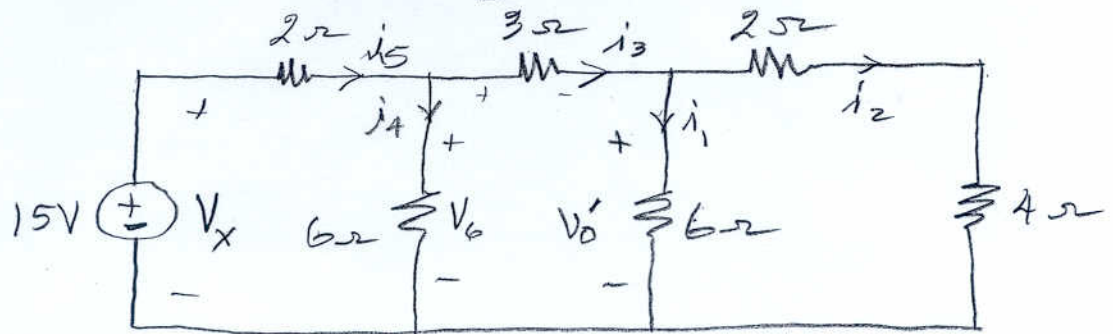


HW# 3 Spring 2007

4.5 For the circuit below assume $V_0 = 1$ and use linearity to find the true V_0



With $V_0 = 1$ volt

$$i_1 = \frac{1}{6}; \quad i_2 = \frac{1}{6}$$

$$i_3 = i_1 + i_2 = \frac{1}{3}$$

$$V_6 = i_3 \times 3 + i_1 \times 6 = \frac{1}{3} \times 3 + \frac{1}{6} \times 6 = 2V$$

$$i_4 = \frac{V_6}{6} = \frac{2}{6} = \frac{1}{3}$$

$$i_5 = i_4 + i_3 = \frac{1}{3} + \frac{1}{3} = \frac{2}{3}$$

$$\begin{aligned} V_x &= 2i_5 + 6i_4 = 2 \times \frac{2}{3} + 6 \times \frac{1}{3} \\ &= \frac{4}{3} + \frac{6}{3} = \frac{10}{3} \end{aligned}$$

Then

$$\frac{V_x}{15} = \frac{V_0'}{V_0} \quad \Rightarrow \quad \frac{\frac{10}{3}}{15} = \frac{1}{V_0}$$

$$V_0 = \frac{15 \times 3}{10} = 4.5V$$

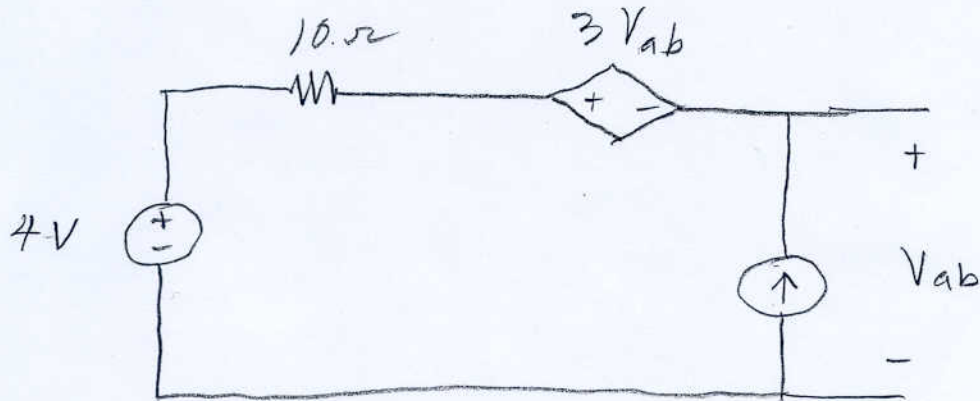
(compare to nodal analysis)

4.10

Find the terminal voltage V_{ab} by

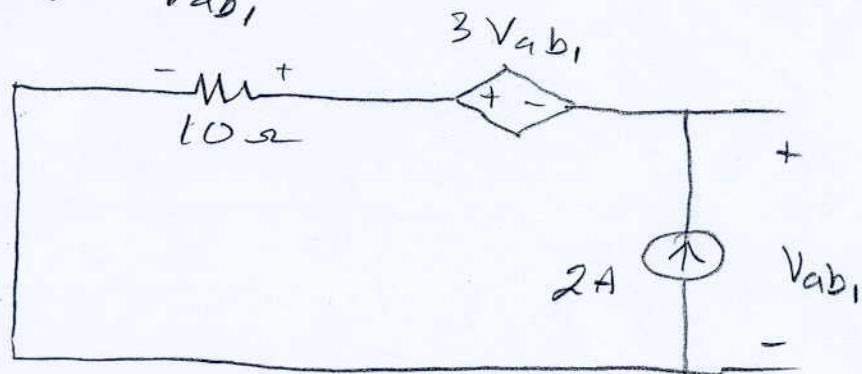
(a) superposition

(b) nodal analysis



(a) superposition

de-energize the 4 volt source and find V_{ab_1}



$$-10 \times 2 + 3V_{ab_1} + V_{ab_1} = 0$$

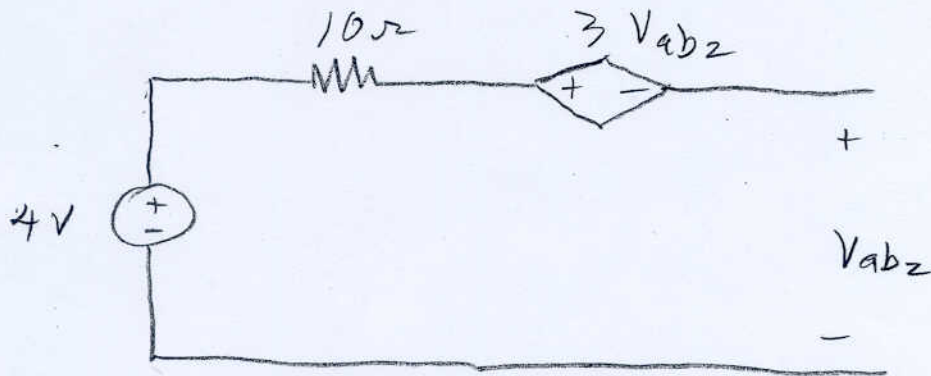
$$4V_{ab_1} = 20$$

$$V_{ab_1} = 5V$$

4.10 continued

2

Now de-energize the current source and find V_{ab2}



NO current so the voltage drop across the 10Ω resistor is zero.

