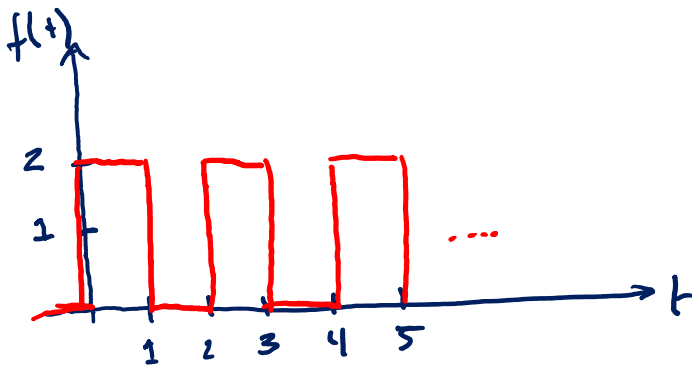


5. Calculate the Fourier coefficients $a_0, a_1, a_2, a_3, b_1, b_2,$ and b_3 for the periodic function $f(t) = 2u(t) - 2u(t+1) + 2u(t+2) - 2u(t+3) + \dots$.



So the period is $T=2$

$$a_0 = \frac{1}{T} \int_0^T f(t) dt = \frac{1}{2} \int_0^1 2 dt = \boxed{1 = a_0}$$

The fundamental frequency is $\omega_0 = \frac{2\pi}{T} = \pi$ rad/sec

$$a_n = \frac{2}{T} \int_0^T f(t) \cos(n\omega_0 t) dt \quad \text{where } f(t) = \begin{cases} 2, & 0 < t < 1 \\ \phi, & 1 < t < 2 \end{cases}$$

$$= \frac{2}{T} \int_0^1 2 \cos(n\omega_0 t) dt = \frac{4}{T} \left[\frac{1}{n\omega_0} \sin(n\omega_0 t) \right]_0^1$$

$$= \frac{4}{T} \frac{1}{n\omega_0} \left(\underbrace{\sin(n\pi \cdot 1)}_{\phi} - \underbrace{\sin(n \cdot \pi \cdot \phi)}_{\phi} \right)$$

So $\boxed{\text{all } a_n = \phi}$

$$b_n = \frac{2}{T} \int_0^T f(t) \sin(n\omega_0 t) dt = \frac{4}{T} \int_0^1 \sin(n\omega_0 t) dt$$

$$= \frac{4}{T} \frac{1}{n\omega_0} \left[-\cos(n\omega_0 t) \right]_0^1$$

$$= \frac{4}{2} \frac{1}{n\pi} \left[-\underbrace{\cos(n\pi)}_{\begin{cases} -1, & n \text{ even} \\ +1, & n \text{ odd} \end{cases}} + \underbrace{\cos(\phi)}_{=1} \right]$$

$$\boxed{b_n = \frac{4}{n\pi}}$$

$$\boxed{b_1 = \frac{4}{\pi} \quad b_2 = \phi \quad b_3 = \frac{4}{3\pi}}$$