# Lecture 24: Inductor Design Procedure

ECE 481: Power Electronics
Prof. Daniel Costinett

Department of Electrical Engineering and Computer Science
University of Tennessee Knoxville
Fall 2013

## Discussion: design of winding geometry to minimize proximity loss

- Interleaving windings can significantly reduce the proximity loss when the winding currents are in phase, such as in the transformers of buckderived converters or other converters
- In some converters (such as flyback or SEPIC) the winding currents are out of phase. Interleaving then does little to reduce the peak MMF and proximity loss. See Vandelac and Ziogas [10].
- For sinusoidal winding currents, there is an optimal conductor thickness near  $\phi=1$  that minimizes copper loss.
- Minimize the number of layers. Use a core geometry that maximizes the width ℓ<sub>w</sub> of windings.
- Minimize the amount of copper in vicinity of high MMF portions of the windings

#### Litz wire

- A way to increase conductor area while maintaining low proximity losses
- Many strands of small-gauge wire are bundled together and are externally connected in parallel
- Strands are twisted, or transposed, so that each strand passes equally through each position on inside and outside of bundle. This prevents circulation of currents between strands.
- Strand diameter should be sufficiently smaller than skin depth
- · The Litz wire bundle itself is composed of multiple layers
- Advantage: when properly sized, can significantly reduce proximity loss
- Disadvantage: increased cost and decreased amount of copper within core window

## 13.5. Several types of magnetic devices, their *B–H* loops, and core vs. copper loss

A key design decision: the choice of maximum operating flux density  ${\it B}_{\it max}$ 

- Choose  $B_{max}$  to avoid saturation of core, or
- Further reduce  $B_{\max}$  , to reduce core losses

Different design procedures are employed in the two cases.

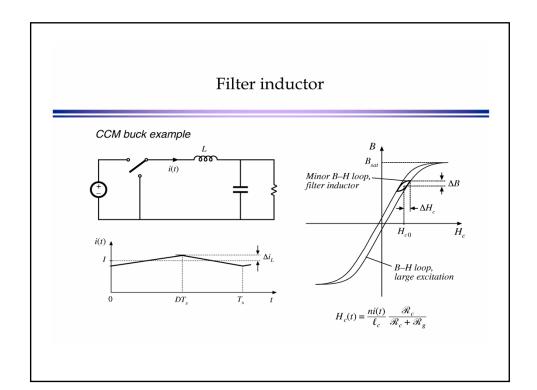
Types of magnetic devices:

Filter inductor AC inductor

Conventional transformer Coupled inductor

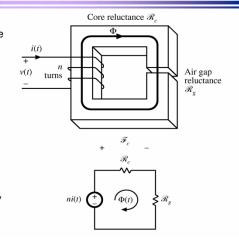
Flyback transformer SEPIC transformer

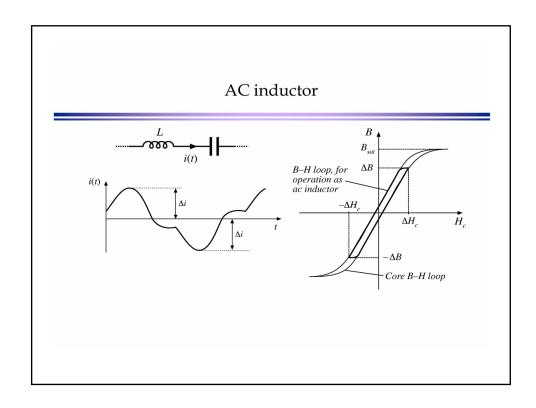
Magnetic amplifier Saturable reactor



#### Filter inductor, cont.

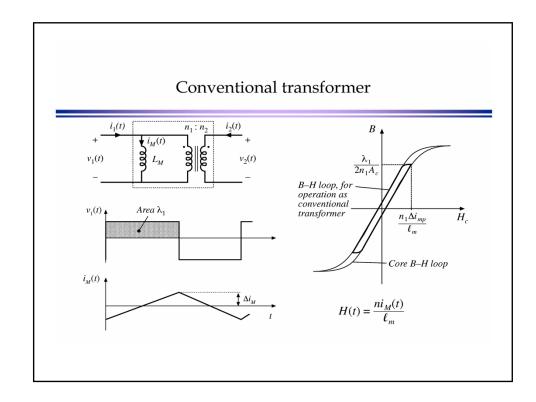
- Negligible core loss, negligible proximity loss
- Loss dominated by dc copper loss
- Flux density chosen simply to avoid saturation
- · Air gap is employed
- Could use core materials having high saturation flux density (and relatively high core loss), even though converter switching frequency is high