$$-4 + 3V_{ab2} + V_{ab2} = 0$$

$$4V_{ab2} = 4$$

$$V_{ab2} = 1V$$

Thus, by superposition

$$V_{ab} = V_{ab1} + V_{ab2} = 5 + 1$$

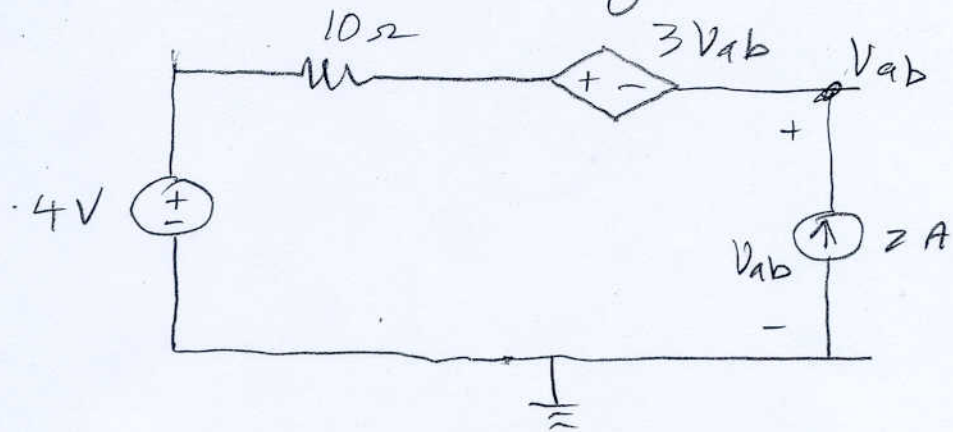
$$V_{ab} = 6V$$

Part (b), next page:

4.10 continued

3

(b) Find V_{ab} by nodal analysis



At node V_{ab} :

$$\frac{V_{ab} + 3V_{ab} - 4}{10} - 2 = 0$$

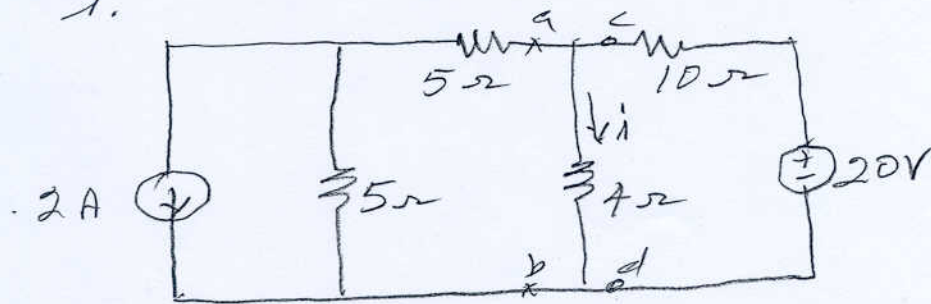
$$V_{ab} + 3V_{ab} - 4 - 20 = 0$$

$$4V_{ab} = 24$$

$$\boxed{V_{ab} = 6V} \quad QED$$

4.22

Use source transformation to find i .

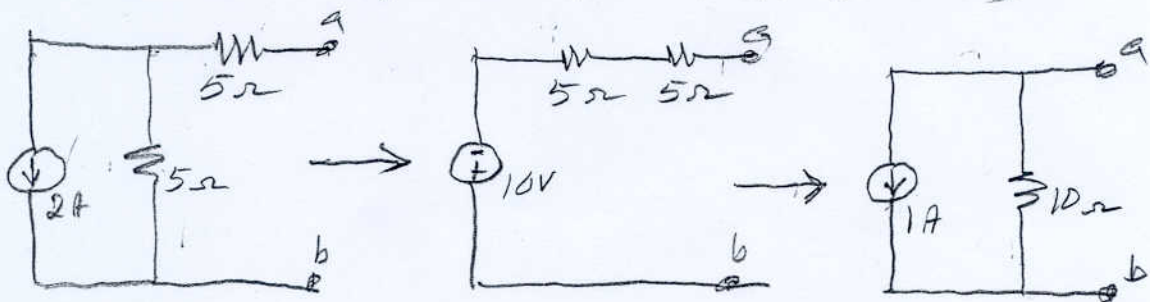


Working circuits using source transformations is a little like a chess or checkers game.

Different people will make different moves to get to the same end.

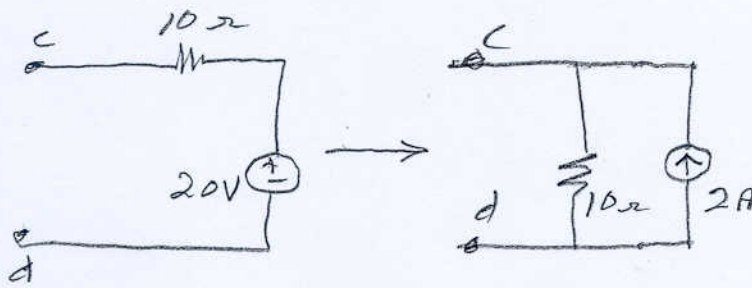
What I see is making a current to voltage transformation to the left of a-b. Then make a voltage to current transformation to the right of c-d. Then combine current sources to one net current source; combine resistors to one resistor - then use the current division to find i .

First step, to the left of a-b

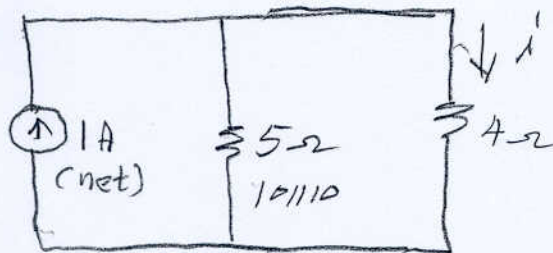
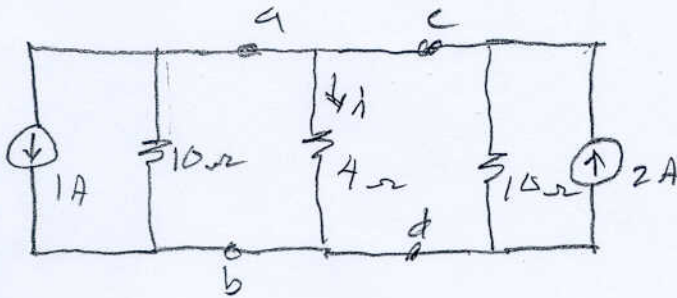


4.22 contd.

