

# CMOS Scaling

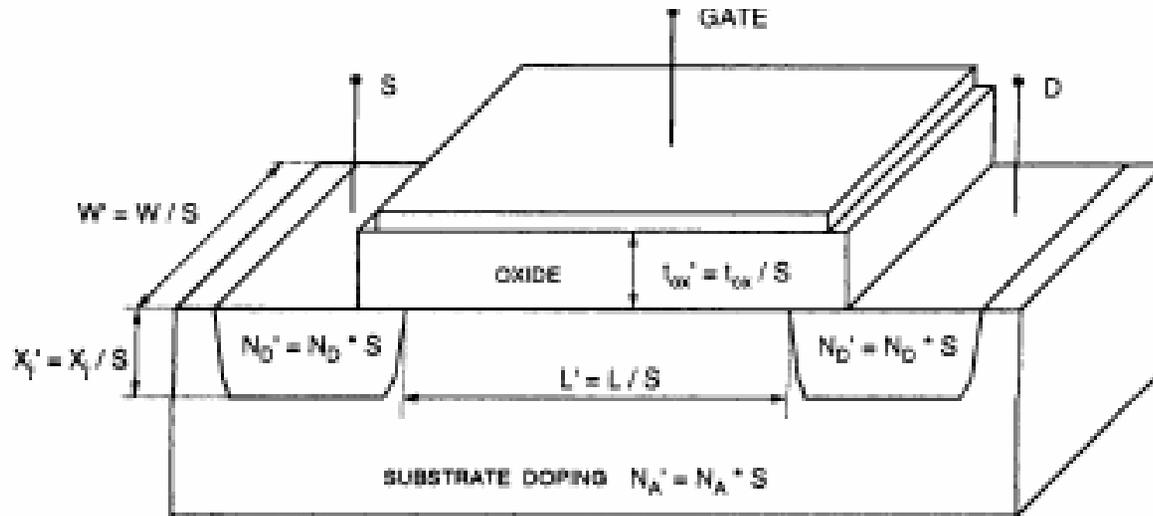
Two motivations to scale down

Faster transistors, both digital and analog

To pack more functionality per area.

Lower the cost!

**Full Scaling (Constant-Field Scaling)** (which makes **some** physical sense)



Scale all dimensions and voltages by the same factor, so the field does not change, and the device physics will be about the same. Makes sense at the first glance.

**Table 3.2** Full scaling of MOSFET dimensions, potentials, and doping densities

| Quantity             | Before scaling | After scaling            |
|----------------------|----------------|--------------------------|
| Channel length       | $L$            | $L' = L/S \quad (S > 1)$ |
| Channel width        | $W$            | $W' = W/S$               |
| Gate oxide thickness | $t_{ox}$       | $t'_{ox} = t_{ox}/S$     |
| Junction depth       | $x_j$          | $x'_j = x_j/S$           |
| Power supply voltage | $V_{DD}$       | $V'_{DD} = V_{DD}/S$     |
| Threshold voltage    | $V_{T0}$       | $V'_{T0} = V_{T0}/S$     |
| Doping densities     | $N_A$          | $N'_A = S \cdot N_A$     |
|                      | $N_D$          | $N'_D = S \cdot N_D$     |

Will talk about these later

Constant field  $\rightarrow$  constant current density  $\left. \begin{array}{l} \text{(A/cm)} \\ W' = W/S \end{array} \right\} \Rightarrow I_D' = I_D/S \quad (S > 1)$

$P = I_D \cdot V_{DS}$   
(holds for every instant)

$P' = I_D' \cdot V_{DS}' = \frac{1}{S^2} \cdot I_D \cdot V_{DS} = \frac{P}{S^2}$

Device resistance  $R = V/I$

Load capacitance  $C = C_{ox}WL$ .  $C' = C/S$  Why? And why not so true?

Switch delay time  $\tau \sim RC$ .  $\tau' = \tau/S$

$f_T \propto (V_G - V_{th})/L^2$  or  $f_T \propto v_{sat}/L$  How's  $f_T$  doing?