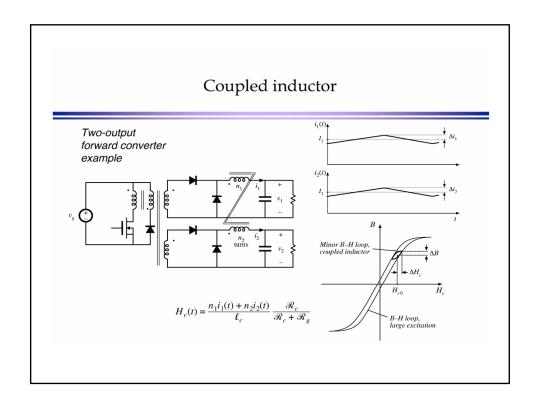
#### AC inductor, cont.

- · Core loss, copper loss, proximity loss are all significant
- An air gap is employed
- Flux density is chosen to reduce core loss
- A high-frequency material (ferrite) must be employed



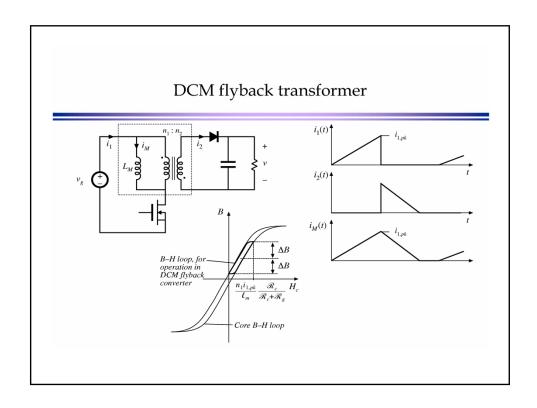
## Conventional transformer, cont.

- Core loss, copper loss, and proximity loss are usually significant
- · No air gap is employed
- · Flux density is chosen to reduce core loss
- A high frequency material (ferrite) must be employed



## Coupled inductor, cont.

- · A filter inductor having multiple windings
- · Air gap is employed
- · Core loss and proximity loss usually not significant
- · Flux density chosen to avoid saturation
- · Low-frequency core material can be employed



## DCM flyback transformer, cont.

- · Core loss, copper loss, proximity loss are significant
- · Flux density is chosen to reduce core loss
- · Air gap is employed
- A high-frequency core material (ferrite) must be used

## Chapter 14 Inductor Design

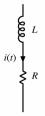
- 14.1 Filter inductor design constraints
- 14.2 A step-by-step design procedure
- 14.3 Multiple-winding magnetics design using the  $K_g$  method
- 14.4 Examples
- 14.5 Summary of key points

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1

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#### 14.1 Filter inductor design constraints



Objective:

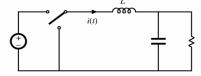
Design inductor having a given inductance L,

which carries worst-case current  $I_{max}$  without saturating,

and which has a given winding resistance R, or, equivalently, exhibits a worst-case copper loss of

$$P_{cu} = I_{rms}^{2} R$$

Example: filter inductor in CCM buck converter



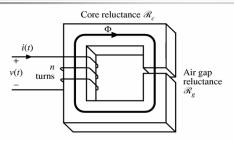
 $\begin{matrix} i(t) \\ I \\ 0 \end{matrix} \qquad \begin{matrix} DT_s \\ T_s \end{matrix} \qquad \begin{matrix} \Delta i_L \\ T_s \end{matrix}$ 

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2

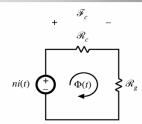
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#### Assumed filter inductor geometry



$$\mathcal{R}_c = \frac{\ell_c}{\mu_c A_c}$$

$$\mathcal{R}_g = \frac{\ell_g}{\mu_0 A_c}$$



Solve magnetic circuit:

$$ni = \Phi\left(\mathcal{R}_c + \mathcal{R}_g\right)$$

Usually  $\mathscr{R}_{c} \ll \mathscr{R}_{g}$  and hence

$$ni \approx \Phi \mathcal{R}_g$$

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#### 14.1.1 Constraint: maximum flux density

Given a peak winding current  $I_{max}$ , it is desired to operate the core flux density at a peak value  $B_{max}$ . The value of  $B_{max}$  is chosen to be less than the worst-case saturation flux density  $B_{sat}$  of the core material.