2



Now combine



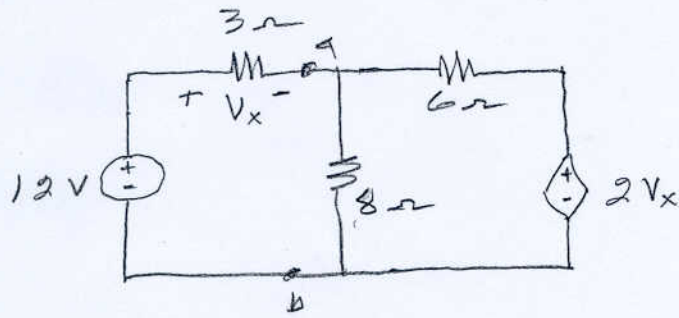
Current Division

$$i' = \frac{1 \times 5}{5 + 4}$$

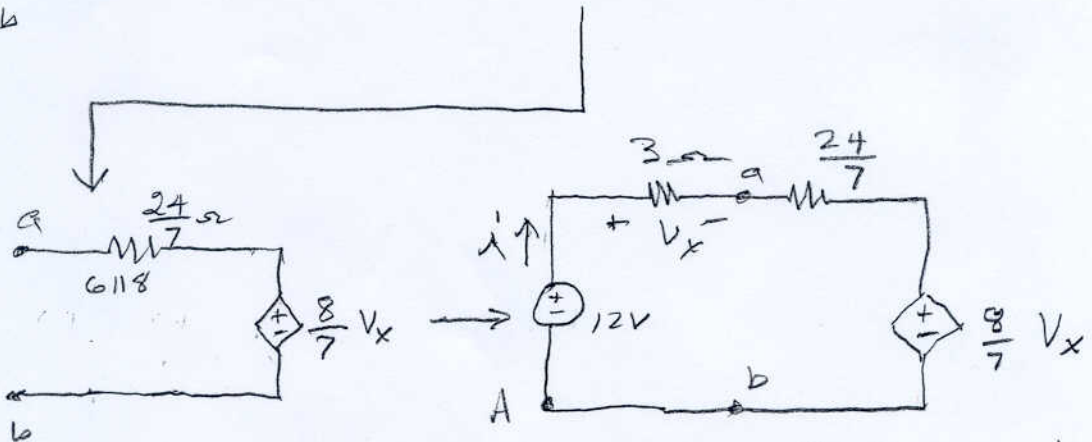
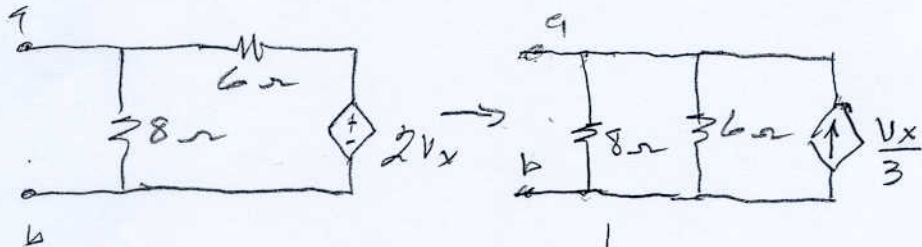
$$i' = \frac{5}{9} \text{ A} = 0.555 \text{ A}$$

4.31

Determine V_x in the following circuit



My plan: I can do a voltage to current transformation to the right of a-b. I will then have a series single loop circuit for which I can apply KVL to find V_x . Notes: I cannot do a source transformation (left of a-b; voltage to current) because I will lose identity of V_x .



Combined Circuit

H.31 cont.

2

From the combined circuit we write KVL, starting at A, go c.w., $\sum \text{drops} = 0$

$$-12 + V_x + \frac{24}{7} i' + \frac{8}{7} V_x = 0$$

$$\text{but } V_x = 3i'$$

so

$$-12 + V_x + \frac{24}{7} \left(\frac{V_x}{3} \right) + \frac{8}{7} V_x = 0$$

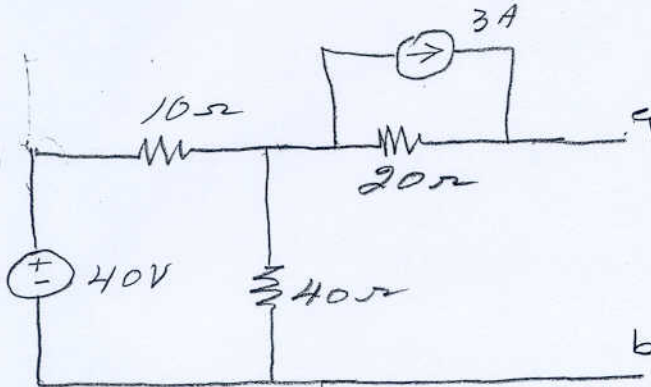
$$-12 + V_x + \frac{16}{7} V_x = 0$$

$$V_x = \frac{84}{23} \text{ V}$$

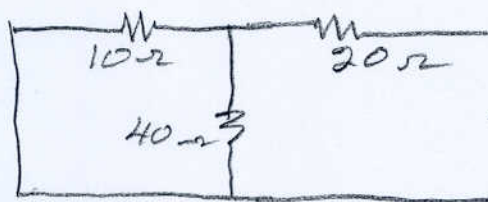
4.34

Find the Thevenin circuit for the following, left of a-b

We worked a problem like this in class - Thu - Feb 8.



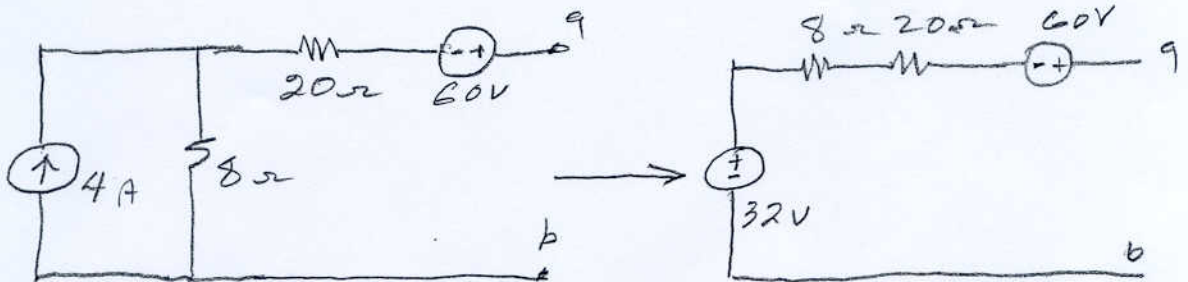
To find R_{TH} , de-energize sources, giving



