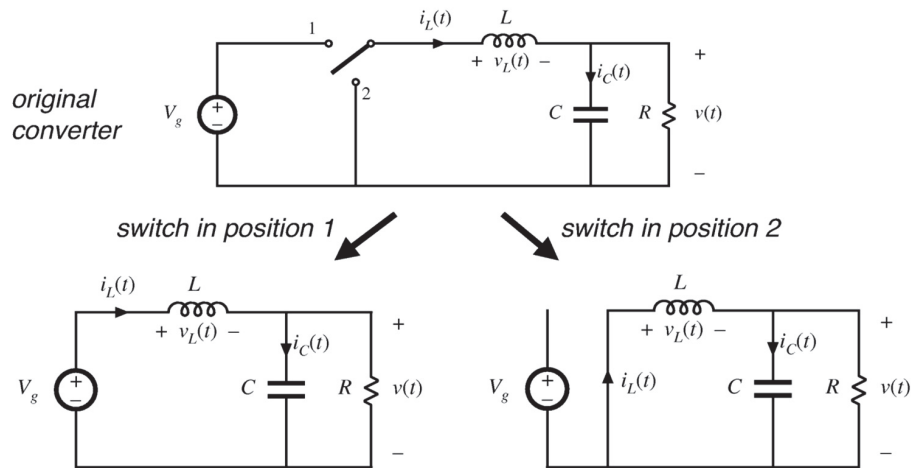
## Charge Vector Analysis in FSL

# DISCRETE TIME MODELING

## Converter Analysis



# Switched Circuits



## Historical Perspective



**Robert D Middlebrook**

PhD, Stanford, 1955

CalTech Professor, 1955-1998



**Slobodan Cúk**

PhD CalTech, 1976

CalTech Prof, 1977-1999

*Modelling, analysis, and design of  
switching converters*

Model a switched system as an  
averaged, time-invariant system with

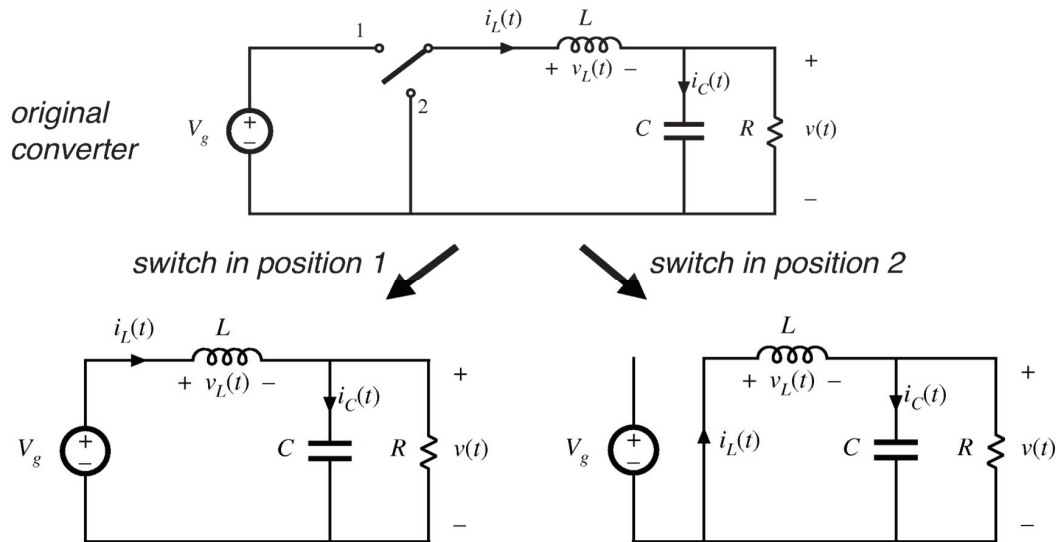
$$\dot{x}(t) = Ax(t) + Bu(t)$$

where

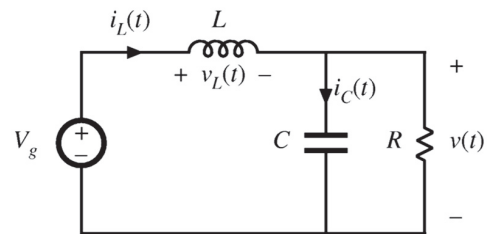
$$A = DA_1 + D'A_2$$

$$B = DB_1 + D'B_2$$

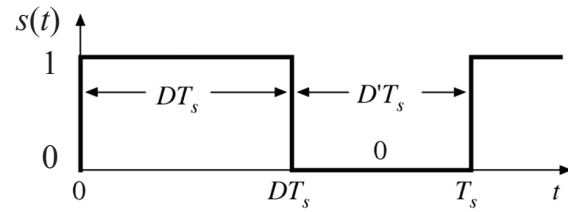