From solution of magnetic circuit:

$$ni = BA_c \mathcal{R}_g$$

Let  $I = I_{max}$  and  $B = B_{max}$ :

$$nI_{max} = B_{max} A_c \mathcal{R}_g = B_{max} \frac{\ell_g}{\mu_0}$$

This is constraint #1. The turns ratio n and air gap length  $\ell_{\rm g}$  are unknown.

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#### 14.1.2 Constraint: inductance

Must obtain specified inductance L. We know that the inductance is

$$L = \frac{n^2}{\mathcal{R}_g} = \frac{\mu_0 A_c n^2}{\ell_g}$$

This is constraint #2. The turns ratio n, core area  $A_c,$  and air gap length  $\ell_{\rm v}$  are unknown.

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5

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#### 14.1.3 Constraint: winding area

Wire must fit through core window (i.e., hole in center of core)

wire bare area

Total area of copper in window:

 $nA_w$ 

Area available for winding conductors:

 $K_uW_A$ 

Third design constraint:

$$K_u W_A \geq n A_W$$

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6

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 $\begin{array}{l} \text{core window} \\ \text{area} \ W_A \end{array}$ 

#### The window utilization factor $K_u$

also called the "fill factor"

 $K_u$  is the fraction of the core window area that is filled by copper Mechanisms that cause  $K_u$  to be less than 1:

- Round wire does not pack perfectly, which reduces  $K_u$  by a factor of 0.7 to 0.55 depending on winding technique
- Insulation reduces  $K_u$  by a factor of 0.95 to 0.65, depending on wire size and type of insulation
- · Bobbin uses some window area
- · Additional insulation may be required between windings

Typical values of  $K_u$ :

0.5 for simple low-voltage inductor

0.25 to 0.3 for off-line transformer

0.05 to 0.2 for high-voltage transformer (multiple kV)

0.65 for low-voltage foil-winding inductor

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#### 14.1.4 Winding resistance

The resistance of the winding is

$$R = \rho \frac{\ell_b}{A_{w}}$$

where  $\rho$  is the resistivity of the conductor material,  $\ell_b$  is the length of the wire, and  $A_W$  is the wire bare area. The resistivity of copper at room temperature is  $1.724\cdot 10^{-6}\,\Omega\text{-cm}$ . The length of the wire comprising an n-turn winding can be expressed as

$$\ell_b = n(MLT)$$

where (MLT) is the mean-length-per-turn of the winding. The mean-length-per-turn is a function of the core geometry. The above equations can be combined to obtain the fourth constraint:

$$R = \rho \, \frac{n \, (MLT)}{A_w}$$

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## 14.1.5 The core geometrical constant $K_g$

The four constraints:

$$nI_{max} = B_{max} A_c \mathcal{R}_g = B_{max} \frac{\ell_g}{\mu_0} \qquad L = \frac{n^2}{\mathcal{R}_g} = \frac{\mu_0 A_c n^2}{\ell_g}$$

$$K_u W_A \ge nA_W \qquad R = \rho \frac{n (MLT)}{A_W}$$

These equations involve the quantities

 $A_c$ ,  $W_A$ , and MLT, which are functions of the core geometry,

 $\textit{I}_{\textit{max}}, \textit{B}_{\textit{max}}$  ,  $\mu_0, \textit{L}, \textit{K}_{\textit{u}}, \textit{R},$  and  $\rho,$  which are given specifications or other known quantities, and

n,  $\ell_{o}$ , and  $A_{W}$ , which are unknowns.

Eliminate the three unknowns, leading to a single equation involving the remaining quantities.

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9

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## Core geometrical constant $K_g$

Elimination of n,  $\ell_g$ , and  $A_W$  leads to

$$\frac{A_c^2W_A}{(MLT)} \geq \frac{\rho L^2 I_{max}^2}{B_{max}^2 RK_u}$$

- · Right-hand side: specifications or other known quantities
- · Left-hand side: function of only core geometry

So we must choose a core whose geometry satisfies the above equation.

