IV. Evolutionary Computing

A. Genetic Algorithms

Read Flake, ch. 20

Genetic Algorithms

- Developed by John Holland in '60s
- Did not become popular until late '80s
- A simplified model of genetics and evolution by natural selection
- Most widely applied to optimization problems (maximize "fitness")

Assumptions

- Existence of fitness function to quantify merit of potential solutions
 - This "fitness" is what the GA will maximize
- A mapping from bit-strings to potential solutions
 - best if each possible string generates a legal potential solution
 - choice of mapping is important
 - can use strings over other finite alphabets

Outline of Simplified GA

- 1. Random initial population P(0)
- 2. Repeat for $t = 0, ..., t_{\text{max}}$ or until converges:
 - a) create empty population P(t + 1)
 - b) repeat until P(t + 1) is full:
 - 1) select two individuals from P(t) based on fitness
 - 2) optionally mate & replace with offspring
 - 3) optionally mutate offspring
 - 4) add two individuals to P(t + 1)

Fitness-Biased Selection

- Want the more "fit" to be more likely to reproduce
 - always selecting the best
 - ⇒ premature convergence
 - probabilistic selection ⇒ better exploration
- Roulette-wheel selection: probability ∝ relative fitness:

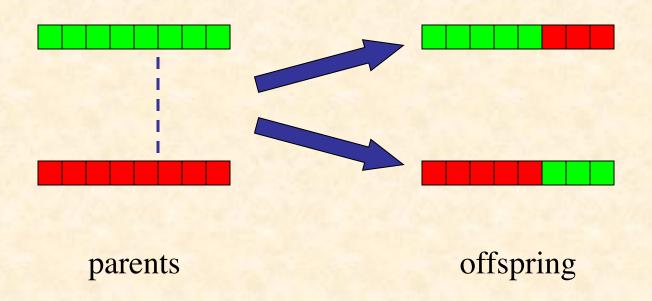
$$\Pr\{i \text{ mates}\} = \frac{f_i}{\sum_{j=1}^n f_j}$$

Crossover: Biological Inspiration

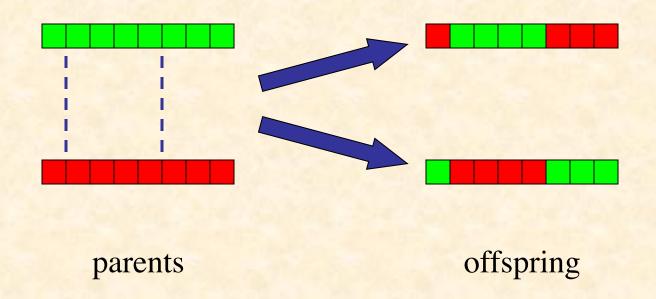
chromatids of homologous chromosomes which will cross over nucleus cytoplasm chiasma

- Occurs during meiosis, when haploid gametes are formed
- Randomly mixes genes from two parents
- Creates genetic variation in gametes

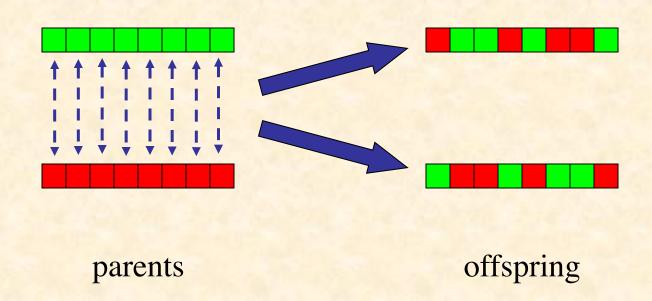
GAs: One-point Crossover



GAs: Two-point Crossover

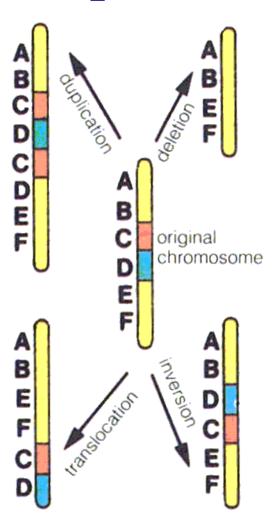


GAs: N-point Crossover

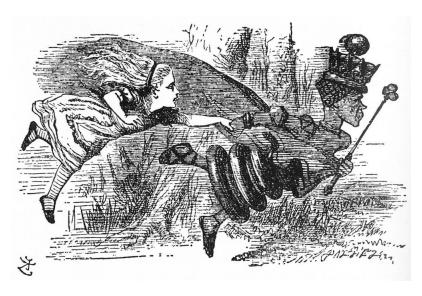


Mutation: Biological Inspiration

- Chromosome mutation ⇒
- Gene mutation: alteration of the DNA in a gene
 - inspiration for mutation in GAs
- In typical GA each bit has a low probability of changing
- Some GAs models rearrange bits



