Graphical Construction

Reactance Paper

80 dBΩ			10 kΩ
60 dBΩ	10 H	100 pF	1 kΩ
40 dBΩ	1 H	1 nF	100 Ω
20 dBΩ	100 mH	10 nF	10 Ω
0 dBΩ	10 mH	100 nF	1 Ω
–20 dBΩ	1 mH	1 μF	100 mΩ
–40 dBΩ	100 μH	10 μF	10 mΩ
–60 dBΩ	10 μH 1 F 1 μH 100 mF 100 nH 10 mF 10 nH 1 mF 1 nH 100 μF		1 mΩ

$100 \frac{rad}{sec}$ $1 \text{ k} \frac{rad}{sec}$ $10 \text{ k} \frac{rad}{sec}$ $100 \text{ k} \frac{rad}{sec}$ $1 \text{ M} \frac{rad}{sec}$
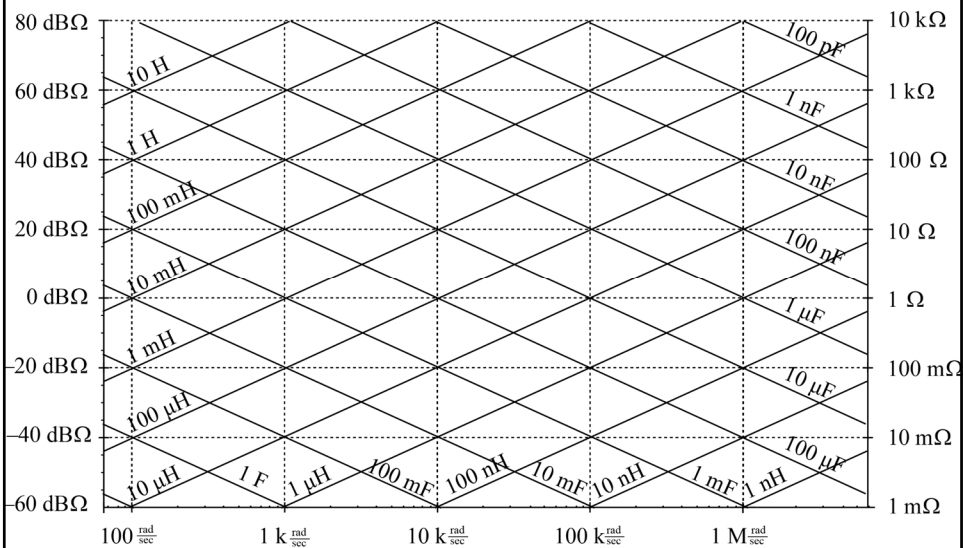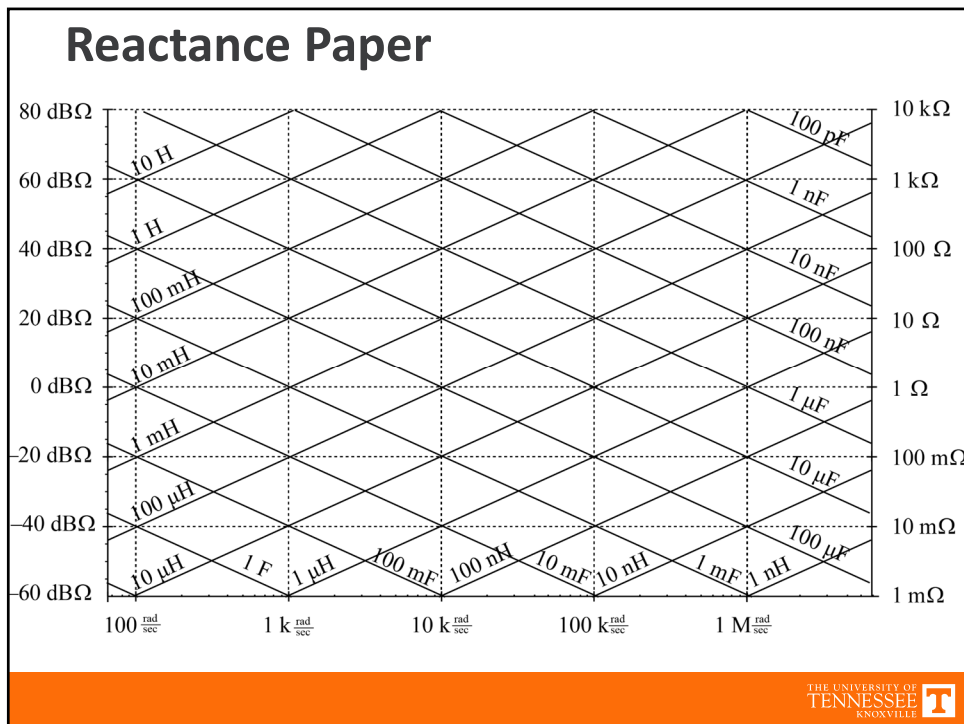
1

