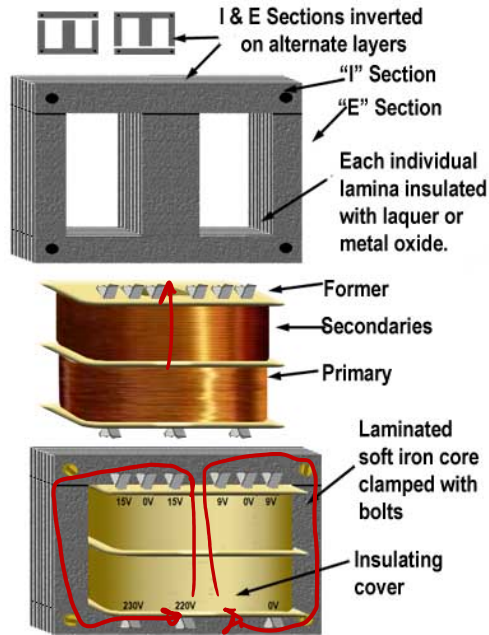
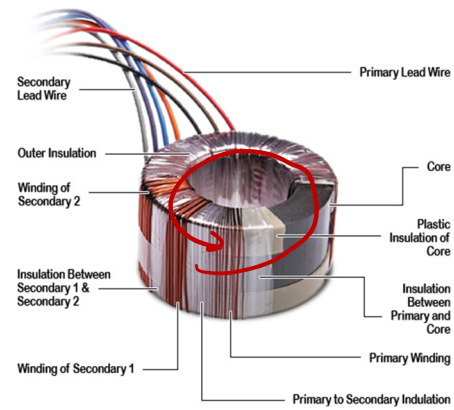


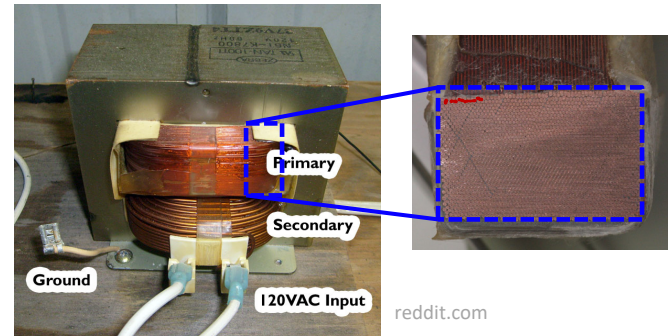
# Example Transformer



[http://www.learnabout-electronics.org/ac\\_theory/transformers03.php](http://www.learnabout-electronics.org/ac_theory/transformers03.php)



<https://www.altrancorp.com/products/toroidal-power-transformers/>



# Transformer Reflection

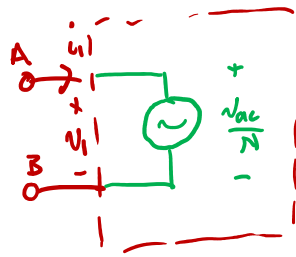
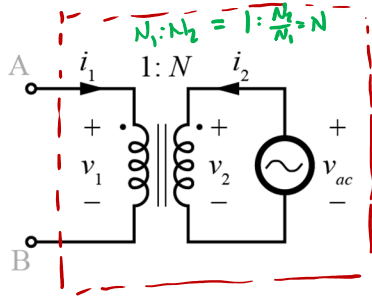
equivalent circuit @ primary

$$\frac{V_1}{I_1} = \frac{Z_2}{N^2}$$

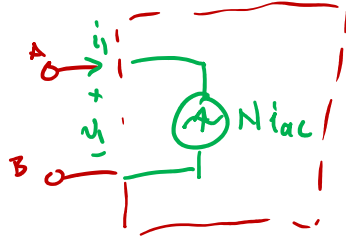
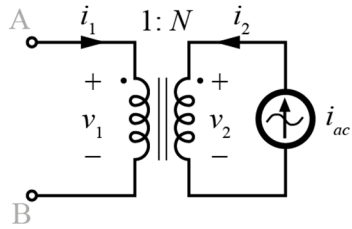
$$1i_1 + Ni_2 = \phi$$

$$N_1 = \frac{N_2}{N}$$

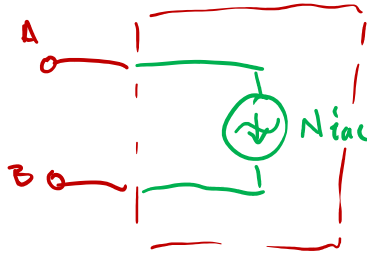
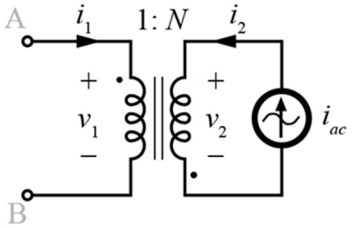
$$i_1 = -Ni_2$$



$$N_1 = \frac{N_2}{N}$$

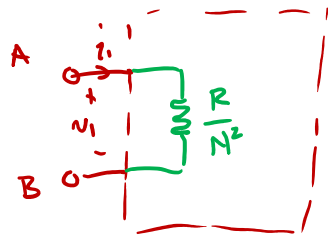
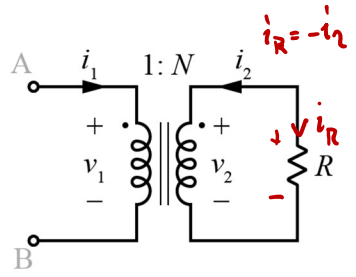