The core geometrical constant  $K_g$  is defined as

$$K_g = \frac{A_c^2 W_A}{(MLT)}$$

#### Discussion

$$K_g = \frac{A_c^2 W_A}{(MLT)} \ge \frac{\rho L^2 I_{max}^2}{B_{max}^2 R K_u}$$

 $K_{\rm g}$  is a figure-of-merit that describes the effective electrical size of magnetic cores, in applications where the following quantities are specified:

- · Copper loss
- · Maximum flux density

How specifications affect the core size:

A smaller core can be used by increasing

 $B_{max} \Rightarrow$  use core material having higher  $B_{sat}$ 

 $R \Rightarrow$  allow more copper loss

How the core geometry affects electrical capabilities:

A larger  $K_{\sigma}$  can be obtained by increase of

 $A_c \Rightarrow$  more iron core material, or

 $W_A \Rightarrow$  larger window and more copper

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1

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## 14.2 A step-by-step procedure

The following quantities are specified, using the units noted:

Wire resistivity  $\rho$  ( $\Omega$ -cm)

Peak winding current  $I_{max}$  (A)

Inductance L (H)

Winding resistance R ( $\Omega$ )

Winding fill factor  $K_u$ Core maximum flux density  $B_{max}$  (T)

The core dimensions are expressed in cm:

Core cross-sectional area  $\stackrel{.}{A_c}$  (cm<sup>2</sup>) Core window area  $\stackrel{.}{W_A}$  (cm<sup>2</sup>) Mean length per turn  $\stackrel{.}{MLT}$  (cm)

The use of centimeters rather than meters requires that appropriate factors be added to the design equations.

#### Determine core size

$$K_g \ge \frac{\rho L^2 I_{max}^2}{B_{max}^2 R K_u} 10^8$$
 (cm<sup>5</sup>)

Choose a core which is large enough to satisfy this inequality (see Appendix D for magnetics design tables).

Note the values of  $A_c$ ,  $W_A$ , and MLT for this core.

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13

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#### Determine air gap length

$$\ell_g = \frac{\mu_0 L I_{max}^2}{B_{max}^2 A_c} 10^4$$
 (m)

with  $A_c$  expressed in cm².  $\mu_0$  =  $4\pi 10^{-7}\,H/m.$ 

The air gap length is given in meters.

The value expressed above is approximate, and neglects fringing flux and other nonidealities.

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14

#### $A_L$

Core manufacturers sell gapped cores. Rather than specifying the air gap length, the equivalent quantity  $A_L$  is used.

 $A_L$  is equal to the inductance, in  $\rm mH,$  obtained with a winding of 1000 turns.

When  ${\cal A}_L$  is specified, it is the core manufacturer's responsibility to obtain the correct gap length.

The required  $A_L$  is given by:

$$A_L = \frac{10B_{max}^2 A_c^2}{LI_{max}^2} \qquad \text{(mH/1000 turns)} \qquad \begin{array}{c} \textit{Units:} \\ A_c & \text{cm}^2, \\ L & \text{Henries,} \\ B_{max} & \text{Tesla.} \end{array}$$

$$L = A_L n^2 10^{-9} \quad \text{(Henries)}$$

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15

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#### Determine number of turns *n*

$$n = \frac{LI_{max}}{B_{max}A_c} \ 10^4$$

#### Evaluate wire size

$$A_W \le \frac{K_u W_A}{n} \quad \text{(cm}^2)$$

Select wire with bare copper area  ${\cal A}_W$  less than or equal to this value. An American Wire Gauge table is included in Appendix D.

As a check, the winding resistance can be computed:

$$R = \frac{\rho n \ (MLT)}{A_w} \quad (\Omega)$$

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17

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# 14.3 Multiple-winding magnetics design using the $K_g$ method

The  $K_g$  design method can be extended to multiplewinding magnetic elements such as transformers and coupled inductors.

This method is applicable when

- Copper loss dominates the total loss (i.e. core loss is ignored), or
- The maximum flux density  $B_{\max}$  is a specification rather than a quantity to be optimized

To do this, we must

- Find how to allocate the window area between the windings
- Generalize the step-by-step design procedure

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18

#### 14.3.1 Window area allocation

Given: application with k windings having known rms currents and rms current desired turns ratios  $\frac{v_1(t)}{n_1} = \frac{v_2(t)}{n_2} = \dots = \frac{v_k(t)}{n_k}$ Window area  $W_A$ rms current  $I_k$ Core mean length per turn (MLT)

> Wire resistivity  $\rho$ Q: how should the window area  $W_{\!\scriptscriptstyle A}$  be allocated among the windings?