Reactance Paper

Chapter 8 Summary

1. The magnitude Bode diagrams of functions which vary as $(f/f_0)n$ have slopes equal to $20n$ dB per decade, and pass through 0dB at $f = f_0$.

2. It is good practice to express transfer functions in normalized pole-zero form; this form directly exposes expressions for the salient features of the response, i.e., the corner frequencies, reference gain, etc.

3. The right half-plane zero exhibits the magnitude response of the left half-plane zero, but the phase response of the pole.

4. Poles and zeroes can be expressed in frequency-inverted form, when it is desirable to refer the gain to a high-frequency asymptote.

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Chapter 8 Summary

5. A two-pole response can be written in the standard normalized form of Eq. (8-53). When $Q > 0.5$, the poles are complex conjugates. The magnitude response then exhibits peaking in the vicinity of the corner frequency, with an exact value of Q at $f = f_0$. High Q also causes the phase to change sharply near the corner frequency.

6. When the Q is less than 0.5, the two pole response can be plotted as two real poles. The low- Q approximation predicts that the two poles occur at frequencies f_0 / Q and Qf_0. These frequencies are within 10% of the exact values for $Q \leq 0.3$.

7. The low- Q approximation can be extended to find approximate roots of an arbitrary degree polynomial. Approximate analytical expressions for the salient features can be derived. Numerical values are used to justify the approximations.

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8. Salient features of the transfer functions of the buck, boost, and buck-boost converters are tabulated in section 8.2.2. The line-to-output transfer functions of these converters contain two poles. Their control-to-output transfer functions contain two poles, and may additionally contain a right half-pland zero.

9. Approximate magnitude asymptotes of impedances and transfer functions can be easily derived by graphical construction. This approach is a useful supplement to conventional analysis, because it yields physical insight into the circuit behavior, and because it exposes suitable approximations. Several examples, including the impedances of basic series and parallel resonant circuits and the transfer function $H_e(s)$ of the boost and buck-boost converters, are worked in section 8.3.

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Chapter 9: Controller Design

9.1. Introduction

9.2. Effect of negative feedback on the network transfer functions

      9.2.1. Feedback reduces the transfer function from disturbances to the output

      9.2.2. Feedback causes the transfer function from the reference input to the output to be insensitive to variations in the gains in the forward path of the loop

9.3. Construction of the important quantities $1/(1+T)$ and $T/(1+T)$ and the closed-loop transfer functions

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Chapter 9: Controller Design

9.4. Stability

      9.4.1. The phase margin test

      9.4.2. The relation between phase margin and closed-loop damping factor

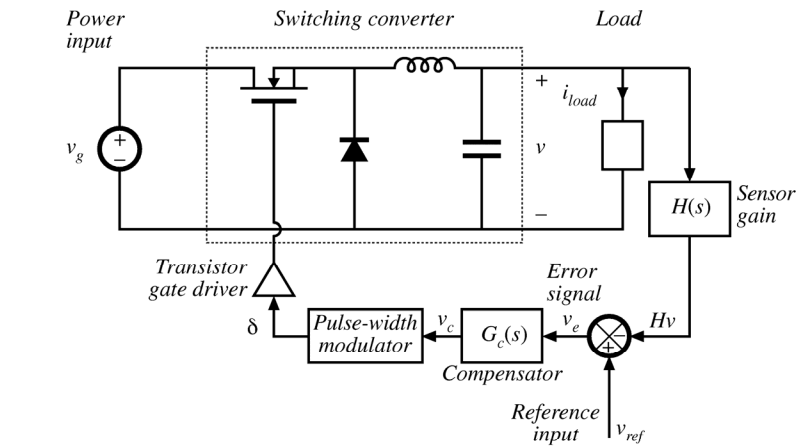   9.4.3. Transient response vs. damping factor