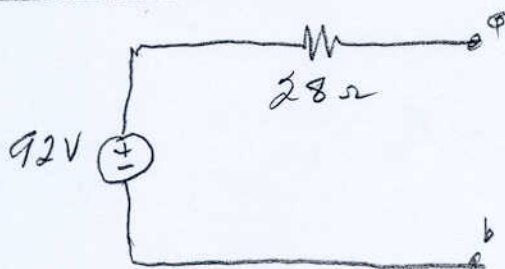
$$\rightarrow R_{TH} = 10 \parallel 40 + 20$$

$$R_{TH} = 28 \Omega$$

If we use source transformations we have

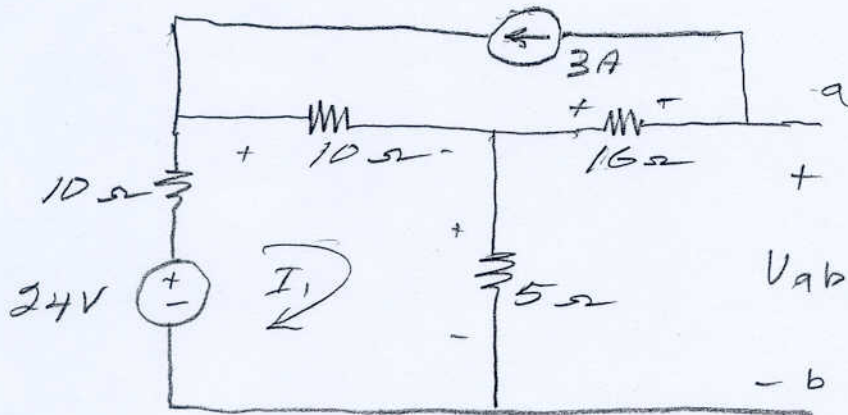


Simplifying:

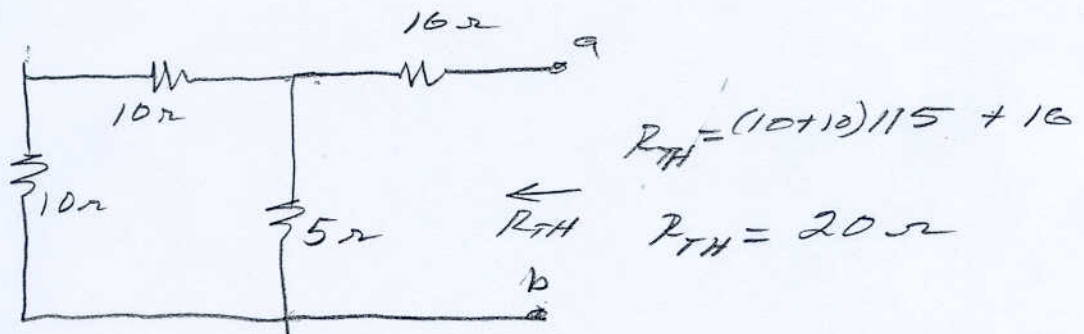


The Thevenin circuit

4.29 Find the Thevenin circuit of the following.



To find R_{TH} de-energize the sources



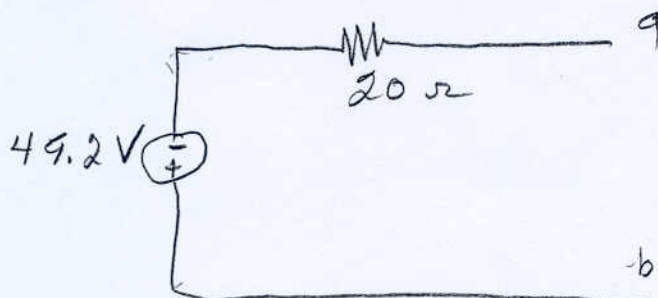
Looks like mesh is the quickest way to solve for $V_{oc} = V_{ab}$. We have

$$-24 + 10I_1 + 10(I_1 + 3) + 5I_1 = 0$$

$$I_1 = -\frac{6}{25}$$

$$\text{Then } -V_{ab} - 16 \times 3 + 5\left(-\frac{6}{25}\right) = 0$$

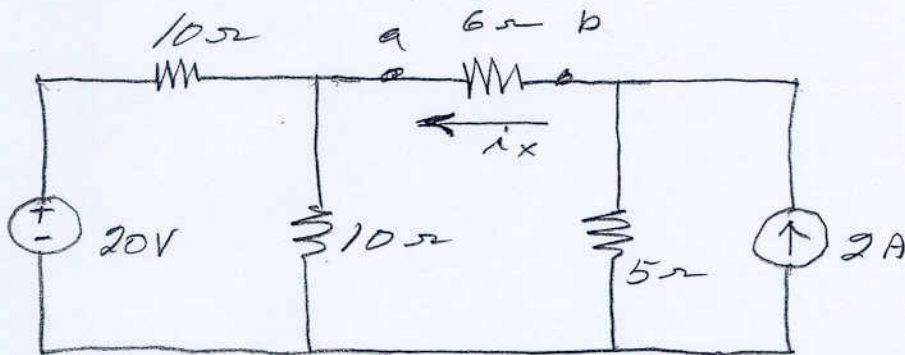
$$V_{ab} = V_{oc} = V_{TH} = -49.2 \text{ V}$$



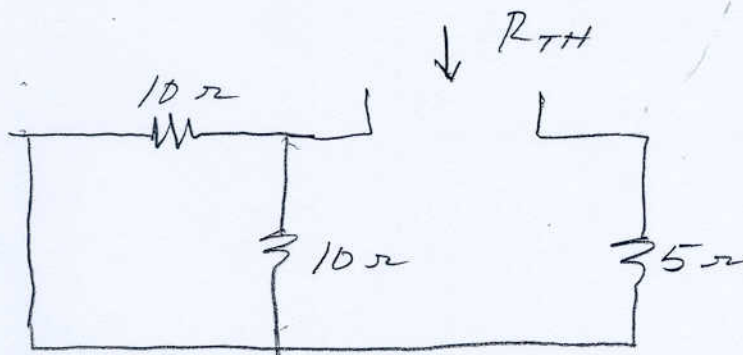
The Thevenin circuit

4.43

Find the Thevenin circuit looking into terminals a-b; then use the Thevenin circuit to find i_x

