Multilevel Inverters for Large Automotive Electric Drives

L. M. Tolbert, F. Z. Peng, D. J. Adams, J. W. McKeever
Oak Ridge National Laboratory
P.O. Box 2009, Bldg 9102-1, MS 8038
Oak Ridge, TN 37831-8038
Phone: (865) 576-6206, Fax: (865) 241-6124
e-mail: tolbertlm@ornl.gov

Abstract—Traditional high-frequency pulse width modulation (PWM) inverters for motor drives have several problems associated with their high frequency switching which produces high voltage change (dV/dt) rates. Multilevel inverters solve these problems because their devices switch at the fundamental frequency. Two different multilevel topologies are identified for use as a converter for electric drives, a cascade inverter with separate dc sources and a back-to-back diode clamped converter. The cascade inverter is a natural fit for large automotive electric drives because of the high VA ratings possible and because it uses several levels of dc voltage sources which would be available from batteries or fuel cells. The back-to-back diode clamped converter is ideal for use where a generator or alternator produces ac voltage. Simulation and experimental results show the superiority of these two converters over PWM based drives.

I. INTRODUCTION

A. Background

Large electric vehicles will require advanced power electronic inverters to meet the high power demands (>1 MW) required of them. One inverter type which is uniquely suited for this application is the multilevel inverter [1]. Two different multilevel converter topologies are ideal for use as electric drives. The cascaded inverter with separate dc sources closely fits the needs of electric vehicles because it can use the onboard batteries or fuel cells to synthesize a sinusoidal voltage waveform to drive the main vehicle traction motor. Where generated ac voltage is available, a back-to-back diode clamped converter can be used to output variable frequency ac voltage for the main traction motor.

Multilevel inverters also solve problems with present high-frequency PWM adjustable speed drives (ASD’s). Adjustable speed drives usually employ a front-end rectifier to convert utility ac voltage to dc voltage and an inverter to convert the dc voltage to variable frequency and variable voltage for motor control. Motor damage and failure has been reported by industry as a result of adjustable speed drive inverters’ high frequency PWM switching. The main problems reported have been “motor bearing failure” and “motor winding insulation breakdown” because of internally induced circulating currents [2-4]. The cause of these currents are related to the capacitive elements between the winding conductor and motor shaft and also the insulation between different winding layers being subject to high voltage transients.

Only recently have circulating currents become a problem with adjustable speed drives because the power semiconductor switches are now able to switch fast enough such that the voltage change rate (dV/dt) is high enough to induce the damaging circulating currents and corona discharge between the winding layers. Present power semiconductors can be turned on and off within one microsecond for 600 V and higher voltages. Although the fast switching can somewhat reduce the switching losses and the switching frequency is well above the acoustic noise level, the dV/dt associated capacitive coupling currents in the motor are also greatly increased. Because these currents are normally non-measurable, the cause of the associated motor failures were unknown until recent papers reported this phenomena [2-4].

Another drawback of conventional adjustable speed drives is efficiency. Because the inverter must switch at supersonic frequency, the associated switching losses (turn-on and turn-off losses) are normally much higher than the device conduction loss, which results in low efficiency power conversion from dc to ac [5].

In summary, the problems associated with conventional adjustable speed drive inverters are as follows:

1. High-frequency switching requires significant derating of switching devices and generates large switching losses.
2. High dV/dt because of switching causes motor bearing failure and stator winding insulation breakdown.
3. High-frequency switching generates broadband (10 kHz to 30 Mhz) electromagnetic interference (EMI) to nearby communication or other electronic equipment.

B. Multilevel Converters

The multilevel voltage source inverters’ unique structure allows them to reach high voltages with low harmonics without the use of transformers. The general structure of the multilevel inverter is to synthesize a sinusoidal voltage from several levels of dc voltages. For this reason, multilevel inverters are a natural fit for high power applications required of a large electric vehicle drive.

