

# ECE 471/571 – Lecture 11

## Classifier Fusion

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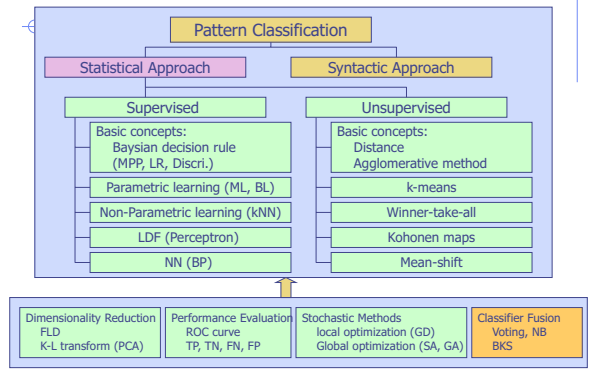
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### Recap



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Three heads are better than one.

### Motivation

- ◆ **Combining classifiers to achieve higher accuracy**
  - Combination of multiple classifiers
  - Classifier fusion
  - Mixture of experts
  - Committees of neural networks
  - Consensus aggregation
  - ...
- ◆ **Reference:**
  - L. I. Kuncheva, J. C. Bezdek, R. P. W. Duin, "Decision templates for multiple classifier fusion: an experimental comparison," *Pattern Recognition*, 34: 299-314, 2001.

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## Popular Approaches

- ◆ Majority voting
- ◆ Naive Bayes combination (NB)
- ◆ Behavior-knowledge space (BKS)
- ◆ Interval-based integration

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## Consensus patterns

- ◆ Unanimity (100%)
- ◆ Simple majority (50%+1)
- ◆ Plurality (most votes)

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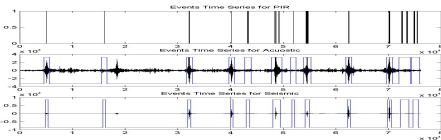
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## Example of Majority Voting - Temporal Fusion

- ◆ Fuse all the 1-sec sub-interval local processing results corresponding to the same event (usually lasts about 10-sec)
- ◆ Majority voting

$$\bar{\varphi}_i^j = \arg \max_c \varphi_c, \quad c \in [1, C]$$

number of local output c occurrence      number of possible local processing results



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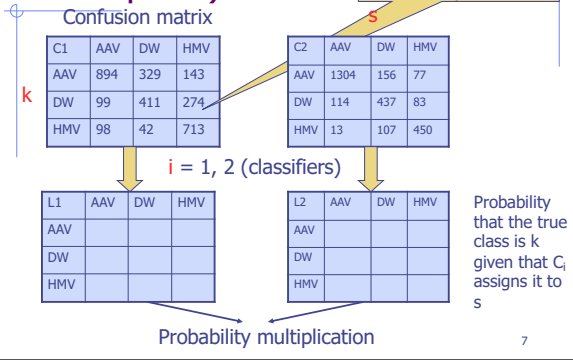
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# NB (the independence assumption)




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# NB - Derivation

- Assume the classifiers are mutually independent
- Bayes combination - Naive Bayes, simple Bayes, idiot's Bayes
- Assume
  - $L$  classifiers,  $i=1, \dots, L$
  - $c$  classes,  $k=1, \dots, c$
  - $s_i$ : class label given by the  $i^{\text{th}}$  classifier,  $i=1, \dots, L, s = \{s_1, \dots, s_L\}$

$$P(\omega_k | s) = \frac{P(s | \omega_k) P(\omega_k)}{P(s)} = \frac{P(\omega_k) \prod_{i=1}^L P(s_i | \omega_k)}{P(s)}$$

$$P(\omega_k) = N_k / N$$

$$P(s_i | \omega_k) = cm_{k,s_i} / N_k$$

$$P(\omega_k | s) \propto \frac{1}{N_k^{L-1}} \prod_{i=1}^L cm_{k,s_i}^i$$

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# BKS

- Majority voting won't work
- Behavior-Knowledge Space algorithm (Huang&Suen)

Assumption:

- 2 classifiers
- 3 classes
- 100 samples in the training set

Then:

- 9 possible classification combinations

$c_1, c_2$	samples from each class	fused result
1,1	10/3/3	1
1,2	3/0/6	3
1,3	5/4/5	1,3
	...	
3,3	0/0/6	3

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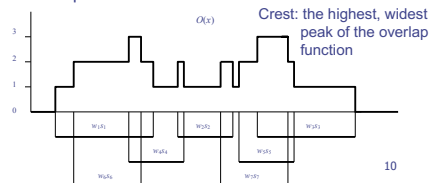
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## Value-based vs. Interval-based Fusion

- ◆ Interval-based fusion can provide fault tolerance
- ◆ Interval integration – overlap function
  - Assume each sensor in a cluster measures the same parameters, the integration algorithm is to construct a simple function (overlap function) from the outputs of the sensors in a cluster and can resolve it at different resolutions as required



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## A Variant of kNN

- ◆ Generation of local confidence ranges (For example, at each node  $i$ , use kNN for each  $k \in \{5, \dots, 15\}$ )

	Class 1	Class 2	...	Class n	
$k=5$	3/5	2/5	...	0	confidence level
$k=6$	2/6	3/6	...	1/6	
...	...	...	...	...	
$k=15$	10/15	4/15	...	1/15	
	{2/6, 10/15}	{4/15, 3/6}	...	{0, 1/6}	confidence range

smallest largest in this column

- ◆ Apply the integration algorithm on the confidence ranges generated from each node to construct an overlapping function

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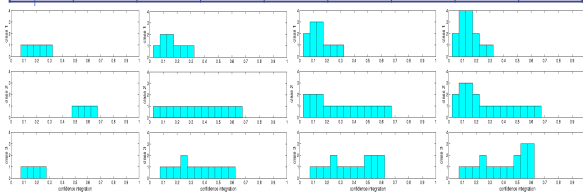
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## Example of Interval-based Fusion

	stop 1		stop 2		stop 3		stop 4	
	c	acc	c	acc	c	acc	c	acc
class 1	1	0.2	0.5	0.125	0.75	0.125	1	0.125
class 2	2.3	0.575	4.55	0.35	0.6	0.1	0.75	0.125
class 3	0.7	0.175	0.5	0.25	3.3	0.55	3.45	0.575



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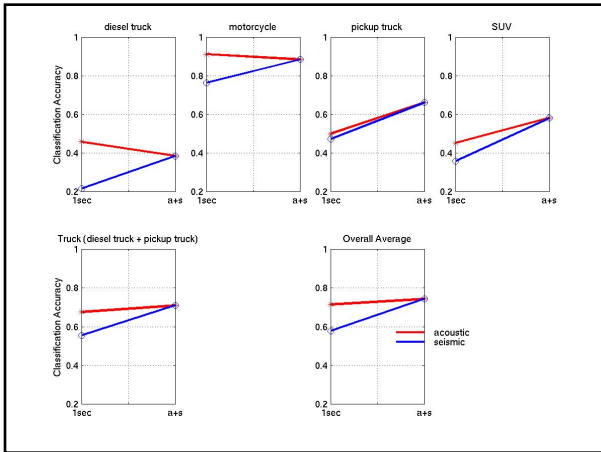
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## Reference

◆ For details regarding majority voting and Naïve Bayes, see

[http://www.cs.rit.edu/~nan2563/combining\\_classifiers\\_notes.pdf](http://www.cs.rit.edu/~nan2563/combining_classifiers_notes.pdf)

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