

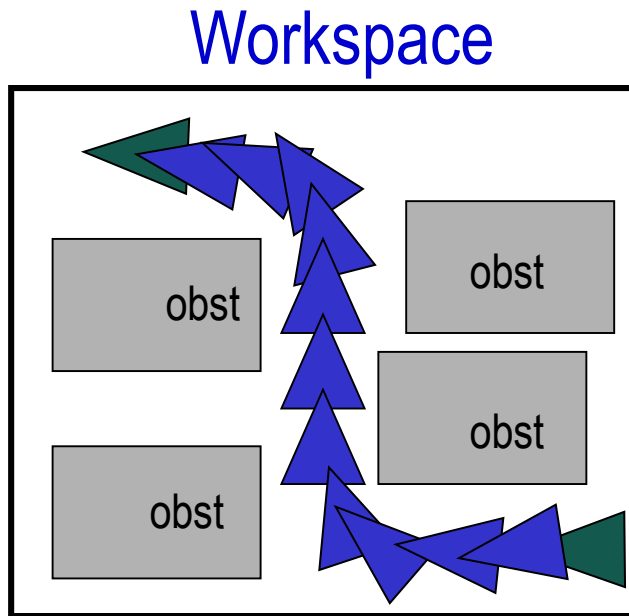
# Randomized Graph Search

October 2, 2014



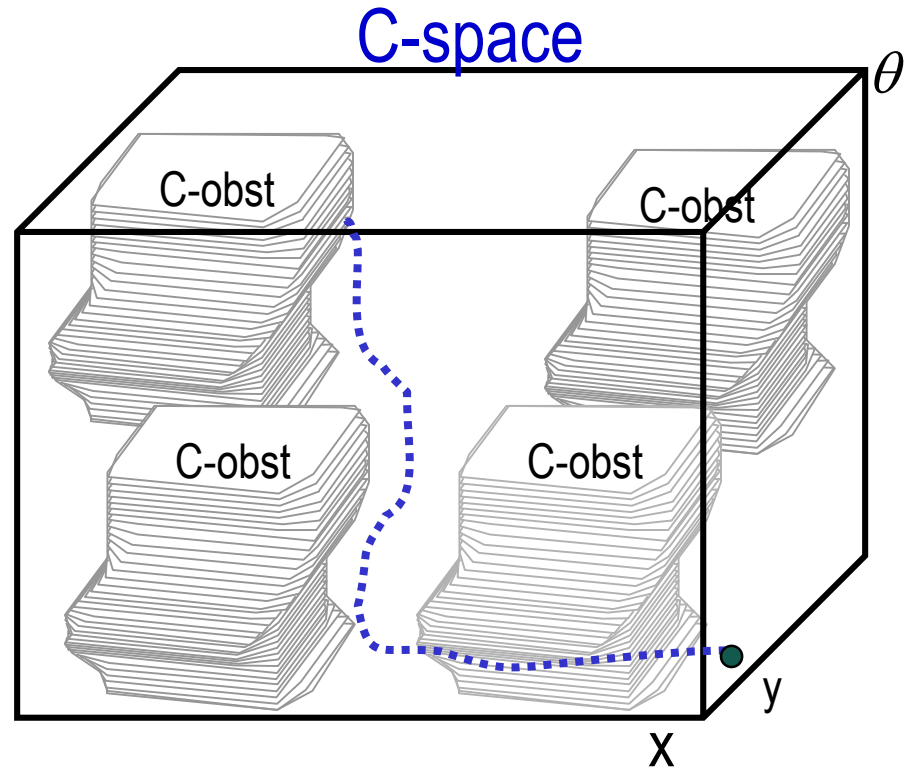
# Motion Planning in C-space

Simple workspace obstacle transformed into complicated C-obstacle!!



 robot

Path is swept volume



 robot

Path is 1D curve


# The Complexity of Motion Planning

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Most motion planning problems of interest are PSPACE-hard

[Reif 79, Hopcroft et al. 84 & 86]

The best deterministic algorithm known has running time that is exponential in the dimension of the robot's C-space [Canny 86]

