

54. Determine the input impedance $Z_{in}(s)$ seen looking into the terminals of the network depicted in Fig. 14.52. Express your answer as a ratio of two s-polynomials.

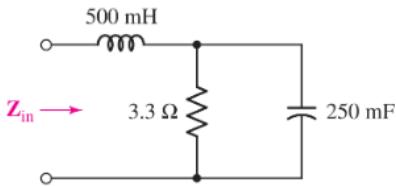


FIGURE 14.52

$$\begin{aligned}
 Z_{in} &= sL + \frac{1}{sC} \\
 &= sL + \frac{R}{1+sRC} \\
 &= \frac{sL + s^2LCR}{1+sRC} + \frac{R}{1+sRC} \\
 &= \frac{s^2LCR + sL + R}{1+sRC}
 \end{aligned}$$

Double-check:
at low frequency, $L \rightarrow \text{short}$, $C \rightarrow \text{open}$, so $Z_{in} \rightarrow R$

$$\text{as } s \rightarrow 0, \lim_{s \rightarrow 0} \frac{s^2LCR + sL + R}{1+sRC} = R \quad \checkmark$$

at high frequency, $C \rightarrow \text{short}$, $L \rightarrow \text{open}$, so $Z_{in} \rightarrow sL$

$$\text{as } s \rightarrow \infty, \lim_{s \rightarrow \infty} \frac{s^2LCR + sL + R}{1+sRC} = \lim_{s \rightarrow \infty} \frac{s^2LCR}{sRC} = sL \quad \checkmark$$

Plugging in

$$Z_{in}(s) = \frac{0.413s^2 + 0.5s + 3.3}{1 + 0.82s}$$