The Red Queen Hypothesis



- "Now, here, you see, it takes all the running you can do, to keep in the same place."
 - Through the Looking-Glass and What Alice Found There

- *Observation*: a species probability of extinction is independent of time it has existed
- *Hypothesis*: species continually adapt to each other
- Extinction occurs with insufficient variability for further adaptation

Demonstration of NetLogo Simple Genetic Algorithm

Run NetLogo Simple Genetic Algorithm

Demonstration of GA: Finding Maximum of Fitness Landscape

Run Genetic Algorithms — An Intuitive

Introduction

by Pascal Glauser

<www.glauserweb.ch/gentore.htm>

Demonstration of GA: Evolving to Generate a Pre-specified Shape (Phenotype)

Run Genetic Algorithm Viewer

<www.rennard.org/alife/english/gavgb.html>

Eaters Seeking Food

- Eaters are FSMs
- Have internal state (memory): 0..15
- Can sense one square ahead
- It can see one of four different things: an Eater, a plant, a blank space, or a wall
- On basis of the above, can change state and:
 - 1. Move forward one square
 - 2. Move backwards one square
 - 3. Turn in place 90 degrees to the left
 - 4. Turn in place 90 degrees to the right
- If lands on a square with food, it eats it
- Genetic strings: $16 \times 4 \times (2 + 4) = 384$ bits

Demonstration of GA: Eaters Seeking Food

http://math.hws.edu/eck/js/genetic-algorithm/GA.html

Morphology Project by Michael "Flux" Chang

- Senior Independent Study project at UCLA
 - users.design.ucla.edu/~mflux/morphology
- Researched and programmed in 10 weeks
- Programmed in Processing language
 - www.processing.org

Genotype ⇒ Phenotype

- Cells are "grown," not specified individually
- Each gene specifies information such as:
 - angle
 - distance
 - type of cell
 - how many times to replicate
 - following gene
- Cells connected by "springs"
- Run phenome:

<users.design.ucla.edu/~mflux/morphology/gallery/sketches/phenome>

Complete Creature

- Neural nets for control (blue)
 - integrate-and-fire neurons
- Muscles (red)
 - Decrease "spring length" when fire
- Sensors (green)
 - fire when exposed to "light"
- Structural elements (grey)
 - anchor other cells together
- Creature embedded in a fluid
- Run <users.design.ucla.edu/~mflux/morphology/gallery/sketches/creature>

Effects of Mutation

- Neural nets for control (blue)
- Muscles (red)
- Sensors (green)
- Structural elements (grey)
- Creature embedded in a fluid
- Run

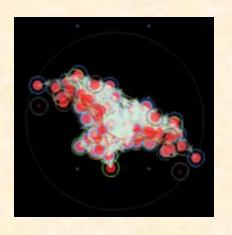
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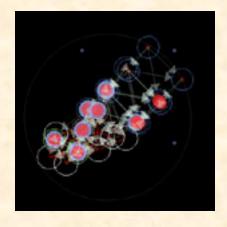
Evolution

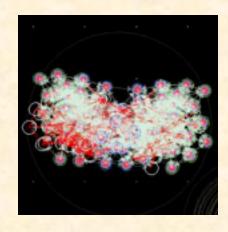
- Population: 150–200
- Nonviable & nonresponsive creatures eliminated
- Fitness based on speed or light-following
- 30% of new pop. are mutated copies of best
- 70% are random
- No crossover