- C-space has high dimension - 6D for rigid body in 3-space
- Simple obstacles have complex C-obstacles  impractical to compute explicit representation of free space for more than 4 or 5 DOF

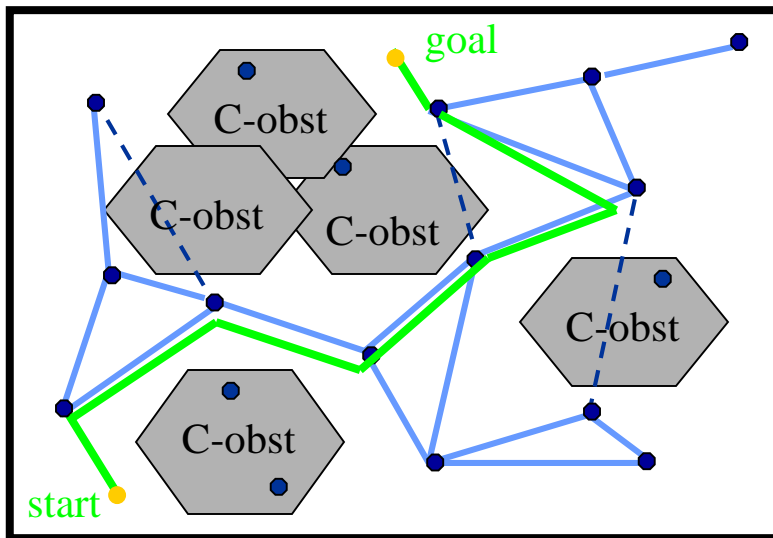
So ... attention has turned to randomized algorithms which:

- trade full completeness of the planner
- for probabilistic completeness and a major gain in efficiency

# Probabilistic Roadmap Methods (PRMs)

[Kavraki, Svestka, Latombe, Overmars 1996]

## C-space



### Roadmap Construction (Pre-processing)

1. Randomly generate robot configurations (nodes)
  - discard nodes that are invalid
2. Connect pairs of nodes to form roadmap
  - simple, deterministic local planner (e.g., straight line)
  - discard paths that are invalid

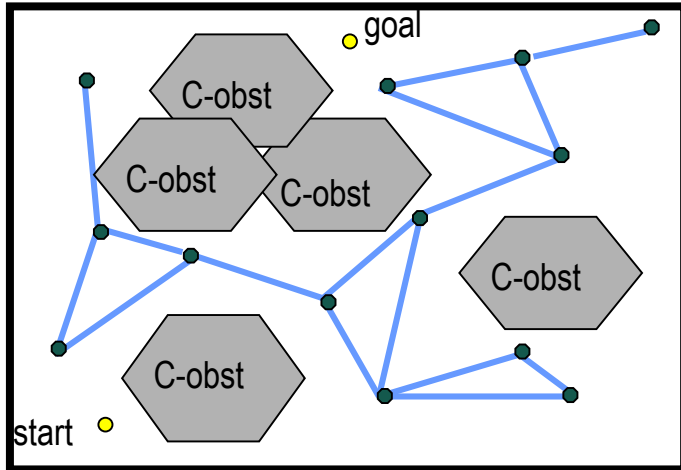
### Query processing

1. Connect start and goal to roadmap
2. Find path in roadmap between start and goal
  - regenerate plans for edges in roadmap

