

27. Reconstruct the time-domain function if its transform is (a)  $\frac{s}{s(s+2)}$ ; (b) 1; (c)

3  $\frac{s+2}{(s^2+2s+4)}$ ; (d)  $4\frac{s}{2s+3}$ .

a)  $\frac{s}{s(s+2)} = \frac{1}{s+2}$ ,  $\mathcal{L}^{-1}\left\{\frac{1}{s+2}\right\} = \boxed{e^{-2t} u(t)}$

b)  $\mathcal{L}^{-1}\{1\} = \boxed{\delta(t)}$

c)  $3\frac{s+2}{s^2+2s+4} = 3\left[\frac{s+1}{(s+1)^2+3} + \frac{1}{(s+1)^2+3}\right]$

$f(t) = 3\mathcal{L}^{-1}\left\{\frac{s+1}{(s+1)^2+3}\right\} + \frac{3}{\sqrt{3}}\mathcal{L}^{-1}\left\{\frac{\sqrt{3}}{(s+1)^2+3}\right\}$

$= 3e^{-t}\cos\sqrt{3}t + \frac{3}{\sqrt{3}}e^{-t}\sin\sqrt{3}t$

$= \sqrt{3^2 + \left(\frac{3}{\sqrt{3}}\right)^2} e^{-t} \cos\left(\sqrt{3}t - \tan^{-1}\left(\frac{3/\sqrt{3}}{3}\right)\right)$

$= \boxed{\sqrt{12} e^{-t} \cos(\sqrt{3}t - 30^\circ)}$

Note: this problem was more involved than intended. the book has a mistake  $\rightarrow$  it meant for the denominator to be  $s^2+4s+4 = (s+2)^2$ .

d) long division: 
$$\begin{array}{r} 1/2 \\ 2s+3 \overline{) s} \\ \underline{-s-3/2} \\ -3/2 \end{array}$$

$4\frac{s}{2s+3} = 4\left[\frac{1}{2} - \frac{3}{2}\frac{1}{2s+3}\right]$

$f(t) = 2\mathcal{L}^{-1}\{1\} - 3\mathcal{L}^{-1}\left\{\frac{1}{s+3/2}\right\} = \boxed{2\delta(t) - 3e^{-3/2t} u(t)}$