Gallery of Evolved Creatures



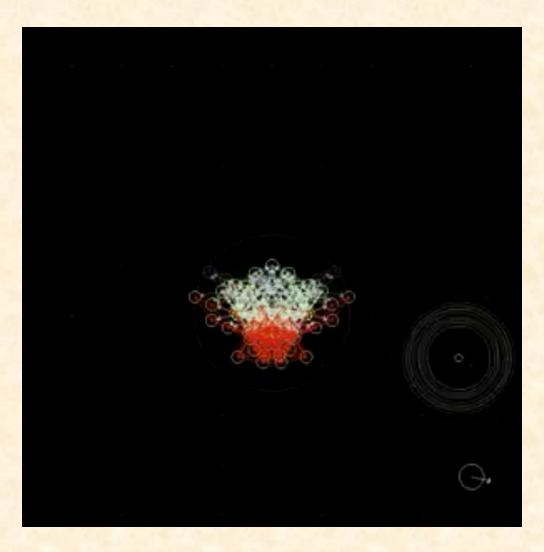




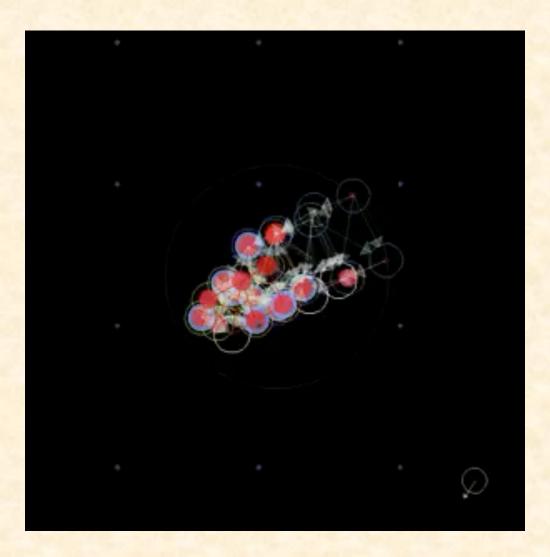
- Selected for speed of movement
- Run

<users.design.ucla.edu/~mflux/morphology/gallery/sketches/creaturegallery>

Example: Circle Swimmer



Example: Slug



Karl Sims' Evolved Creatures

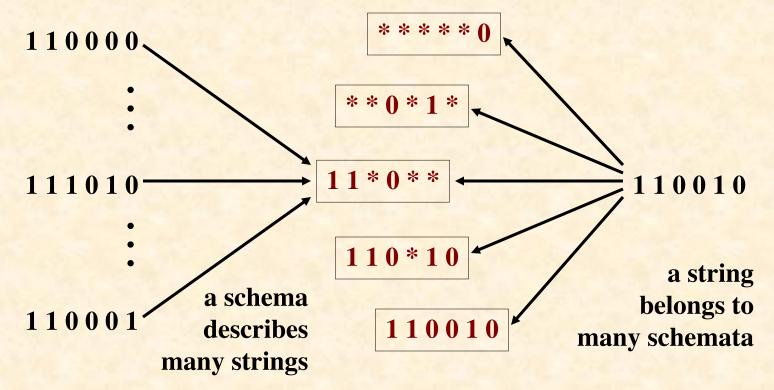


Why Does the GA Work?

The Schema Theorem

Schemata

A schema is a description of certain patterns of bits in a genetic string



The Fitness of Schemata

- The schemata are the building blocks of solutions
- We would like to know the average fitness of all possible strings belonging to a schema
- We cannot, but the strings in a population that belong to a schema give an estimate of the fitness of that schema
- Each string in a population is giving information about all the schemata to which it belongs (implicit parallelism)

Effect of Selection

Let n = size of population

Let m(S,t) = number of instances of schema S at time t

String *i* gets picked with probability $\frac{f_i}{\sum_j f_j}$

Let f(S) = avg fitness of instances of S at time t

So expected
$$m(S,t+1) = m(S,t) \cdot n \cdot \frac{f(S)}{\sum_{j} f_{j}}$$

Since
$$f_{av} = \frac{\sum_{j} f_{j}}{n}$$
, $m(S,t+1) = m(S,t) \frac{f(S)}{f_{av}}$

Exponential Growth

• We have discovered:

$$m(S, t+1) = m(S, t) \cdot f(S) / f_{av}$$

- Suppose $f(S) = f_{av} (1 + c)$
- Then $m(S, t) = m(S, 0) (1 + c)^t$
- That is, exponential growth in aboveaverage schemata

Effect of Crossover

- Let λ = length of genetic strings
- Let $\delta(S)$ = defining length of schema S
- Probability {crossover destroys S}: $p_d \le \delta(S) / (\lambda 1)$
- Let p_c = probability of crossover
- Probability schema survives:

$$p_{\rm s} \ge 1 - p_{\rm c} \frac{\delta(S)}{\lambda - 1}$$

Selection & Crossover Together

$$m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{\text{av}}} \left[1 - p_c \frac{\delta(S)}{\lambda - 1} \right]$$

