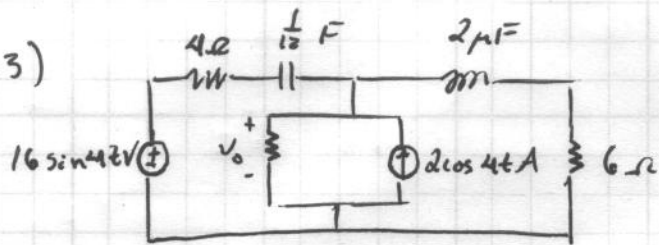


(10.3)

Determine  $V_o$  in the circuit.

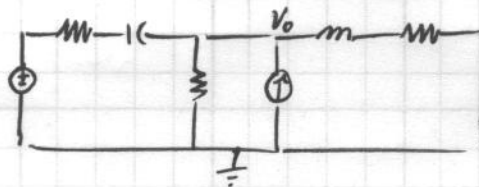
$$\omega = 4$$

$$2 \cos 4t = 2 \angle 0$$

$$16 \sin 4t = 16 \angle -90 = -j16$$

$$2 \text{ H} = j\omega L = j8$$

$$\frac{1}{12} \text{ F} = \frac{1}{j\omega C} = -j3$$



Nodal Analysis:

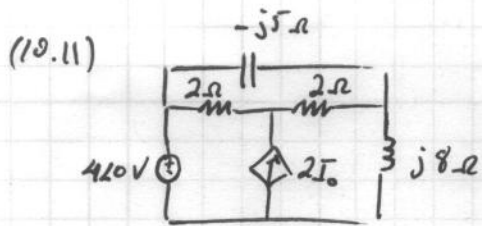
$$\frac{-j16 - V_o}{4 - j3} + 2 = \frac{V_o}{6 + j8} + \frac{V_o}{6}$$

$$\frac{-j16}{4 - j3} + 2 = \left(1 + \frac{1}{4 - j3} + \frac{1}{6 + j8}\right) V_o$$

$$V_o = \frac{3.97 - j2.56}{1.22 + j0.04} = \frac{4.647 \angle -33.15^\circ}{1.2207 \angle 1.88^\circ}$$

$$= 3.835 \angle -35.02^\circ$$

$$V_o(t) = \underline{\underline{3.835 \cos(4t - 35.02^\circ) \text{ V}}}$$



Determine  $I_0$

$$\text{Node : 1: } \frac{V_1 - 420}{2} - 2I_0 + \frac{V_1 - V_2}{2} = 0$$

$$V_1 - 0.5V_2 - 2I_0 = 2$$

$$I_0 = \frac{(4 - V_2)}{-j5} = -j0.2V_2 + j0.8$$

$$V_1 - 0.5V_2 + j0.4V_2 - j1.6 = 2$$

$$V_1 + (-0.5 + j0.4)V_2 = 2 + j1.6$$

$$\text{Node : 2: } \frac{V_2 - V_1}{2} + \frac{V_2 - 4}{-j5} + \frac{V_2 - 0}{j8} = 0$$

$$-0.5V_1 + (0.5 + j0.075)V_2 = j0.8$$

$$Y = \begin{bmatrix} 1 & -0.5 + j0.4 \\ -0.5 & 0.5 + j0.075 \end{bmatrix}$$

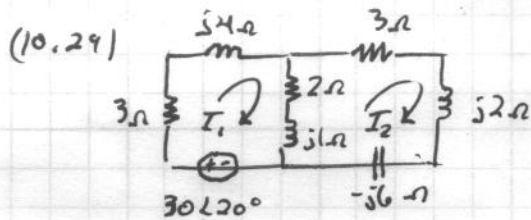
$$I = \begin{bmatrix} 2 + j1.6 \\ 0 + j0.8 \end{bmatrix}$$

$$V = Y^{-1} * I = \begin{matrix} 4.8597 + j0.0543 \\ 4.9955 + j0.9050 \end{matrix}$$

$$I_0 = -j0.2V_2 + j0.8 = -j0.9992 + 0.01086 + j0.8$$

$$= 0.01086 - j0.1992$$

$$= \underline{\underline{199.5 \angle 86.89^\circ \text{ mA}}}$$



Find  $I_1$  and  $I_2$  using mesh analysis.

$$\text{mesh 1: } (5 + j5)I_1 - (2 + j)I_2 - 30 \angle 20^\circ = 0$$

$$30 \angle 20^\circ = (5 + j5)I_1 - (2 + j)I_2$$

$$\text{mesh 2: } (5 + j3 - j6)I_2 - (2 + j)I_1 = 0$$

$$0 = -(2 + j)I_1 + (5 - j3)I_2$$

$$\begin{bmatrix} 30 \angle 20^\circ \\ 0 \end{bmatrix} = \begin{bmatrix} 5 + j5 & -(2 + j) \\ -(2 + j) & 5 - j3 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$\Delta = 37 + j6$$