As the number of levels increases, the synthesized output
The waveform has more steps, which produces a staircase wave that approaches a sinusoidal waveform. Also, as more steps are added to the waveform, the harmonic distortion of the output wave decreases until it reaches zero with an infinite number of levels. As the number of levels increases, the higher the voltage which can be spanned by connecting devices in series. The structure of the multilevel inverter is such that no voltage sharing problems are encountered by the series-connected devices.

Three types of multilevel inverters have been proposed by researchers thus far: the diode-clamped inverter, the flying-capacitor inverter, and the cascade inverter. Proposed uses for these converters have included static var compensation [5-10], back-to-back high voltage intertie [11], and as an adjustable speed drive [11-16].

Using multilevel inverters as drives for electric motors is a much different application than for static var compensation. Only reactive power flows between the converter and the system in static var compensation, whereas the converters must handle bidirectional real power flow in the case of motor drives. One of the keys to using multilevel converters is balancing the voltage across the series connected dc bus capacitors. Capacitors will tend to overcharge or completely discharge and the multilevel converter will revert to a 3-level converter unless an explicit control is realized to accomplish capacitor charge balancing.

Three, four, and five level rectifier-inverter drive systems have been investigated in the literature [12-16] which have used some form of multilevel PWM as a means to control the switching of the rectifier and inverter sections. Multilevel PWM reduces the high dV/dt experienced in traditional high frequency PWM drives because switching is between several smaller voltage levels. However, switching losses are still relatively high for these proposed schemes and the voltage THD at the output of the inverter section was reported to be 19.7% for a four-level scheme [15].

This paper will propose two multilevel inverter control schemes where devices are switched only at the fundamental frequency and the inverter output line voltage THD is less than 5 percent. In addition, a control scheme will be demonstrated in the multilevel diode clamped converter that obtains well balanced voltages across the dc link capacitors.

III. CASCADED INVERTERS WITH SEPARATE DC SOURCES

A. General Structure

One converter structure proposed for use as an automotive electric drive is a multilevel inverter which uses cascaded inverters with separate dc sources (SDC’s). The general structure of this multilevel inverter is to synthesize a sinusoidal voltage from several levels of dc voltages, which may be obtained from either batteries, fuel cells, solar cells, or capacitors charged from a rectified ac voltage source. Fig. 1 shows a single-phase structure of the cascade inverter with SDC’s [6]. Each SDC is connected to a single-phase full-bridge inverter. Each inverter level can generate three different voltage outputs, +Vdc, 0, and -Vdc by connecting the dc source to the ac output side by different combinations of the four switches, S1, S2, S3, and S4. To obtain +Vdc, switches S1 and S4 are turned on. Turning on switches S2 and S3 yields -Vdc. By turning on S1 and S2 or S3 and S4, the output voltage is 0.

![Fig. 1. Single phase structure of a multilevel cascaded inverter.](image1)

The ac output of each of the different level full-bridge inverters are connected in series such that the synthesized voltage waveform is the sum of the inverter outputs. The level in a cascade-inverter is defined by m = 2s + 1, where m is the output phase voltage level and s is the number of dc sources. An example phase voltage waveform for an 11-level cascaded inverter with five SDC’s and five full bridges is shown in Fig. 2. The phase voltage \( V_{off} = V_1 + V_2 + V_3 + V_4 + V_5 \).

![Fig. 2. Output voltage waveform of an 11-level cascade inverter.](image2)
For a stepped waveform such as the one depicted in Fig. 2 with \( s \) steps, the Fourier Transform for this waveform is as follows:

\[
V(\omega t) = \frac{4V_{dc}}{\pi} \sum_{n=0}^{\infty} \left[ \cos(n\theta_1) + \cos(n\theta_2) + \ldots + \cos(n\theta_s) \right] \sin(n\omega t) = \frac{4V_{dc}}{\pi} \sum_{n=1}^{\infty} \left[ \cos(n\theta_1) + \cos(n\theta_2) + \ldots + \cos(n\theta_s) \right] \sin(n\omega t)
\]

where \( n = 1, 3, 5, 7, \ldots \) (1)