### Primitives Required:

1. Method for Sampling points in C-Space
2. Method for `validating` points in C-Space

# PRMs: Pros & Cons



## PRMs: The Good News

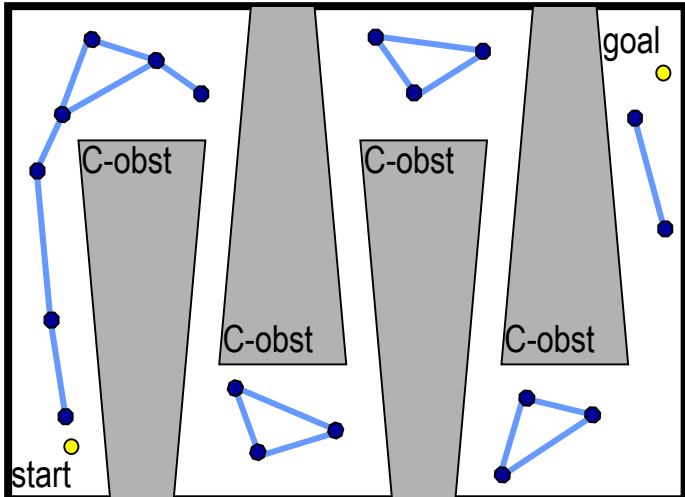
1. PRMs are probabilistically complete
2. PRMs apply easily to high-dimensional C-space
3. PRMs support fast queries w/ enough preprocessing

Many success stories where PRMs solve previously unsolved problems

## PRMs: The Bad News

PRMs don't work as well for some problems:

- unlikely to sample nodes in narrow passages
- hard to sample/connect nodes on constraint surfaces



# Rapidly Exploring Random Trees (RRTs)

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- Promoted by Steve Lavelle and James Kuffner
- Alternative to other randomized approaches
  - Probabilistic roadmap planner
- RRT (rapidly exploring random trees) use Configuration Space
  - $C$  : configuration space where  $q$  belongs to  $C$  and describes the position and orientation of a body place in the space.
  - $C_{free}$  : set of configuration where the body does not collide with obstacles

# The RRT Algorithm

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BUILD\_RRT( $q_{init}$ )

```
1  $\mathcal{T}.\text{init}(q_{init});$ 
2 for  $k = 1$  to  $K$  do
3    $q_{rand} \leftarrow \text{RANDOM\_CONFIG}();$ 
4    $\text{EXTEND}(\mathcal{T}, q_{rand});$ 
5 Return  $\mathcal{T}$ 
```

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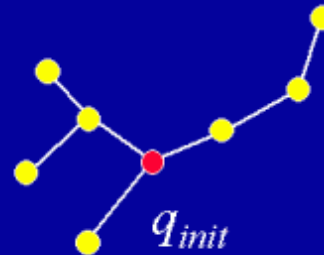
EXTEND( $\mathcal{T}, q$ )

```
1  $q_{near} \leftarrow \text{NEAREST\_NEIGHBOR}(q, \mathcal{T});$ 
2 if  $\text{NEW\_CONFIG}(q, q_{near}, q_{new})$  then
3    $\mathcal{T}.\text{add\_vertex}(q_{new});$ 
4    $\mathcal{T}.\text{add\_edge}(q_{near}, q_{new});$ 
5   if  $q_{new} = q$  then
6     Return Reached;
7   else
8     Return Advanced;
9 Return Trapped;
```