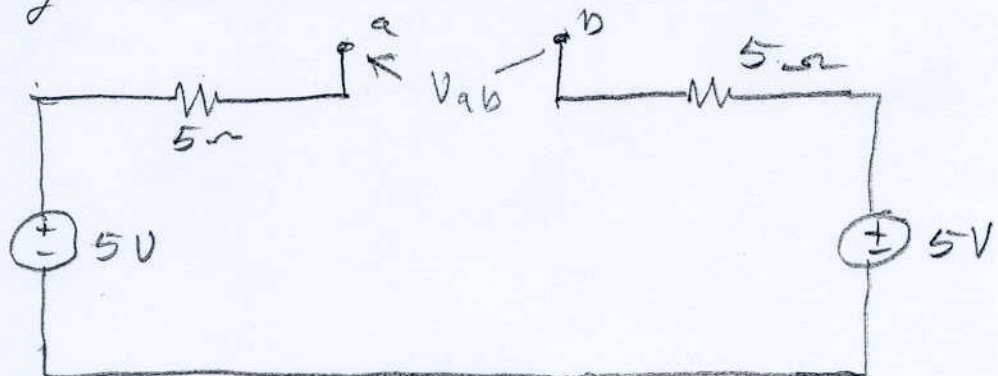


To find R_{TH} , de-energize the sources. This gives



$$R_{TH} = 10 \parallel 10 + 5 = 10 \Omega$$

Using source transformations we have



4.43 cont

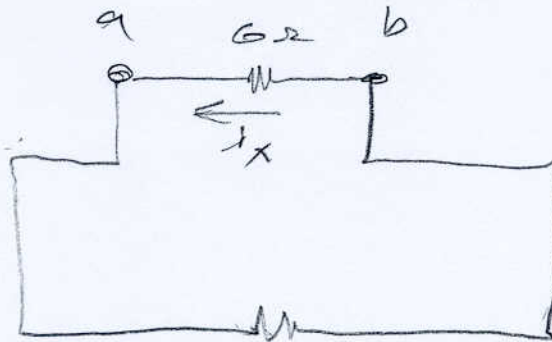
2

Writing KVL

$$-V_{ab} + 5 - 5 = 0$$

$$V_{ab} = V_{oc} = V_{TH} = 0$$

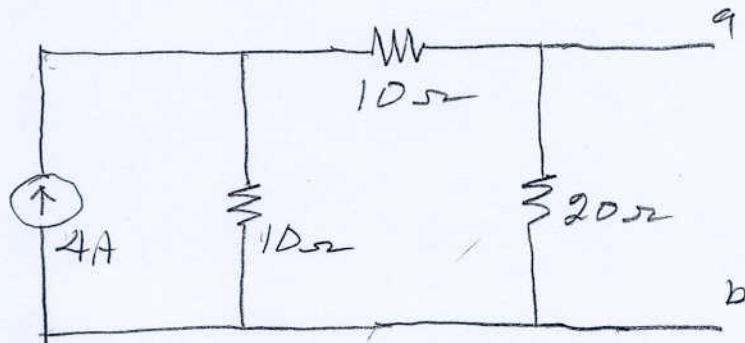
The Thevenin circuit with
the 6Ω connected:



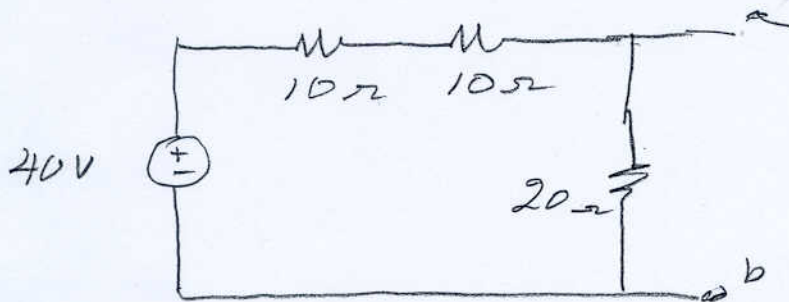
obviously $i_x = 0$

4.46 Given the circuit below

- FIND the open-circuit voltage
- FIND the short-circuit current
- From (a) & (b) determine I_N & R_{TH}

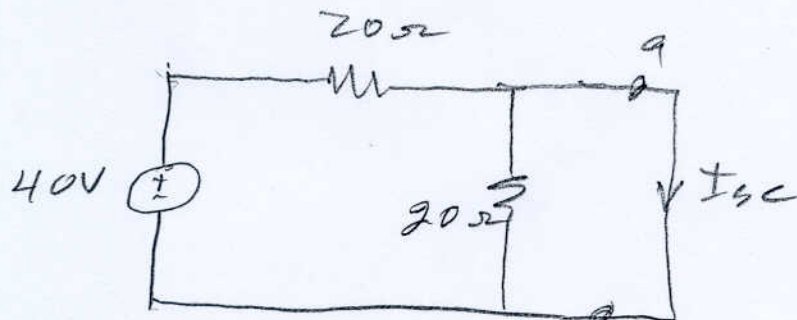


To find the open-circuit voltage
use source transformation.



$$V_{ab} = \underline{V_{oc}} = V_{TH} = \frac{40 \times 20}{20 + 20} = 20V = V_{oc}$$

Use the above ckt to find I_{sc}



4.46 cont.