9.5. Regulator design

      9.5.1. Lead (PD) compensator

      9.5.2. Lag (PI) compensator

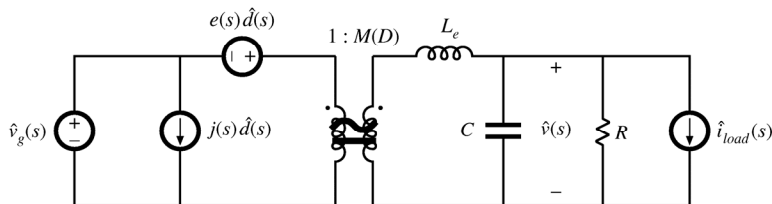   9.5.3. Combined (PID) compensator

      9.5.4. Design example

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Closed-Loop Regulation

Open-Loop Behavior

Small signal model: open-loop converter

Output voltage can be expressed as

$$\hat{v}(s) = G_{vd}(s)\,\hat{d}(s) + G_{vg}(s)\,\hat{v}_g(s) - Z_{out}(s)\,\hat{i}_{load}(s)$$

where

$$G_{vd}(s) = \left.\frac{\hat{v}(s)}{\hat{d}(s)}\right|_{\substack{\hat{v}_g = 0 \\ \hat{i}_{load} = 0}} \qquad G_{vg}(s) = \left.\frac{\hat{v}(s)}{\hat{v}_g(s)}\right|_{\substack{\hat{d} = 0 \\ \hat{i}_{load} = 0}} \qquad Z_{out}(s) = -\left.\frac{\hat{v}(s)}{\hat{i}_{load}(s)}\right|_{\substack{\hat{d} = 0 \\ \hat{v}_g = 0}}$$
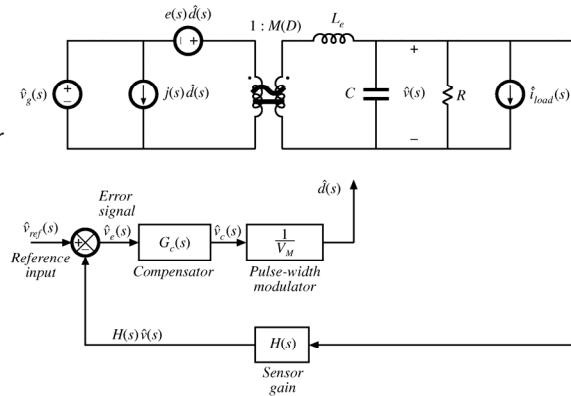
Small-Signal Closed-Loop Model

- *Use small-signal converter model*
- *Perturb and linearize remainder of feedback loop:*

$v_{ref}(t) = V_{ref} + \hat{v}_{ref}(t)$

$v_e(t) = V_e + \hat{v}_e(t)$

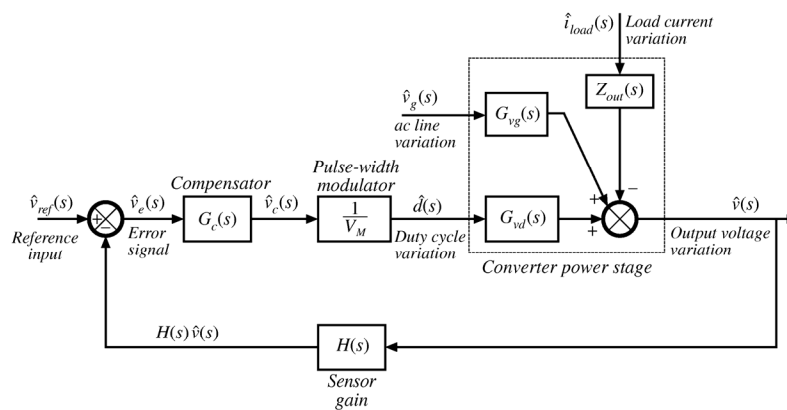 *etc.*

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Block Diagram

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Closed-Loop Transfer Functions

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