# Large Signal Modeling of SMPS: Averaging



## Linear Circuit Modeling Using State Space

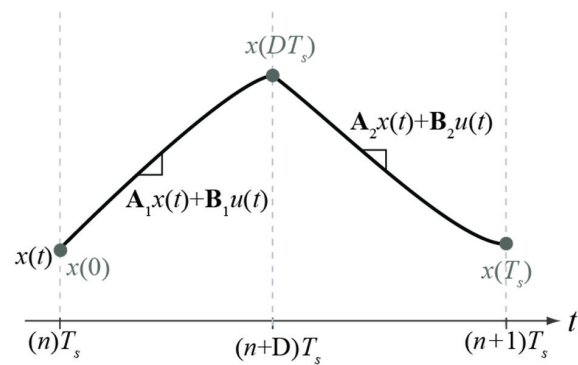


# Switching Signal

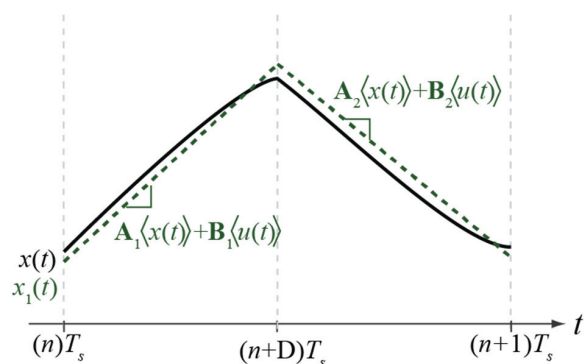


## Converting to Linear System

# Approximate Steady State Waveforms

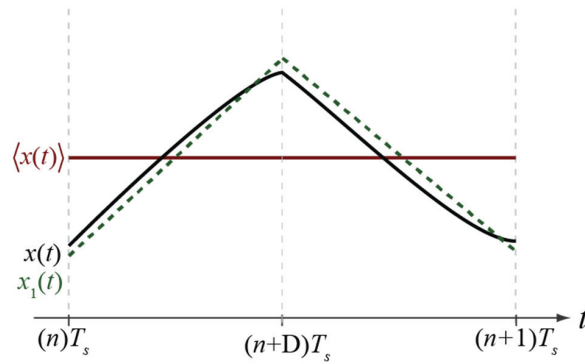


# Approximate Steady State Waveforms



$$\langle x(t) \rangle = \frac{1}{T_s} \int_0^{T_s} x(t) dt$$

# Approximate Steady State Waveforms

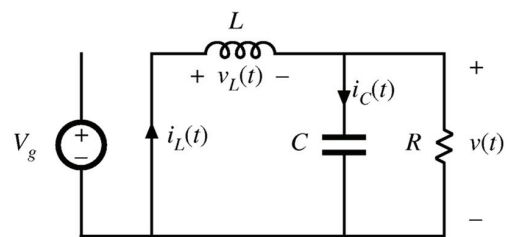
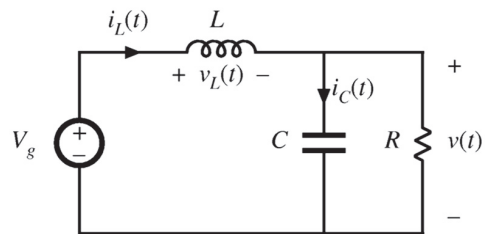


## The Averaging Approximation



# The Averaged System

## Buck State Space Averaging



# Buck Averaged Model