

State Plane Analysis of a Buck-Boost Converter

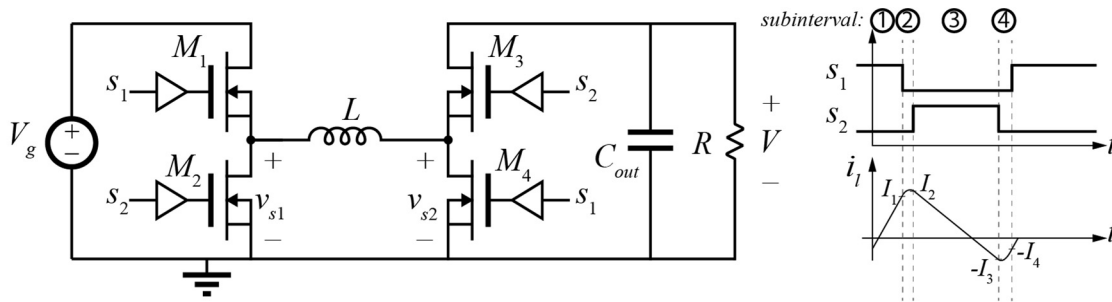


Figure 1: Noninverting Buck-Boost Converter

The noninverting buck-boost converter of Fig. 1 is switched using the given logic-level signals, s_1 and s_2 . The voltages, passives, and switching durations are sized so that the inductor current takes the shape shown in Fig. 1

Devices M_1 - M_4 , are implemented with the same MOSFET, having corresponding capacitances C_{ds1} - C_{ds4} , respectively. C_{out} is very large. The dead times are longer than any switching transient dynamics, but you may assume that $t_{d1} + t_{d2} \ll T_s$. Assume $V = V_g$

- a) During subintervals 2 and 4, when M_1 - M_4 are OFF, sketch the AC-equivalent resonant circuit for state plane analysis. This circuit may have only one L , one C , and any DC voltage and current sources which participate in the resonance. Solve, analytically, the values of all elements in this circuit.

For parts (b)-(e), you may assume that C_{ds1} - C_{ds4} are equal in value.

- b) Sketch the j - m state plane of the converter over an entire switching period. The voltage and current normalized should be those from the resonant elements of part (b). Use $V_{base} = V_g$ and report your I_{base} . Label all salient features.
- c) Determine the conditions for Zero-Voltage Switching each of
 - i) Subinterval 2
 - ii) Subinterval 4
 in the normalized domain. Denormalize these conditions to obtain inequalities which relate the currents I_1 and I_3 to the passive elements and circuit voltages.
- d) Solve for a system of equations which describe the geometry of the state plane. This should include four equations describing J_1 - J_4 , and two equations describing the conduction angles of subintervals 2 and 4.
- e) Average the inductor current over one switching period and normalize to find an expression for J_L in terms of the values solved in (d)