ECE 301
Fall Semester, 2006
HW Set \#10
Due: November 2, 2006 wlg

Name $\qquad$
Print(last, first)
circle: $\quad 2: 10$ section $\quad 3: 40$ section
Use Engineering Paper. Work only on one side of the paper. Use this sheet as your cover sheet, placed on top of your work and stapled in the top left-hand corner. Number the problems at the top of the page, in the center of the sheet. Do neat work. Underline your answers. Show how you got your equations. Be sure to show how you got your answers. Each problem counts 10 points. Note: Unless otherwise stated, all voltages and currents are peak values.
(1) Consider the circuit of Figure 10.1.
(a) Find the average power generated by each source. Ans: $\mathrm{P}_{\mathrm{S} 1 \text { (gen) }}=367.8 \mathrm{~W}, \mathrm{P}_{\mathrm{S} 2(\mathrm{gen})}=-207.8 \mathrm{~W}$
(b) Find the average power absorbed by each circuit element. Ans: $\mathrm{P}_{1}=160 \mathrm{~W}, \mathrm{P}_{2}=\mathrm{P}_{3}=0$.


Figure 10.1: Circuit for problem 1.
(2) Consider the circuit shown in Figure 10.2.
(a) Find $\mathrm{Z}_{\mathrm{L}}$ for maximum power transfer. Ans: $\mathrm{Z}_{\mathrm{L}}=3.415-\mathrm{j} 0.7317 \Omega$
(b) Calculate the maximum average power with this load. Ans: 1.429 W .


Figure 10.2: Circuit for problem 2.
(3) You ae given the voltage waveform shown in Figure 10.3.
(a) Find the RMS value of the voltage waveform. Ans: 2.92 V
(b) Find the average power absorbed by a $2 \Omega$ resistor when the voltage is applied across the resistor. Ans: $\mathrm{P}=4.267 \mathrm{~W}$


Figure 10.3: Waveform for problem 3.
(4) For the power system shown in Figure 10.4 , with 220 V rms applied, find;
(a) the average power. Ans: $\mathrm{P}=1634.7 \mathrm{~W}$
(b) the reactive power. Ans: $\mathrm{Q}=913.47 \mathrm{VA}$ (vars)
(c) the power factor. Ans: $\mathrm{pf}=0.8732$ leading


Figure 10.4: Circuit for problem 4.
(5) For the following voltage and current phasors calculate the (i) complex power, (ii) apparent power, (iii) real power, (iiii) reactive power, (v) specify whether the pf is leading or lagging.

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\begin{aligned}
& \text { (a) } V=220 \angle 30^{\circ} V \mathrm{rms}, I=0.5 \angle 60^{\circ} \mathrm{Arms} \\
& \text { Ans :95.26-j55VA,110VA, 92.26W, 55VARs, pf leading } \\
& \text { (b) } V=250 \angle-10^{\circ} V \mathrm{rms}, I=6.2 \angle-25^{\circ} \mathrm{Arms} \\
& \text { Ans:1497.2+j401.2VA, 1550VA, 1497.2W, 401.2VARs, pf lagging } \\
& \text { (c) } V=120 \angle 0^{\circ} V \mathrm{rms}, I=2.4 \angle-15^{\circ} \mathrm{Arms} \\
& \text { Ans: } 278.2+j 74.5 V A, 288 V A, 278.2 W, 74.54 V A R s, p f \text { lagging } \\
& \text { (d) } V=160 \angle 45^{\circ} V \mathrm{rms}, I=8.5 \angle 90^{\circ} \mathrm{Arms} \\
& \text { Ans :961.7 - j961.7VA, 1360VA, 961.7W, 961.7VARs, pf leading }
\end{aligned}
$$

(6) For the entire circuit of Figure 10.6 calculate:
(a) the power factor, $\mathrm{pf}=.9956$ lagging
(b) the average power delivered by the source, $\mathrm{P}=15.56 \mathrm{~W}$
(c) the reactive power, $\mathrm{Q}=1.466$ VARs
(d) the apparent power, $|\mathrm{S}|=15.63$ VA
(e) the complex power $. \mathbf{S}=15.56+\mathrm{j} 1.466 \mathrm{VA}$


Figure 10.6: Circuit for problem 6.
(7) Find $\mathbf{I}_{\mathbf{0}}$ in the circuit of Figure 10.7. Ans: $443 \angle-28.13^{\circ}$ A.


Figure 10.7: Circuit for problem 10.7.
(8) An ac motor with impedance $\mathrm{Z}_{\mathrm{L}}=4.2+\mathrm{j} 3.6 \Omega$ is supplied by a $220 \mathrm{~V} \mathrm{rms}, 60-\mathrm{Hz}$ source.
(a) Find the $\mathrm{pf}, \mathrm{P}$, and Q: Ans: $\mathrm{pf}=0.7592$ lagging, $\mathrm{P}=6.643 \mathrm{~kW}, \mathrm{Q}=5.695 \mathrm{kVARs}$
(b) Determine the capacitor required to be connected in parallel with the motor so that the power factor is corrected to unity. Ans: $\mathrm{C}=312 \mu \mathrm{~F}$
(9) For the network given in Figure 10.9, find the complex power absorbed by each element and the complex power supplied by the source.
Ans: S supplied by the source: $5.12+\mathrm{j} 2.56$ VA
S absorbed by the resistor: 5.12 VA (watts)
S absorbed by capacitor: -j3.84 VA
S absorbed by the inductor: j6.4 VA


Figure 10.9: Circuit for problem 9.