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19

Fill factor  $K_u$ 

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## Allocation of winding area

Winding 1 allocation Winding 2 allocation  $\alpha_2 W_A$ Total window area  $W_A$ etc.  $0 < \alpha_j < 1$ 

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 $\alpha_1 + \alpha_2 + \cdots + \alpha_k = 1$ 

## Copper loss in winding j

Copper loss (not accounting for proximity loss) is

$$P_{cu,j} = I_j^2 R_j$$

Resistance of winding j is

$$R_j = \rho \, \frac{\ell_j}{A_{W,j}}$$

with

$$\ell_j = n_j (MLT)$$

length of wire, winding j

$$A_{\mathit{W},j} = \frac{\mathit{W}_{\mathit{A}}\mathit{K}_{\mathit{u}}\alpha_{\mathit{j}}}{\mathit{n}_{\mathit{j}}} \qquad \text{wire area, winding } \mathit{j}$$

$$R_j = \rho \, \frac{n_j^2 (MLT)}{W_A K_u \alpha}$$

$$R_{j} = \rho \frac{n_{j}^{2}(MLT)}{W_{A}K_{u}\alpha_{j}} \qquad P_{cu,j} = \frac{n_{j}^{2}i_{j}^{2}\rho(MLT)}{W_{A}K_{u}\alpha_{j}}$$

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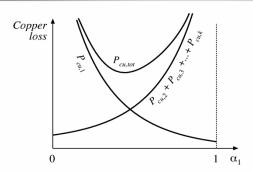
## Total copper loss of transformer

Sum previous expression over all windings:

$$P_{cu,tot} = P_{cu,1} + P_{cu,2} + \dots + P_{cu,k} = \frac{\rho (MLT)}{W_A K_u} \sum_{j=1}^{k} \left( \frac{n_j^2 I_j^2}{\alpha_j} \right)$$

Need to select values for  $\alpha_1, \alpha_2, ..., \alpha_k$  such that the total copper loss is minimized

## Variation of copper losses with $\alpha_1$



For  $\alpha_1$  = 0: wire of winding 1 has zero area.  $P_{cu,1}$  tends to infinity

For  $\alpha_1$  = 1: wires of remaining windings have zero area. Their copper losses tend to infinity

There is a choice of  $\alpha_{\rm l}$  that minimizes the total copper loss

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23

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## Method of Lagrange multipliers

to minimize total copper loss

Minimize the function

$$P_{cu,tot} = P_{cu,1} + P_{cu,2} + \dots + P_{cu,k} = \frac{\rho (MLT)}{W_A K_u} \sum_{j=1}^{k} \binom{n_j^2 I_j^2}{\alpha_j}$$

subject to the constraint

$$\alpha_1 + \alpha_2 + \dots + \alpha_k = 1$$

Define the function

$$f(\alpha_1,\alpha_2,\cdots,\alpha_k,\xi) = P_{cu,tot}(\alpha_1,\alpha_2,\cdots,\alpha_k) + \xi \, g(\alpha_1,\alpha_2,\cdots,\alpha_k)$$

where

$$g(\alpha_1, \alpha_2, \dots, \alpha_k) = 1 - \sum_{j=1}^k \alpha_j$$

is the constraint that must equal zero  $\mbox{and } \xi \mbox{ is the Lagrange multiplier}$ 

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24

#### Lagrange multipliers continued

Optimum point is solution of the system of equations

$$\frac{\partial f(\alpha_1, \alpha_2, \dots, \alpha_k, \xi)}{\partial \alpha_1} = 0$$

$$\begin{split} \frac{\partial f(\alpha_1, \alpha_2, \cdots, \alpha_k, \xi)}{\partial \alpha_1} &= 0 \\ \frac{\partial f(\alpha_1, \alpha_2, \cdots, \alpha_k, \xi)}{\partial \alpha_2} &= 0 \\ &\vdots \end{split}$$

$$\frac{\partial f(\alpha_1, \alpha_2, \dots, \alpha_k, \xi)}{\partial \alpha_k} = 0$$

$$\frac{\partial f(\alpha_1, \alpha_2, \dots, \alpha_k, \xi)}{\partial \xi} = 0$$