Effect of Mutation

- Let $p_{\rm m}$ = probability of mutation
- So $1 p_{\rm m}$ = probability an allele survives
- Let o(S) = number of fixed positions in S
- The probability they all survive is $(1 p_{\rm m})^{o(S)}$
- If $p_{\rm m} \ll 1$, $(1 p_{\rm m})^{o(S)} \approx 1 o(S) p_{\rm m}$

Schema Theorem: "Fundamental Theorem of GAs"

$$m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{\text{av}}} \left[1 - p_{\text{c}} \frac{\delta(S)}{\lambda - 1} - o(S) p_{\text{m}} \right]$$

Note:
$$\left(1 - p_{c} \frac{\delta(S)}{\lambda - 1}\right) (1 - o(S)p_{m}) \approx 1 - p_{c} \frac{\delta(S)}{\lambda - 1} - o(S)p_{m}$$

The Bandit Problem

- Two-armed bandit:
 - random payoffs with (unknown) means m_1 , m_2 and variances σ_1^2 , σ_2^2
 - optimal strategy: allocate exponentially greater number of trials to apparently better lever
- k-armed bandit: similar analysis applies
- Analogous to allocation of population to schemata
- Suggests GA may allocate trials optimally

Goldberg's Analysis of Competent & Efficient GAs

Paradox of GAs

- Individually uninteresting operators:
 - selection, recombination, mutation
- Selection + mutation ⇒ continual improvement
- Selection + recombination ⇒ innovation
 - fundamental to invention:generation vs. evaluation
- Fundamental intuition of GAs: the three work well together

blind variation & selective retention

Race Between Selection & Innovation: Takeover Time

- Takeover time t^* = average time for most fit to take over population
- Transaction selection: population replaced by *s* copies of top 1/*s*
- s quantifies selective pressure
- Estimate $t^* \approx \ln n / \ln s$

Innovation Time

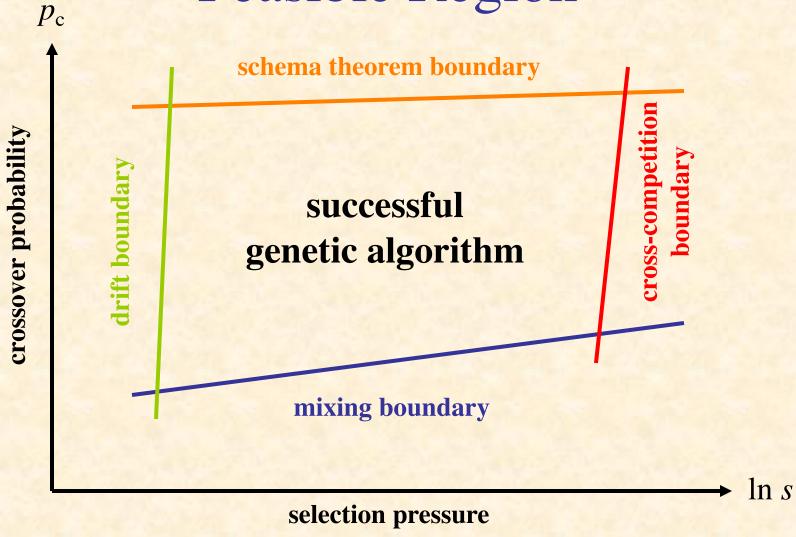
- Innovation time t_i = average time to get a better individual through crossover & mutation
- Let p_i = probability a single crossover produces a better individual
- Number of individuals undergoing $crossover = p_c n$
- Number of probable improvements = $p_i p_c n$
- Estimate: $t_i \approx 1 / (p_c p_i n)$

Steady State Innovation

- Bad: $t^* < t_i$
 - because once you have takeover, crossover does no good
- Good: $t_i < t^*$
 - because each time a better individual is produced, the t* clock resets
 - steady state innovation
- Innovation number:

$$Iv = \frac{t^*}{t_i} = p_c p_i \frac{n \ln n}{\ln s} > 1$$

Feasible Region



Other Algorithms Inspired by Genetics and Evolution

- Evolutionary Programming
 - natural representation, no crossover, time-varying continuous mutation
- Evolutionary Strategies
 - similar, but with a kind of recombination
- Genetic Programming
 - like GA, but program trees instead of strings
- Classifier Systems
 - GA + rules + bids/payments
- and many variants & combinations...

Additional Bibliography

- 1. Goldberg, D.E. The Design of Innovation: Lessons from and for Competent Genetic Algorithms. Kluwer, 2002.
- 2. Milner, R. The Encyclopedia of Evolution. Facts on File, 1990.