From (1), the magnitude of the Fourier coefficients when normalized with respect to \( V_{dc} \) are as follows:

\[
H(n) = \frac{4}{\pi n} \left[ \cos(n\theta_1) + \cos(n\theta_2) + \ldots + \cos(n\theta_s) \right] \sin(n\omega t) = \frac{4}{\pi n} \left[ \cos(n\theta_1) + \cos(n\theta_2) + \ldots + \cos(n\theta_s) \right] \sin(n\omega t)
\]

where \( n = 1, 3, 5, 7, \ldots \) (2)

The conducting angles, \( \theta_1, \theta_2, \ldots, \theta_s \), can be chosen such that the voltage total harmonic distortion is a minimum. Normally, these angles are chosen so as to cancel the predominant lower frequency harmonics [10]. For the 11-level case in Fig. 2, the 5th, 7th, 11th, and 13th harmonics can be eliminated with the appropriate choice of the conducting angles. One degree of freedom is used so that the magnitude of the output waveform corresponds to the reference modulation index, \( M_i \), which is defined as \( V_L/V_{L_{max}} \), where \( V_{L} \) is the amplitude command of the inverter output phase voltage, and \( V_{L_{max}} \) is the maximum attainable amplitude of the converter, i.e. the amplitude of the phase voltage when all the switching angles \( \theta_i \) are equal to zero[11].

Let the equations from formula (2) be as follows:

\[
\cos(5\theta_1) + \cos(5\theta_2) + \cos(5\theta_3) + \cos(5\theta_4) + \cos(5\theta_5) = 0
\]

\[
\cos(7\theta_1) + \cos(7\theta_2) + \cos(7\theta_3) + \cos(7\theta_4) + \cos(7\theta_5) = 0
\]

\[
\cos(11\theta_1) + \cos(11\theta_2) + \cos(11\theta_3) + \cos(11\theta_4) + \cos(11\theta_5) = 0
\]

\[
\cos(13\theta_1) + \cos(13\theta_2) + \cos(13\theta_3) + \cos(13\theta_4) + \cos(13\theta_5) = 0
\]

\[
\cos(\theta_1) + \cos(\theta_2) + \cos(\theta_3) + \cos(\theta_4) + \cos(\theta_5) = 5M_i
\]

The set of equations (3) are nonlinear transcendental equations which can be solved by an iterative method such as the Newton-Raphson method. Using a modulation index of 0.8 obtains:

\( \theta_1 = 6.57^\circ, \theta_2 = 18.94^\circ, \theta_3 = 27.18^\circ, \theta_4 = 45.14^\circ, \theta_5 = 62.24^\circ \).

This means that if the inverter output is symmetrically switched during the positive half cycle of the fundamental voltage to \( +V_{dc} \) at 6.57°, \( +2V_{dc} \) at 18.94°, \( +3V_{dc} \) at 27.18°, \( +4V_{dc} \) at 45.14°, and \( +5V_{dc} \) at 62.24°, and similarly in the negative half cycle to \( -V_{dc} \) at 186.57°, \( -2V_{dc} \) at 198.94°, \( -3V_{dc} \) at 207.18°, \( -4V_{dc} \) at 225.14°, \( -5V_{dc} \) at 242.24°, the output voltage of the 11-level inverter will not contain the 5th, 7th, 11th, and 13th harmonic components.

### B. Three Phase Motor Drive

For a three-phase system, the output voltages of three single phase cascaded inverters can be connected in either a wye or delta configuration. Fig. 3 illustrates the connection diagram for a wye-configured 11-level converter using cascaded-inverters with five SDC voltage sources per phase. In the motoring mode, power flows from the batteries through the cascade inverters to the motor. In the charging mode, the cascade converters act as rectifiers, and power flows from the charger to the batteries.

From Fig. 2, note that the duty cycle for each of the voltage levels is different. If this same pattern of duty cycles is used on a motor drive continuously, then the level 1 battery is cycled on for a much longer duration than the level 5 battery. This means that the level 1 battery will discharge much sooner than the level 5 battery. However, by rotating the duty cycles among the various levels as shown in Fig. 4, the batteries will be discharged or charged evenly, and they all should reach the end of their lifetime near the same time.