$$\frac{\partial f(\alpha_1, \alpha_2, \dots, \alpha_k, \xi)}{\partial \xi} = 0$$

$$\xi = \frac{\rho \left(MLT\right)}{W_A K_u} \left(\sum_{j=1}^k n_j I_j\right)^2 = P_{cu,tot}$$

$$\alpha_m = \frac{n_m I_m}{\sum_{n=1}^{\infty} n_j I_j}$$

An alternate form:

$$\alpha_m = \frac{V_m I_m}{\sum_{m=1}^{\infty} V_j I_j}$$

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## Interpretation of result

$$\alpha_m = \frac{V_m I_m}{\sum_{n=1}^{\infty} V_j I_j}$$

Apparent power in winding j is

 $V_jI_j$ 

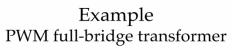
where

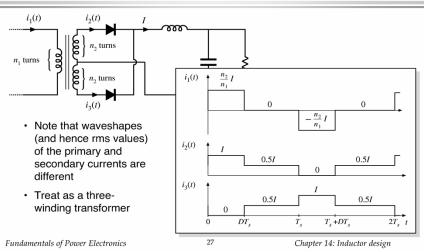
 $V_j$  is the rms or peak applied voltage

 $I_i$  is the rms current

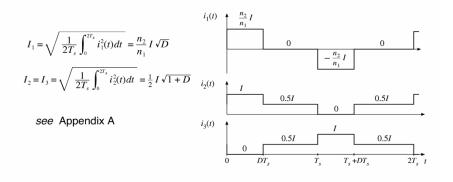
Window area should be allocated according to the apparent powers of the windings

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## Expressions for RMS winding currents



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28

# Allocation of window area: $\alpha_m = \frac{V_m I_m}{\sum_{n=1}^{\infty} V_j I_j}$

Plug in rms current expressions. Result:

$$\alpha_1 = \frac{1}{\left(1 + \sqrt{\frac{1+D}{D}}\right)}$$

Fraction of window area allocated to primary winding

$$\alpha_2 = \alpha_3 = \frac{1}{2} \frac{1}{\left(1 + \sqrt{\frac{D}{1+D}}\right)}$$

Fraction of window area allocated to each secondary winding

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29

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## Numerical example

Suppose that we decide to optimize the transformer design at the worst-case operating point D=0.75. Then we obtain

$$\alpha_1 = 0.396$$

$$\alpha_2 = 0.302$$

$$\alpha_3 = 0.302$$

The total copper loss is then given by

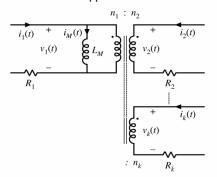
$$\begin{split} P_{cu,tot} &= \frac{\rho(MLT)}{W_A K_u} \left( \sum_{j=1}^{3} n_j I_j \right)^2 \\ &= \frac{\rho(MLT) n_2^2 I^2}{W_A K_u} \left( 1 + 2D + 2\sqrt{D(1+D)} \right) \end{split}$$

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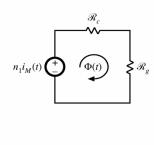
30

#### 14.3.2 Coupled inductor design constraints

Consider now the design of a coupled inductor having k windings. We want to obtain a specified value of magnetizing inductance, with specified turns ratios and total copper loss.



Magnetic circuit model:

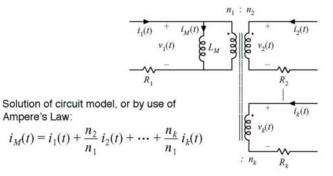


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31

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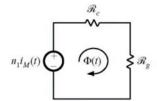
## Relationship between magnetizing current and winding currents



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32

#### Solution of magnetic circuit model: Obtain desired maximum flux density



Assume that gap reluctance is much larger than core reluctance:

$$n_1 i_M(t) = B(t) A_c \mathcal{R}_g$$

Design so that the maximum flux density  $B_{max}$  is equal to a specified value (that is less than the saturation flux density  $B_{sat}$ ).  $B_{max}$  is related to the maximum magnetizing current according to

$$n_1 I_{M,max} = B_{max} A_c \mathcal{R}_g = B_{max} \frac{\ell_g}{\mu_0}$$

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33

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## Obtain specified magnetizing inductance