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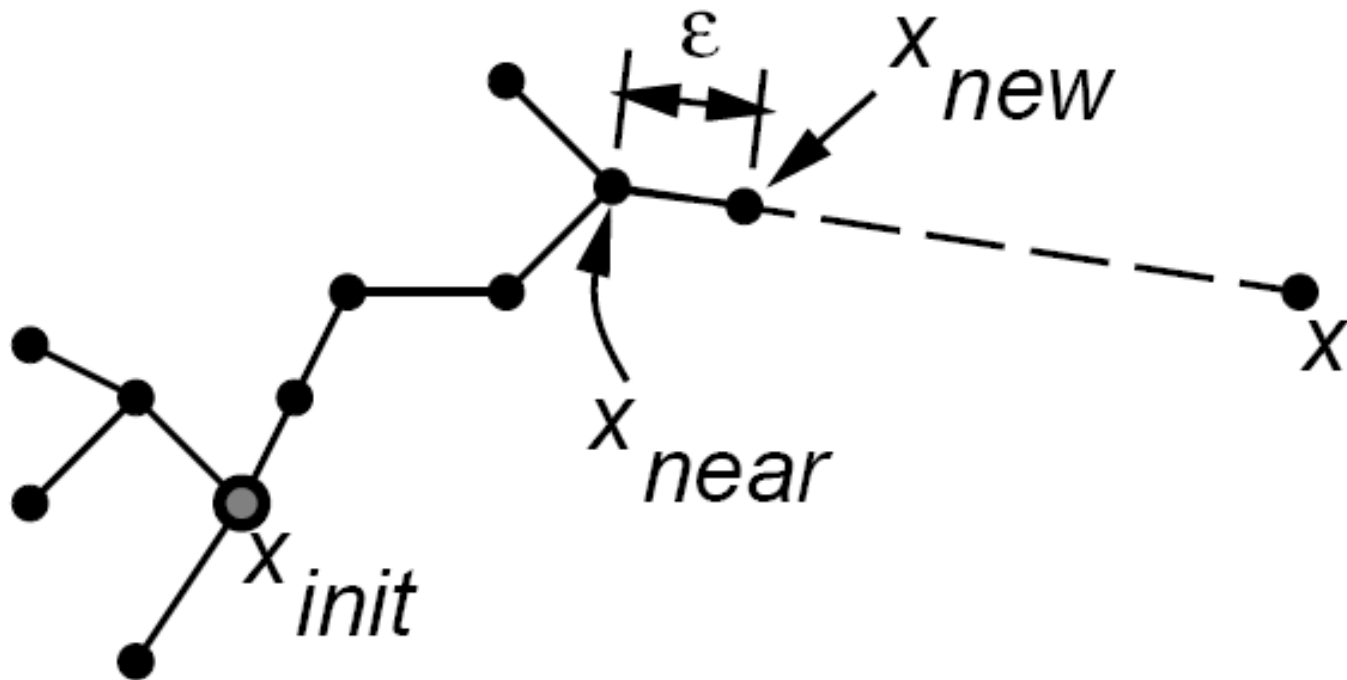
- Start with initial (random) tree
- Select random configuration in free space
- The tree node closest to the selected random configuration is found
- An edge is “grown” toward the new configuration, taking into account the robot kinematic motion model

Existing RRT is “grown” as follows...



# Basic Extend

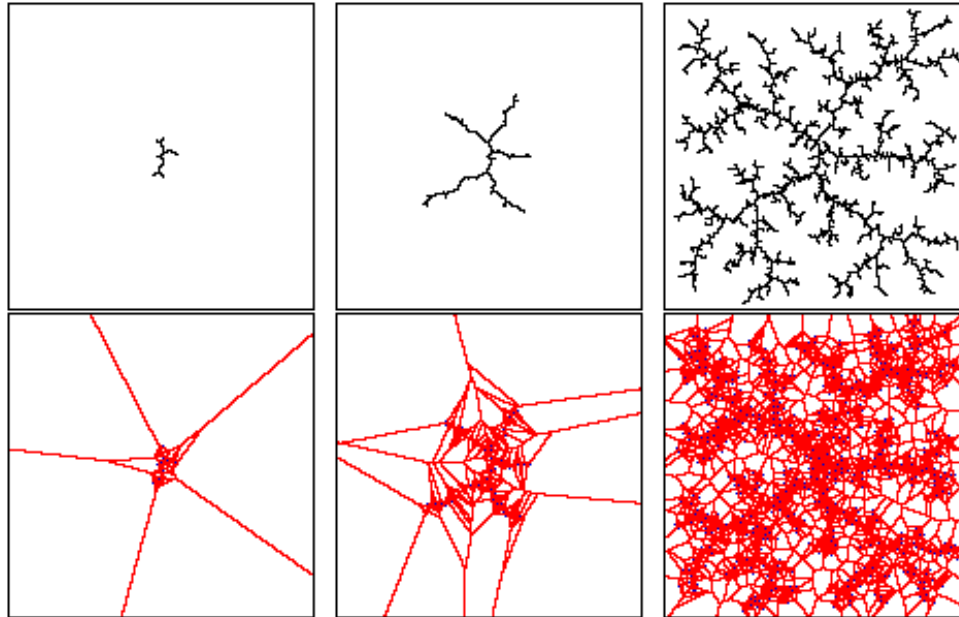
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# Where is the “Rapid” in RRTs?