In Fig. 4, the fundamental active component of the load current, \( I_{La,n} \), is shown to be in phase with the output load voltage, \( V_{La,n} \). This is the portion of the current that is responsible for charge or discharge of the batteries and contributes to real power flow. The nonactive portion of the current is orthogonal to the output load voltage and does not contribute to charging or discharging of the batteries.

Fig. 5 shows the system configuration and control block diagram of a vehicle drive using an 11-level cascade inverter. The duty cycle look up table contains switching timings to generate the desired output voltage as shown in Fig. 4. The switching angles, \( \theta_i, (s = 1, 2, 3, 4, 5) \), are calculated off-line to minimize harmonics for each modulation index, \( M_i \).

An 11-level prototype cascade inverter has been built and used for static var compensation with great success [6-7]. The control scheme for this application is much more complicated than using the inverter as an electric drive because of synchronization with the utility and measurement of power phase angles and voltages. In the near future, this same 11-level prototype will be connected to a battery bank and used to drive an induction motor.
III. BACK-TO-BACK DIODE CLAMPED CONVERTER DRIVE

Two 6-level diode clamped inverters connected back-to-back are shown in Fig. 6. The dc bus for these two inverters consists of five capacitors, and the voltage across each capacitor is $V_{dc}$. The voltage stress across each switching device is limited to $V_{dc}$ through the clamping diodes.

Table I lists the voltage output levels possible for one phase of the inverter using the negative dc rail 0 as a reference point. State condition 1 means the switch is on, and 0 means the switch is off. Note that each active device is only switched once per cycle. Each phase has five complementary switch pairs such that turning on one of the switches of the pair requires that the other switch be turned off. The complementary switch pairs for phase leg $a$ are $(S_{a1}, S_{a'1}), (S_{a2}, S_{a'2}), (S_{a3}, S_{a'3}), (S_{a4}, S_{a'4}),$ and $(S_{a5}, S_{a'5})$.

Fig. 7 shows phase and line voltage waveforms for one phase of a 6-level inverter. The line voltage $V_{ab}$ consists of a positive phase-leg $a$ voltage and a negative phase-leg $b$ voltage. The resulting line voltage is an 11-level staircase waveform. This means that an $m$-level diode clamped inverter has an $m$-level output phase voltage and a $(2m-1)$-level output line voltage.

Although each active switching device is only required to block a voltage level of $V_{dc}$, the clamping diodes require different voltage ratings for reverse voltage blocking. Using phase $a$ of Fig. 6 as an example, when all the lower switches $S_{a'1}$ through $S_{a'5}$ are turned on, $D_4$ must block four capacitor voltages, or $4V_{dc}$. Similarly, $D_1$ must block $3V_{dc}$, $D_2$ must block $2V_{dc}$, and $D_5$ must block $V_{dc}$. If the inverter is designed such that each blocking diode has the same voltage rating as the active switches, the number of diodes required for each phase is $(m-1)\times(m-2)$. Thus, the number of blocking diodes are quadratically related to the number of levels in a diode clamped converter [11].