By the usual methods, we can solve for the value of the magnetizing inductance  ${\cal L}_{\!M}$  (referred to the primary winding):

$$L_{M} = \frac{n_{1}^{2}}{\mathcal{R}_{g}} = n_{1}^{2} \frac{\mu_{0} A_{c}}{\ell_{g}}$$

## Copper loss

Allocate window area as described in Section 14.3.1. As shown in that section, the total copper loss is then given by

$$P_{cu} = \frac{\rho(MLT)n_1^2 I_{tot}^2}{W_A K_u}$$

with

$$I_{tot} = \sum_{j=1}^{k} \frac{n_j}{n_1} I_j$$

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3

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## Eliminate unknowns and solve for $K_g$

Eliminate the unknowns  $\ell_{g}$  and  $n_{1}$ :

$$P_{cu} = \frac{\rho(MLT)L_{M}^{2}I_{tot}^{2}I_{M,max}^{2}}{B_{max}^{2}A_{c}^{2}W_{A}K_{u}}$$

Rearrange equation so that terms that involve core geometry are on RHS while specifications are on LHS:

$$\frac{A_{c}^{2}W_{A}}{(MLT)} = \frac{\rho L_{M}^{2}I_{tot}^{2}I_{M,max}^{2}}{B_{max}^{2}K_{u}P_{cu}}$$

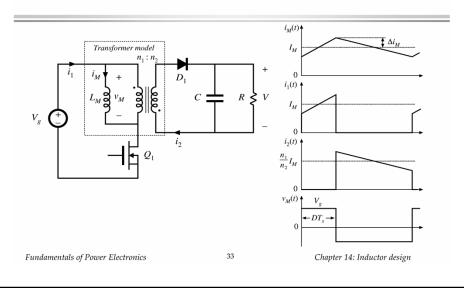
The left-hand side is the same  $K_{\rm g}$  as in single-winding inductor design. Must select a core that satisfies

$$K_g \geq \frac{\rho L_M^2 I_{tot}^2 I_{M,max}^2}{B_{max}^2 K_u P_{cu}}$$

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36





## Specifications

Input voltage  $V_g = 200 \text{V}$ Output (full load) 20 V at 5 A
Switching frequency 150 kHz

Magnetizing current ripple 20% of dc magnetizing current

Duty cycleD = 0.4Turns ratio $n_2/n_1 = 0.15$ Copper loss1.5 WFill factor $K_u = 0.3$ Maximum flux density $B_{max} = 0.25 \text{ T}$ 

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#### Basic converter calculations

Components of magnetizing current, referred to primary:

$$I_M = \left(\frac{n_2}{n_1}\right) \frac{1}{D'} \frac{V}{R} = 1.25 \text{ A}$$

$$\Delta i_M = (20\%)I_M = 0.25 \text{ A}$$

$$I_{M,max} = I_M + \Delta i_M = 1.5 \text{ A}$$

Choose magnetizing inductance:

$$L_M = \frac{V_g DT_s}{2\Delta i_M}$$
$$= 1.07 \text{ mH}$$

RMS winding currents:

$$I_1 = I_M \sqrt{D} \sqrt{1 + \frac{1}{3} \left(\frac{\Delta i_M}{I_M}\right)^2} = 0.796 \text{ A}$$

$$I_2 = \frac{n_1}{n_2} I_M \sqrt{D'} \sqrt{1 + \frac{1}{3} \left(\frac{\Delta i_M}{I_M}\right)^2} = 6.50 \text{ A}$$

$$I_{tot} = I_1 + \frac{n_2}{n_1} I_2 = 1.77 \text{ A}$$

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3

Chapter 14: Inductor design

#### Choose core size

$$K_g \ge \frac{\rho L_M^2 I_{tot}^2 I_{M,max}^2}{B_{max}^2 P_{cu} K_u} 10^8$$

$$= \frac{\left(1.724 \cdot 10^{-6} \Omega \cdot \text{cm}\right) \left(1.07 \cdot 10^{-3} \text{ H}\right)^2 \left(1.77 \text{ A}\right)^2 \left(1.5 \text{ A}\right)^2}{\left(0.25 \text{ T}\right)^2 \left(1.5 \text{ W}\right) \left(0.3\right)} 10^8$$

$$= 0.049 \text{ cm}^5$$

The smallest EE core that satisfies this inequality (Appendix D) is the EE30.