- Why are RRT's rapidly exploring?
  - the probability of a node being selected for expansion is proportional to the area of its Voronoi region



- If just choose a vertex at random and extend, then it would act like random walk instead
  - Biased towards start vertex

# Variation: RRT-Connect

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- RRT-connect is a variation of RRT
  - grows two trees from both the source and destination until they meet
  - grows the trees towards each other (rather than towards random configurations)
  - the greediness becomes stronger by growing the tree with multiple epsilon steps instead of a single one

# RRT-Connect Algorithm

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CONNECT( $\mathcal{T}, q$ )

```
1 repeat
2    $S \leftarrow$  EXTEND( $\mathcal{T}, q$ );
3 until not ( $S = Advanced$ )
4 Return  $S$ ;
```

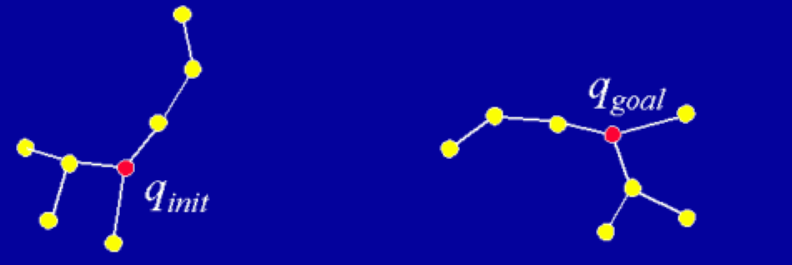
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RRT\_CONNECT\_PLANNER( $q_{init}, q_{goal}$ )

```
1  $\mathcal{T}_a.init(q_{init}); \mathcal{T}_b.init(q_{goal});$ 
2 for  $k = 1$  to  $K$  do
3    $q_{rand} \leftarrow$  RANDOM_CONFIG();
4   if not (EXTEND( $\mathcal{T}_a, q_{rand}$ ) = Trapped) then
5     if (CONNECT( $\mathcal{T}_b, q_{new}$ ) = Reached) then
6       Return PATH( $\mathcal{T}_a, \mathcal{T}_b$ );
7   SWAP( $\mathcal{T}_a, \mathcal{T}_b$ );
8 Return Failure
```

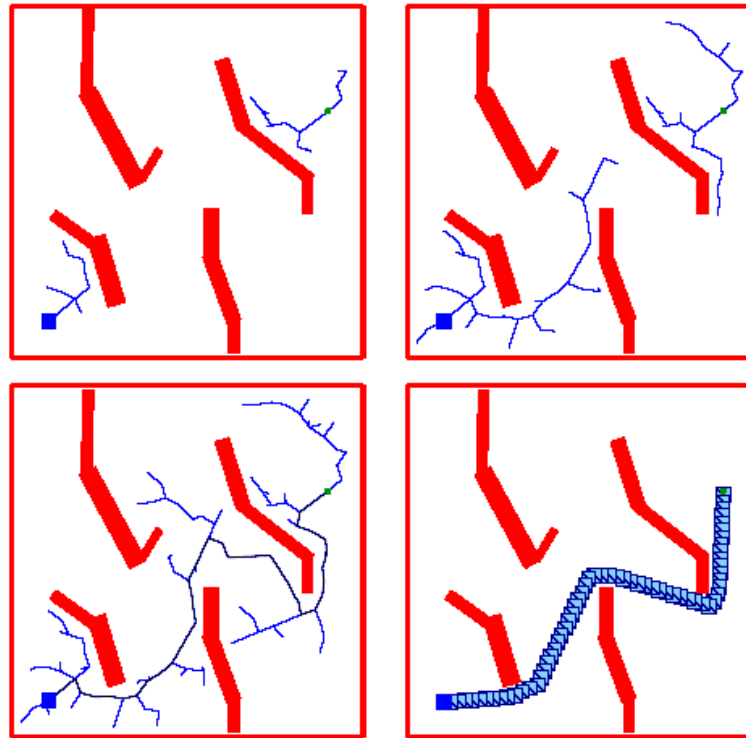
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A single RRT-Connect iteration...