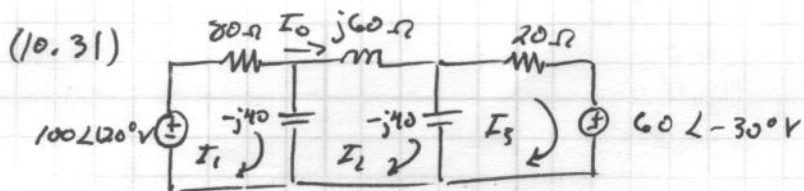
$$= 37.49 \angle 9.21^\circ$$

$$\Delta_1 = (30 \angle 20^\circ)(5.831 \angle -30.96^\circ) = 175 \angle -10.96^\circ$$

$$\Delta_2 = (30 \angle 20^\circ)(2.356 \angle 26.56^\circ) = 67.08 \angle 46.56^\circ$$

$$I_1 = \frac{\Delta_1}{\Delta} = \underline{\underline{4.67 \angle -20.17^\circ \text{ A}}}$$

$$I_2 = \frac{\Delta_2}{\Delta} = \underline{\underline{1.79 \angle 37.35^\circ \text{ A}}}$$



$$\text{Loop 1: } -100 \angle 120^\circ + (80 - j40) I_1 + j40 I_2 = 0$$

$$10 \angle 20^\circ = 4(2 - j) I_1 + j4 I_2$$

$$\text{Loop 2: } j40 I_1 + (j60 - j80) I_2 + j40 I_3 = 0$$

$$0 = 2 I_1 - I_2 + 2 I_3$$

$$\text{Loop 3: } 60 \angle -30^\circ + (20 - j40) I_3 + j40 I_2 = 0$$

$$-6 \angle -30^\circ = j4 I_2 + 2(1 - j2) I_3$$

$$2 I_3 = I_2 - 2 I_1$$

Substituting:

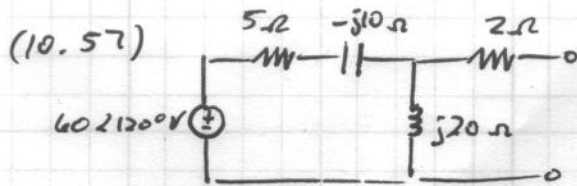
$$-6 \angle -30^\circ = -2(1 - j2) I_1 + (1 + j2) I_2$$

$$\begin{bmatrix} 10 \angle 120^\circ \\ -6 \angle -30^\circ \end{bmatrix} = \begin{bmatrix} 4(2 - j) & j4 \\ -2(1 - j) & 1 + j2 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$A = \begin{bmatrix} 8 - j4 & -j4 \\ -2 + j4 & 1 + j2 \end{bmatrix} \cdot 37 + j20 = 37.74 \angle 32^\circ$$

$$A_2 = \begin{bmatrix} 8 - j4 & 10 \angle 120^\circ \\ -2 + j4 & -6 \angle -30^\circ \end{bmatrix} = -4.928 + j582.11$$

$$I_0 = I_2 = \frac{A_2}{A} = \underline{\underline{2.179 \angle 61.44^\circ \text{ A}}}$$



- Find the Thevenin and Norton equivalent circuits

$$Z_n = Z_{th} = 2 + j20 \parallel (5 - j10) = 2 + \frac{(j20)(5 - j10)}{5 + j10}$$

$$= 18 - j12 = \underline{\underline{21.63 \angle -33.7^\circ \Omega}}$$

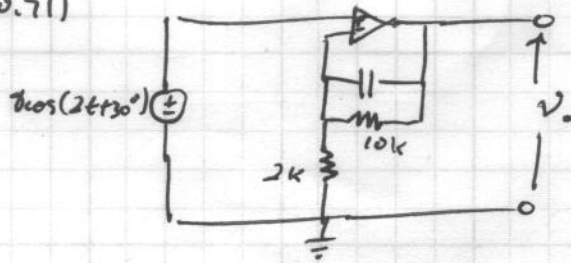
$$V_{th} = \frac{j20}{5 - j10 + j20} (60 \angle 120^\circ) = \frac{j4}{1 + j2} (60 \angle 120^\circ)$$

$$= \underline{\underline{107.3 \angle 146.56^\circ V}}$$

$$I_N = \frac{V_{th}}{Z_{th}} = \underline{\underline{4.961 \angle -179.7^\circ A}}$$



(10.71)

Find  $V_o$  in the opamp circuit.

$$8 \cos(2t + 30^\circ) \rightarrow 8 \angle 30^\circ$$

$$0.5 \mu\text{F} \rightarrow \frac{1}{j\omega C} = \frac{1}{(j2)(0.5)(10^{-6})} = -j1 \text{M}\Omega$$

$$\text{Inverting Terminal: } \frac{V_o - 8 \angle 30^\circ}{-j1000k} + \frac{V_o - 8 \angle 30^\circ}{10k} = \frac{8 \angle 30^\circ}{2k}$$

$$V_o (1 - j100) = 8 \angle 30^\circ + 800 \angle -60^\circ + 4000 \angle -60^\circ$$

$$V_o = \frac{6.928 + j4 + 2400 - j4157}{1 - j100} = \frac{4800 \angle -59.9^\circ}{100 \angle -89.43^\circ}$$

$$= 48 \angle 29.53^\circ$$

$$V_o(t) = \underline{\underline{48 \cos(2t + 29.53^\circ) \text{ V}}}$$