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57

Chapter 14: Inductor design

## Choose air gap and turns

$$\ell_g = \frac{\mu_0 L_M I_{M,max}^2}{B_{max}^2 A_c} 10^4$$

$$= \frac{\left(4\pi \cdot 10^{-7} \text{H/m}\right) \left(1.07 \cdot 10^{-3} \text{ H}\right) \left(1.5 \text{ A}\right)^2}{\left(0.25 \text{ T}\right)^2 \left(1.09 \text{ cm}^2\right)} 10^4$$

$$= 0.44 \text{ mm}$$

$$n_1 = \frac{L_M I_{M,max}}{B_{max} A_c} 10^4$$

$$= \frac{\left(1.07 \cdot 10^{-3} \text{ H}\right) \left(1.5 \text{ A}\right)}{\left(0.25 \text{ T}\right) \left(1.09 \text{ cm}^2\right)} 10^4$$

$$= 8.81$$

$$= 58.7 \text{ turns}$$

Round to  $n_1 = 59$ 

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Chapter 14: Inductor design

## Wire gauges

$$\alpha_1 = \frac{I_1}{I_{tot}} = \frac{(0.796 \text{ A})}{(1.77 \text{ A})} = 0.45$$

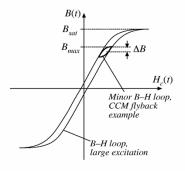
$$\alpha_2 = \frac{n_2 I_2}{n_1 I_{tot}} = \frac{(9)(6.5 \text{ A})}{(59)(1.77 \text{ A})} = 0.55$$

$$A_{W1} \le \frac{\alpha_1 K_u W_A}{n_1} = 1.09 \cdot 10^{-3} \text{ cm}^2$$
 — use #28 AWG  
 $A_{W2} \le \frac{\alpha_2 K_u W_A}{n_2} = 8.88 \cdot 10^{-3} \text{ cm}^2$  — use #19 AWG

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## Core loss CCM flyback example

B-H loop for this application:

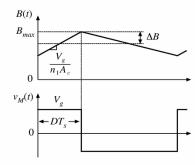


B(t) vs. applied voltage, from Faraday's law:

$$\frac{dB(t)}{dt} = \frac{v_M(t)}{n_1 A_c}$$

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The relevant waveforms:



For the first subinterval:

$$\frac{dB(t)}{dt} = \frac{V_g}{n_1 A}$$

Chapter 14: Inductor design

## Calculation of ac flux density and core loss

Solve for  $\Delta B$ :

$$\Delta B = \left(\frac{V_g}{n_1 A_c}\right) (DT_s)$$

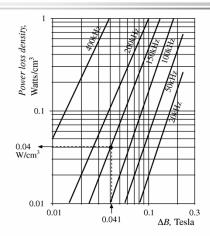
Plug in values for flyback example:

$$\Delta B = \frac{(200 \text{ V})(0.4)(6.67 \text{ µs})}{2(59)(1.09 \text{ cm}^2)} 10^4$$
$$= 0.041 \text{ T}$$

From manufacturer's plot of core loss (at left), the power loss density is  $0.04~\rm W/cm^3$ . Hence core loss is

$$P_{fe} = (0.04 \text{ W/cm}^3)(A_c \ell_m)$$
  
= (0.04 W/cm<sup>3</sup>)(1.09 cm<sup>2</sup>)(5.77 cm)  
= 0.25 W

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#### Comparison of core and copper loss

- Copper loss is 1.5 W
  - does not include proximity losses, which could substantially increase total copper loss
- · Core loss is 0.25 W
  - Core loss is small because ripple and  $\Delta B$  are small
  - It is not a bad approximation to ignore core losses for ferrite in CCM filter inductors
  - Could consider use of a less expensive core material having higher core loss
  - Neglecting core loss is a reasonable approximation for this application
- Design is dominated by copper loss
  - The dominant constraint on flux density is saturation of the core, rather than core loss

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41

Chapter 14: Inductor design

#### 14.5 Summary of key points

- A variety of magnetic devices are commonly used in switching converters. These devices differ in their core flux density variations, as well as in the magnitudes of the ac winding currents. When the flux density variations are small, core loss can be neglected. Alternatively, a low-frequency material can be used, having higher saturation flux density.
- 2. The core geometrical constant  $K_g$  is a measure of the magnetic size of a core, for applications in which copper loss is dominant. In the  $K_g$  design method, flux density and total copper loss are specified.

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