<table>
<thead>
<tr>
<th>TABLE I</th>
<th>Diode-clamp 6-level converter voltage levels and corresponding switch states</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output</td>
<td>Switch State</td>
</tr>
<tr>
<td>$V_{la}$</td>
<td>$S_{a1}$ $S_{a2}$ $S_{a3}$ $S_{a4}$ $S_{a5}$ $S_{a'1}$ $S_{a'2}$ $S_{a'3}$ $S_{a'4}$ $S_{a'5}$</td>
</tr>
<tr>
<td>$V_6 = 5V_{dc}$</td>
<td>1 1 1 1 1 0 0 0 0 0</td>
</tr>
<tr>
<td>$V_5 = 4V_{dc}$</td>
<td>0 1 1 1 1 1 0 0 0 0</td>
</tr>
<tr>
<td>$V_4 = 3V_{dc}$</td>
<td>0 0 1 1 1 1 1 0 0 0</td>
</tr>
<tr>
<td>$V_3 = 2V_{dc}$</td>
<td>0 0 0 1 1 1 1 1 0 0</td>
</tr>
<tr>
<td>$V_2 = V_{dc}$</td>
<td>0 0 0 0 1 1 1 1 1 0</td>
</tr>
<tr>
<td>$V_1 = 0$</td>
<td>0 0 0 0 0 1 1 1 1 1</td>
</tr>
</tbody>
</table>
A 6-level back-to-back converter prototype has been built and used to drive a 1.5 hp induction motor. Fig. 8 shows the source voltage, \( V_{Sab} \), and the source current, \( I_{Sa} \), drawn by the converter. Fig. 9 shows the inverter output line voltage, \( V_{Lab} \), and the load current, \( I_{La} \), drawn by the motor. This prototype diode clamped rectifier drew a source current that had a THD of 0.95 percent and had an input power factor of 1.0. The output voltage at the motor terminals had a THD of 5 percent and the converter output current had a THD of 1 percent. Additionally, the experiment shows that the output line voltage \( \frac{dV}{dt} \) is reduced by 11 times with the 6-level converter as compared to a high-frequency PWM drive. The dramatic one order of magnitude reduction in \( \frac{dV}{dt} \) can prevent motor windings and bearings from failure.

One of the keys to using multilevel converters is balancing the voltage across the series connected dc bus capacitors. Capacitors will tend to overcharge or completely discharge and the multilevel converter will revert to a 3-level converter unless an explicit control is realized to accomplish capacitor charge balancing. The method used to accomplish voltage balancing in this back-to-back configuration was to use identical

---

**Fig. 6.** 6-level diode clamped back-to-back converter structure for motor drive.

**Fig. 7.** Phase and line voltage waveforms for six-level diode clamped inverter.

**Fig. 8.** Source and converter voltage and source current waveforms for a six level diode clamped drive prototype.

**Fig. 9.** Inverter output voltage and load current for six level diode clamped drive prototype.
the following advantages over the traditional PWM inverter: high efficiency and power factor. Frequency, these converters have low output voltage THD and control strategy that operates the switches at fundamental frequency.

Simulation and experimental results have shown that with a variable frequency ac voltage for the main traction motor. A back-to-back diode clamped converter can be used to convert generated ac voltage to vehicle traction motor. A back-to-back diode clamped converter can be used to convert generated ac voltage to vehicle traction motor. A back-to-back diode clamped converter can be used to convert generated ac voltage to vehicle traction motor. A back-to-back diode clamped converter can be used to convert generated ac voltage to vehicle traction motor.

switching patterns for the rectifier and the inverter portions of the converter. Thus, the real power flow into a capacitor was the same as the real power flow out of the capacitor, and the net charge on the capacitor over one cycle remained the same. The dc voltage levels across the capacitors remained balanced as shown in Fig. 10 for the 6-level diode clamped converter prototype.

If for some reason the dc capacitors start to have an unbalance in their voltage levels, a modification to the previously described control scheme can be implemented. By monitoring the voltages of each of the dc link levels, minor adjustments can be made to the either the inverter switching angles or the rectifier switching angles which will transfer a net charge either into or out of a particular voltage level to raise or lower the voltage level as required.

**IV. CONCLUSIONS**

Two different multilevel inverters have been proposed for use in large automotive electric drives. The cascaded inverter with separate dc sources closely fits the needs of electric vehicles because it can use the onboard batteries or fuel cells to synthesize a sinusoidal voltage waveform to drive the main vehicle traction motor. A back-to-back diode clamped converter can be used to convert generated ac voltage to variable frequency ac voltage for the main traction motor. Simulation and experimental results have shown that with a control strategy that operates the switches at fundamental frequency, these converters have low output voltage THD and high efficiency and power factor.

In addition, multilevel converters have been shown to have the following advantages over the traditional PWM inverter:

1. They are more suitable for large VA rated motor drives.
2. Their efficiency is much higher because of the minimum switching frequency.
3. Power factor is close to unity for multilevel inverters used as rectifier to convert generated ac to dc.
4. No voltage sharing problems exist for series connected devices unlike traditional inverters.
5. Switching stress and EMI are low.

**REFERENCES**


