

# Limitations and Discussion

$$\mathbf{X}_0 = \left( I - \prod_{i=k}^0 e^{A_i t_i} \right)^{-1} \sum_{i=1}^k \left( \prod_{j=k}^{i+1} e^{A_j t_j} \right) A_i^{-1} (e^{A_i t_i} - I) B_i \mathbf{u}_i$$



# Topological Time Invariance

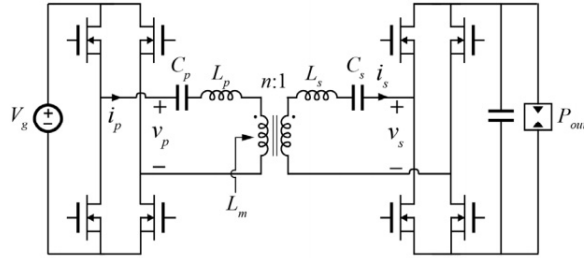


Fig. 1: Series Resonant Converter

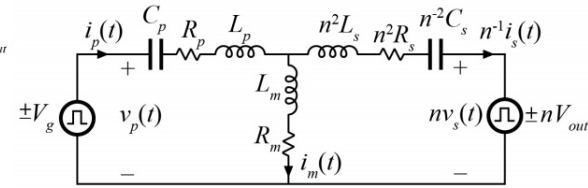


Fig. 2: Time-Invariant Circuit Model of SRC

# Augmented State Space Approach

$$\mathbf{x}(t) = e^{At}\mathbf{x}_0 + \int_0^t e^{A(t-\tau)}\mathbf{B}\mathbf{u}(\tau)d\tau \quad \Longrightarrow \quad \mathbf{x}(t) = e^{At}\mathbf{x}_0 + \mathbf{A}^{-1}(e^{At} - \mathbf{I})\mathbf{B}\mathbf{u}$$

# Non-invertible A Matrices

$$C = \begin{bmatrix} A_1 & B_1 & C_1 & D_1 \\ 0 & A_2 & B_2 & C_2 \\ 0 & 0 & A_3 & B_3 \\ 0 & 0 & 0 & A_4 \end{bmatrix} \begin{array}{l} \} n_1 \\ \} n_2 \\ \} n_3 \\ \} n_4 \end{array}$$

$$\underbrace{\quad}_{n_1} \quad \underbrace{\quad}_{n_2} \quad \underbrace{\quad}_{n_3} \quad \underbrace{\quad}_{n_4}$$

$$e^{Ct} = \begin{bmatrix} F_1(t) & G_1(t) & H_1(t) & K_1(t) \\ 0 & F_2(t) & G_2(t) & H_2(t) \\ 0 & 0 & F_3(t) & G_3(t) \\ 0 & 0 & 0 & F_4(t) \end{bmatrix}$$

$$F_j(t) = e^{A_j t}, \quad j=1,2,3,4$$

$$G_j(t) = \int_0^t e^{A_j(t-s)} B_j e^{A_{j+1}s} ds, \quad j=1,2,3$$

$$H_j(t) = \int_0^t e^{A_j(t-s)} C_j e^{A_{j+2}s} ds$$

$$+ \int_0^t \int_0^s e^{A_j(t-s)} B_j e^{A_{j+1}(s-r)}$$

$$\cdot B_{j+1} e^{A_{j+2}r} dr ds, \quad j=1,2$$

$$K_1(t) = \int_0^t e^{A_1(t-s)} D_1 e^{A_4 s} ds + \int_0^t \int_0^s e^{A_1(t-s)} [C_1 e^{A_3(s-r)} B_3$$

$$+ B_1 e^{A_2(s-r)} C_2] e^{A_4 r} dr ds$$

$$+ \int_0^t \int_0^s \int_0^r e^{A_1(t-s)} B_1 e^{A_2(s-r)} B_2 e^{A_3(r-w)} B_3 e^{A_4 w} dw dr ds.$$





# Computing Integrals