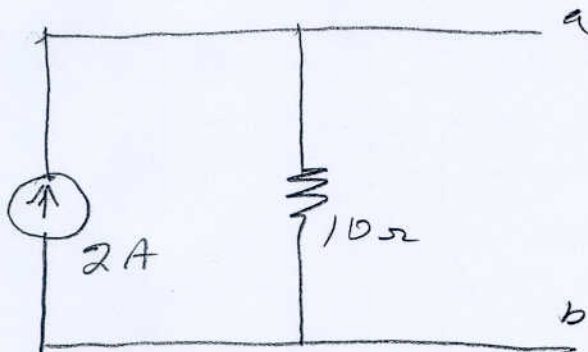
2

$$I_{sc} = \frac{40}{20} = 2A$$

$$(c) R_N = R_{TH} = \frac{V_{oc}}{I_{sc}} = \frac{20}{2} = 10\Omega$$

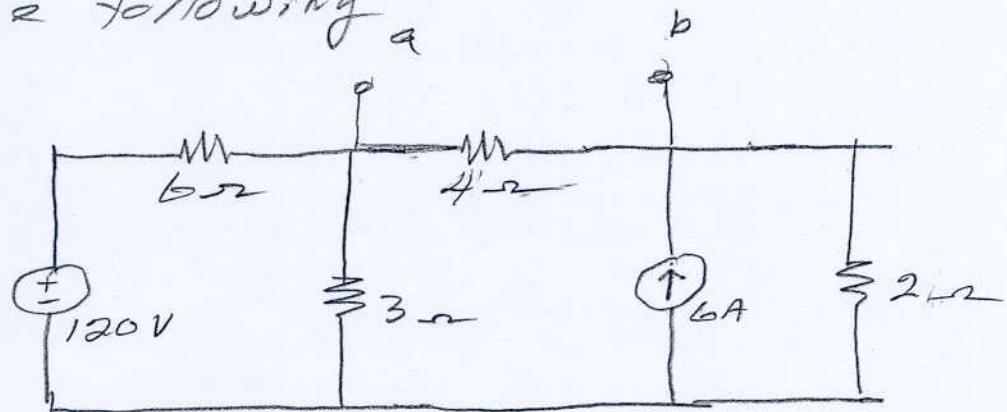
$$I_N = I_{sc} = 2A$$

Norton net

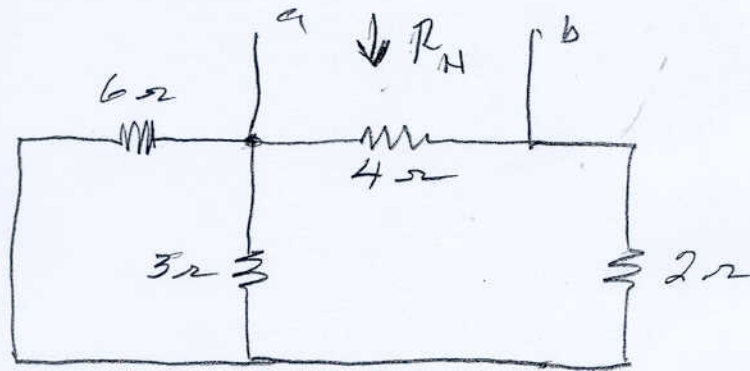


4.51

(a) Obtain the Norton circuit for the following a

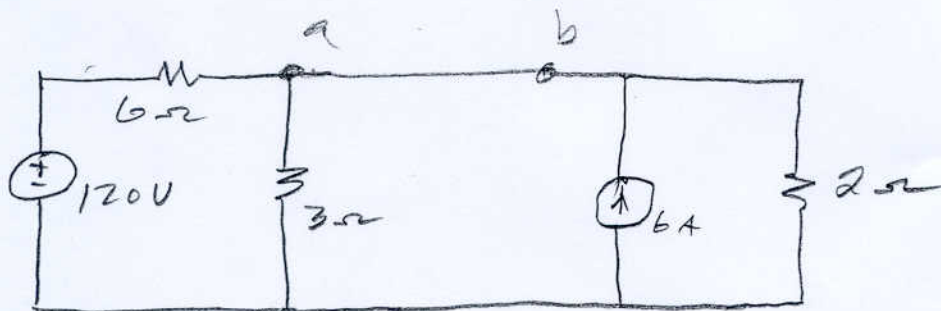


To find $R_N = R_{TH}$ De-energize the independent sources.



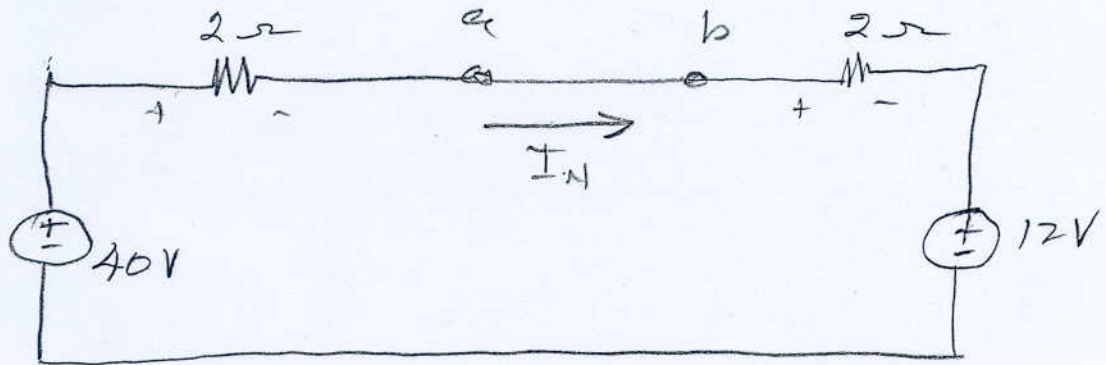
$$R_N = 4 \parallel 4 = 2\Omega$$

When we place a short across a-b we short out the 4Ω resistor. The circuit becomes as follows:



4.51 cont

Using source transformations²
we have.



$$-40 + 4I_N + 12 = 0$$

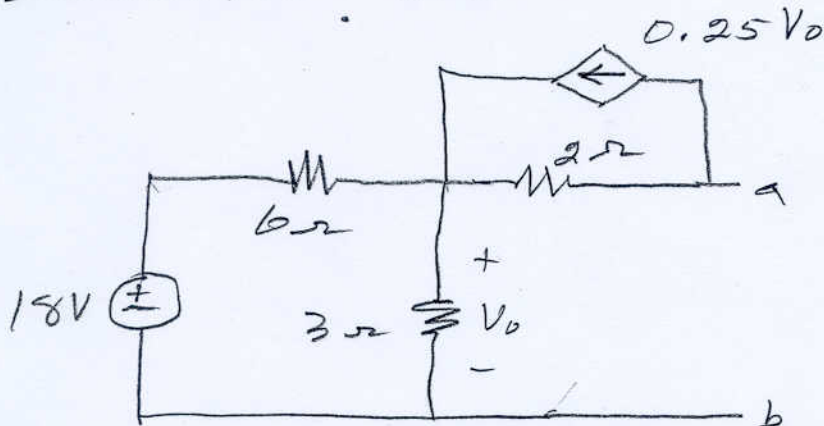
$$I_N = 7A$$

$$R_N = 2\Omega$$

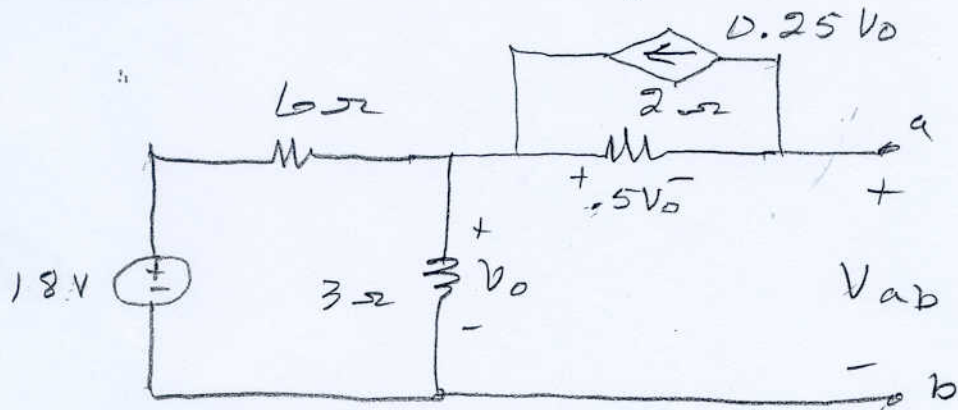
current goes right to left

4.53

Find the Norton equivalent at terminals a-b



First find the open-circuit voltage.