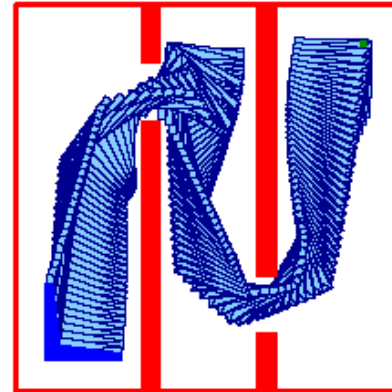
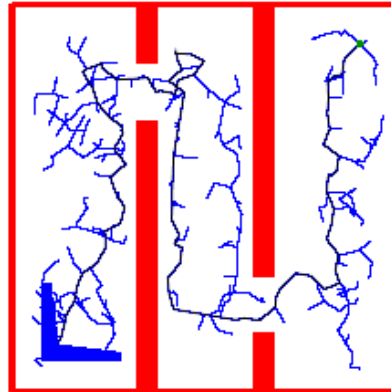
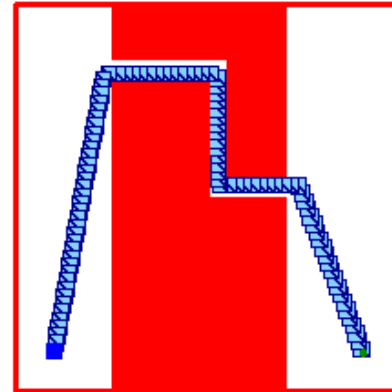
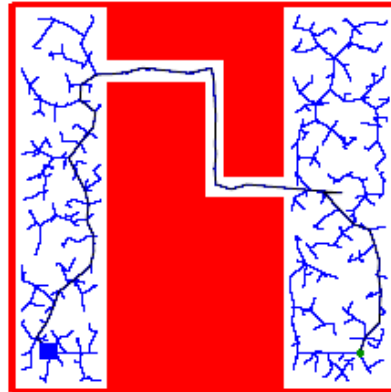
# Examples

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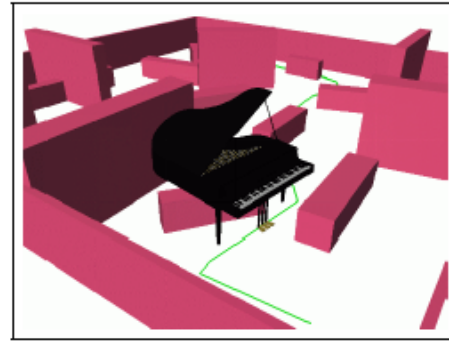
# Examples

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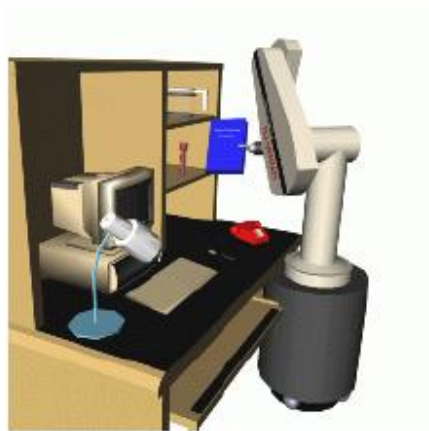
# Examples

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# Examples

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# RRT-Connect Performance

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- Much faster than common RRT methods for uncluttered environments and slightly faster in very cluttered environments
- 2D cases are solved in  $\leq 1$  second depending on the complexity of the situation
- 3D piano scene required 12 seconds
- 6 DOF robot arm required 4 seconds



# RRT-Connect: Pros and Cons

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- Improved version of RRT for faster convergence
- Finds paths in high dimensional spaces at interactive time rates
- Experiments showed it to be consistent
- Drawback: a lot of nearest neighbor searches are performed

# Extension to Non-holonomic

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- The new\_state computation handles all the complicated part
- Given a state  $x$  and inputs  $u$

$$\dot{x} = f(x, u)$$

- Integrate numerically to get new position

# Examples

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- <http://msl.cs.uiuc.edu/rrt/gallery.html>