$$i_1 = -Ni_2$$



$$v_1 = \frac{L}{N} \dot{i}_1$$

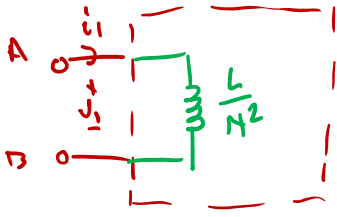
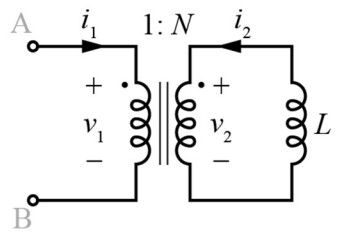
$$i_1 = -N^2 \dot{i}_2$$



$$v_2 = (-i_2) R$$

$$N v_1 = \left(\frac{1}{N}\right) i_1 R$$

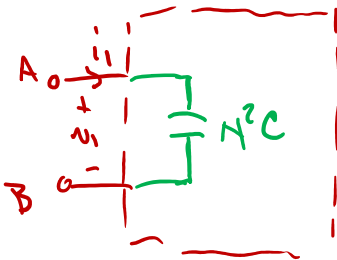
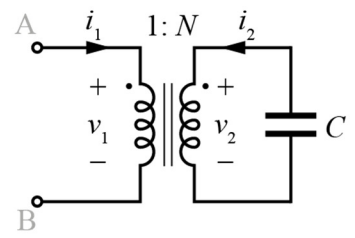
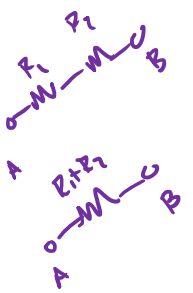
$$v_1 = \left(\frac{1}{N^2} R\right) i_1$$



$$v_2 = L \frac{d(-i_2)}{dt}$$

$$N v_1 = L \frac{d}{dt} \left(\frac{1}{N} i_1\right)$$

$$v_1 = \frac{1}{N^2} L \frac{di_1}{dt}$$

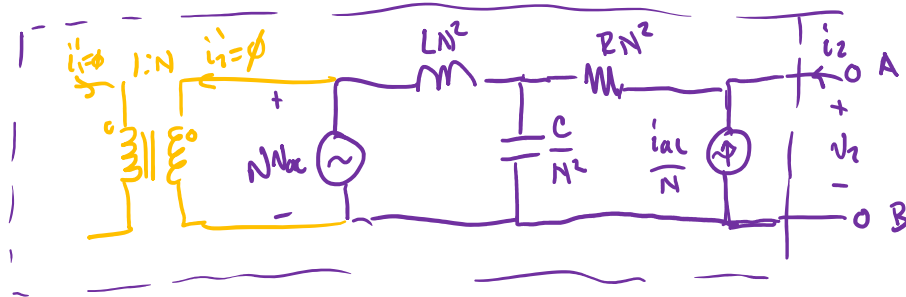
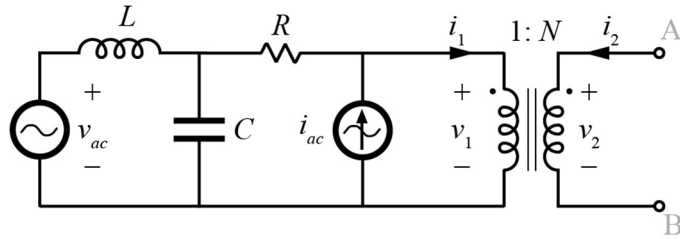


$$-i_2 = C \frac{dv_2}{dt}$$

$$\frac{1}{N} i_1 = C \frac{d}{dt} N v_1$$

$$i_1 = N^2 C \frac{dv_1}{dt}$$

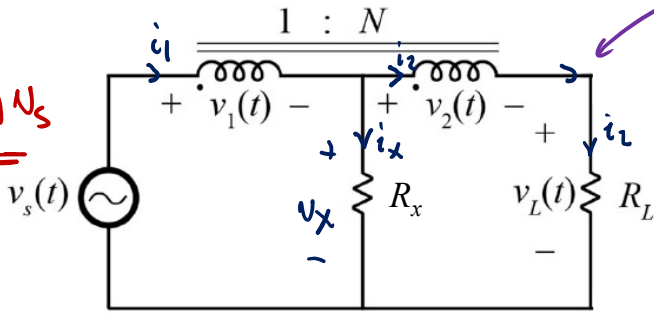
# Example Circuit Simplification



# Ideal Transformer Example

Autotransformer (Variac)

$V_L = f(N, R_L, R_x) V_s$



solve for  $v_L(t)$

Transformer equations

$$N_1 = \frac{N_2}{N}$$

$$i_1 = -N i_2$$

other elements

$$v_x = i_x R_x$$

$$v_L = i_2 R_L$$

KVL :

$$v_x = v_2 + v_L$$

$$v_s = v_1 + v_2 + v_L$$

KCL :

$$i_1 = i_2 + i_x$$