Using KVL

$$-V_{ab} - 0.5V_0 + V_0 = 0$$

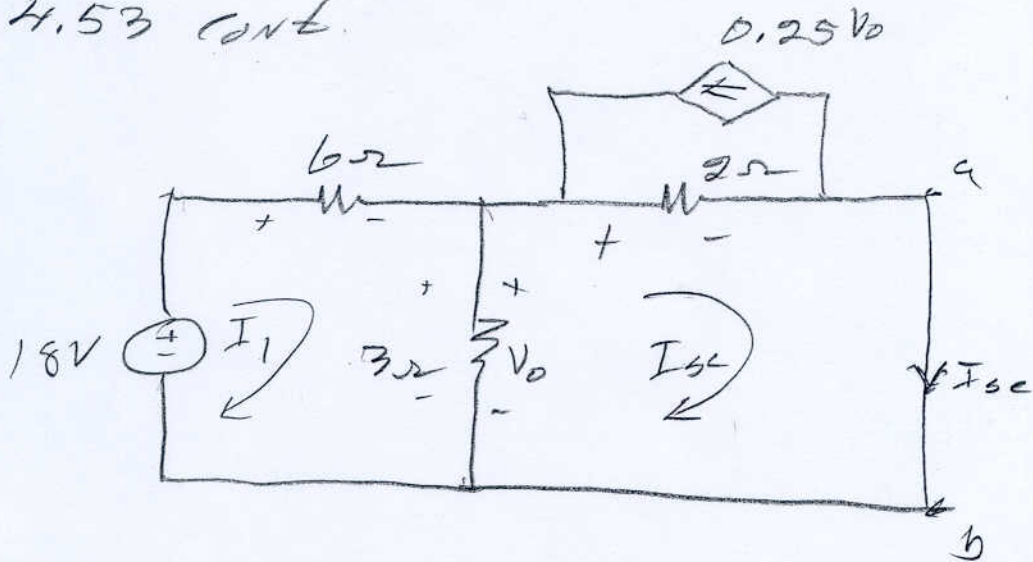
$$\text{but } V_0 = \frac{18 \times 3}{3 + 6} = 6V$$

$$\therefore V_{ab} = 0.5V_0 = \boxed{3V = V_{oc}}$$

Now find I_{sc}

H.53 cont.

2



Using mesh analysis

$$-18 + 6I_1 + 3(I_1 - I_{sc}) = 0$$

$$\boxed{9I_1 - 3I_{sc} = 18}$$

$$-3(I_1 - I_{sc}) + 2(I_{sc} + 0.25V_o) = 0$$

$$\text{but } V_o = 3(I_1 - I_{sc})$$

so

$$-3(I_1 - I_{sc}) + 2(I_{sc} + 0.25 \times 3(I_1 - I_{sc})) = 0$$

$$-3I_1 + 3I_{sc} + 2I_{sc} + 1.5I_1 - 1.5I_{sc} = 0$$

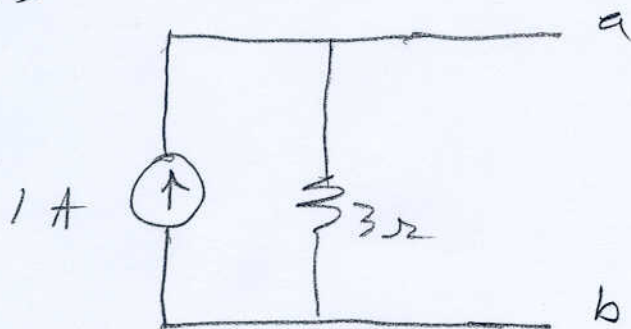
$$\boxed{-1.5I_1 + 3.5I_{sc} = 0}$$

$$\boxed{I_{sc} = 1A} ; V_{oc} = 3V$$

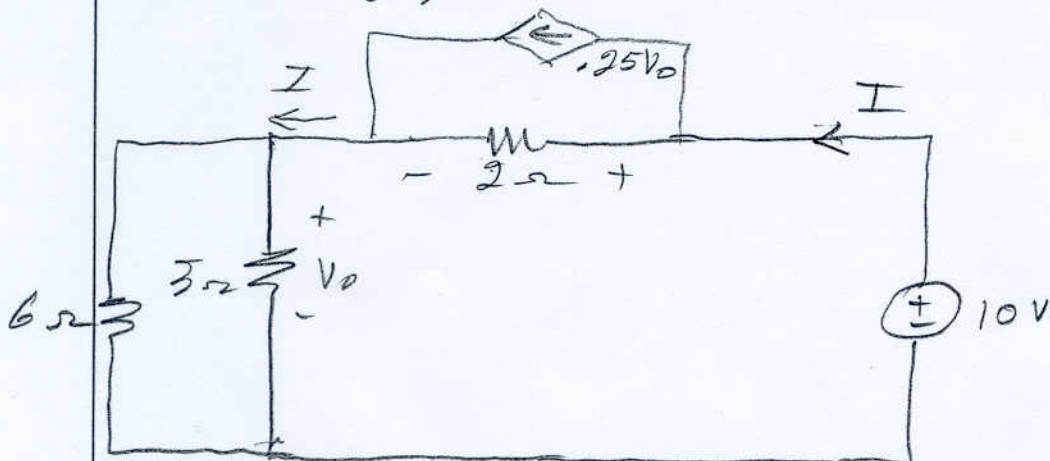
$$\therefore I_H = 1A ; R_H = \frac{V_{oc}}{I_{sc}} = \frac{3}{1} = 3\Omega$$

4.53 cont

so the Norton equivalent circuit is



Another way of finding $R_N = R_{TH}$ is given below. We will apply a 10V signal to the circuit and find the resulting current when all independent sources are de-energized, we have

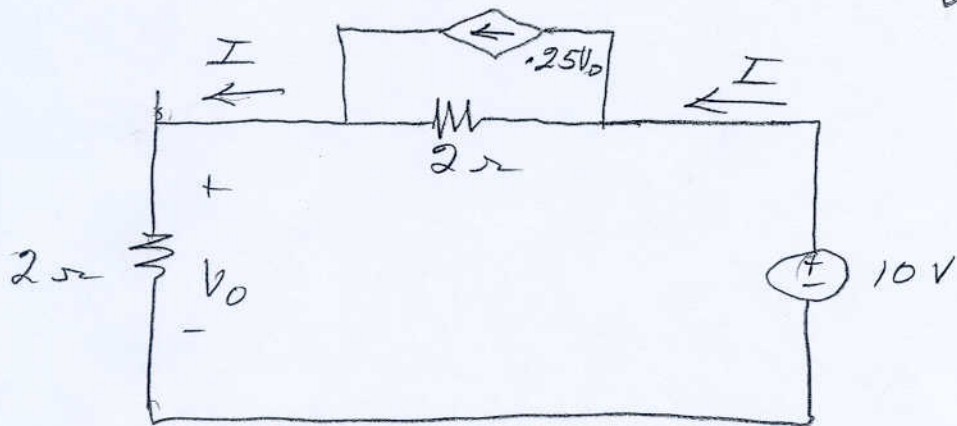


$$R_{TH} = \frac{10}{I}$$

4.53 cont

4

so we solve the following ckt



Using KVL

$$-10 + 2(I - 0.5V_0) + V_0 = 0$$

$$-10 + 2I - 0.5V_0 + V_0 = 0$$

$$-10 + 2I + 0.5V_0 = 0$$

$$\text{but } V_0 = 2I$$

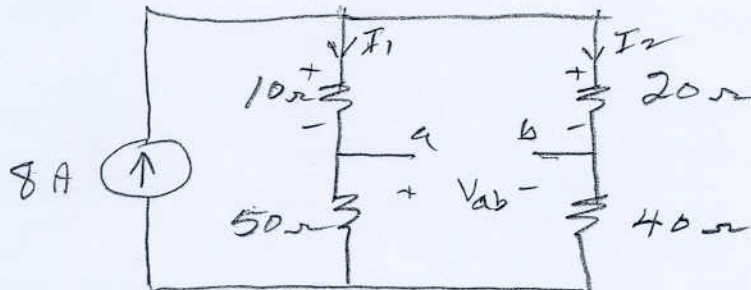
so

$$-10 + 2I + I = 0$$

$$\boxed{\frac{10}{I} = 3 = R_{TH}} \quad \text{QED}$$

4.59

Determine the Thevenin and Norton circuit for the following



Thevenin

With the 8A source de-energized we have

$$R_{TH} = 30 \parallel 90 = 22.5 \Omega$$

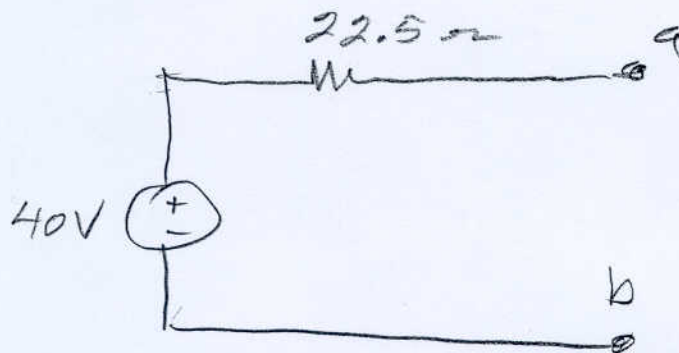
By inspection $I_1 = I_2 = 4 \text{ A}$

$$V_{TH} = V_{ab}$$

$$-V_{ab} - 10I_1 + 20I_2 = 0$$

$$V_{ab} = 20 \times 4 - 10 \times 4 = 40 \text{ V}$$

$$V_{TH} = 40 \text{ V}$$

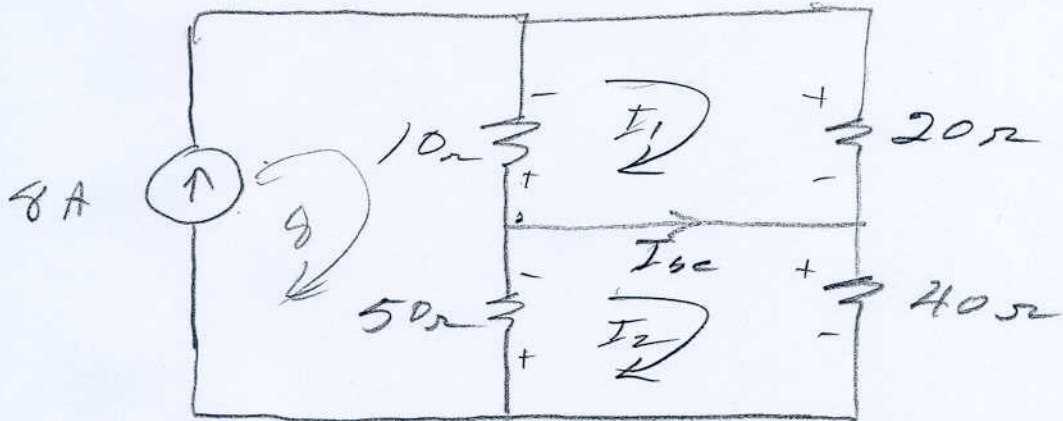


Thevenin
Circuit

4.59 cont

2

To find I_{sc}



$$10(I_1 - 8) + 20I_1 = 0$$

$$30I_1 = 80$$

$$I_1 = \frac{8}{3}$$

$$50(I_2 - 8) + 40I_2 = 0$$

$$90I_2 = 400$$

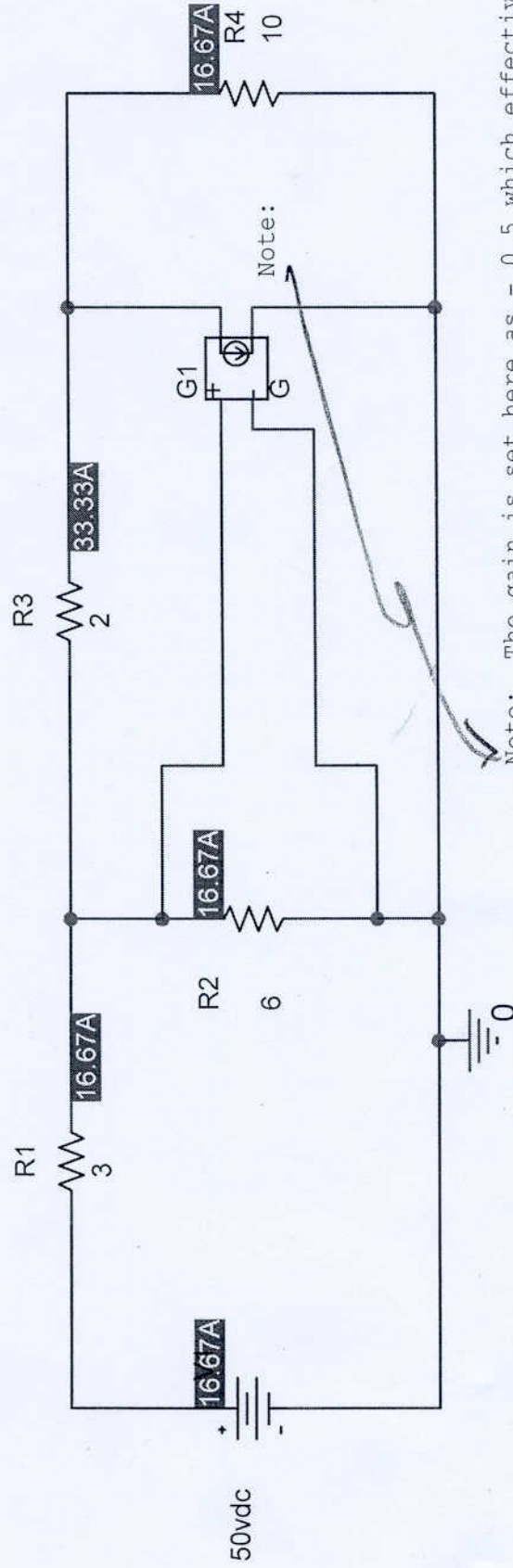
$$I_2 = \frac{40}{9}$$

$$I_{sc} = I_2 - I_1 = \frac{40}{9} - \frac{8}{3} = \frac{16}{9}$$

$$I_{sc} = 1.7778 \text{ A}$$

$$\text{Also } I_N = \frac{V_{TH}}{R_{TH}} = \frac{40}{22.5} = 1.778 \text{ A}$$

This is problem 4.57 from Alexander 3rd Edition



Note: The gain is set here as - 0.5 which effectively turns the current arrow to point upward