**Table 3.3** Effects of full scaling upon key device characteristics

| Quantity          | Before scaling | After scaling              |
|-------------------|----------------|----------------------------|
| Oxide capacitance | $C_{ox}$       | $C'_{ox} = S \cdot C_{ox}$ |
| Drain current     | $I_D$          | $I_D' = I_D/S$             |
| Power dissipation | $P$            | $P' = P/S^2$               |
| Power density     | $P/Area$       | $P'/Area' = P/Area$        |

## Constant-Voltage Scaling (to make some economic sense by being compatible)

**Table 3.4** Constant-voltage scaling of MOSFET dimensions, potentials, and doping densities

| Quantity         | Before scaling      | After scaling  |
|------------------|---------------------|--|
| Dimensions       | $W, L, t_{ox}, x_j$ | reduced by $S$ ( $W' = W/S, \dots$ )                 |
| Voltages         | $V_{DD}, V_T$       | remain unchanged                                     |
| Doping densities | $N_A, N_D$          | increased by $S^2$ ( $N'_A = S^2 \cdot N_A, \dots$ ) |

( $S > 1$ )

**Table 3.5** Effects of constant-voltage scaling upon key device characteristics

| Quantity          | Before scaling | After scaling                   |
|-------------------|----------------|---------------------------------|
| Oxide capacitance | $C_{ox}$       | $C'_{ox} = S \cdot C_{ox}$      |
| Drain current     | $I_D$          | $I'_D = S \cdot I_D$            |
| Power dissipation | $P$            | $P' = S \cdot P$                |
| Power density     | $P/Area$       | $P'/Area' = S^3 \cdot (P/Area)$ |

Switching delay time

$1/S^2$

# Moore's Law

- Gordon E. Moore (born 1929), a co-founder of Intel
- Moore's Law is the **empirical observation** made in 1965 that the number of transistors on an integrated circuit **for minimum component cost** doubles every 24 months (sometimes quoted as 18 months).
- Moore's law is not about just the density of transistors that can be achieved, but about the density of transistors at which the cost per transistor is the lowest.

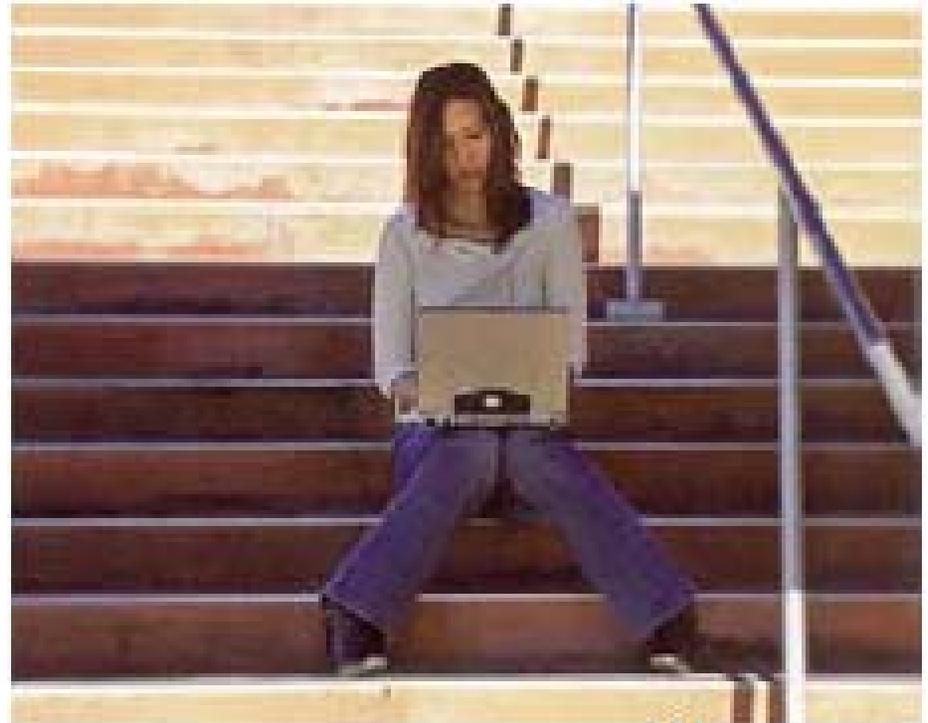
## Why Small (if they are already so small that we can't make them better)?

- To pack more functionality into each unit area
  - With feature size shrinking and wafer size growing, more and better products each wafer – better economics



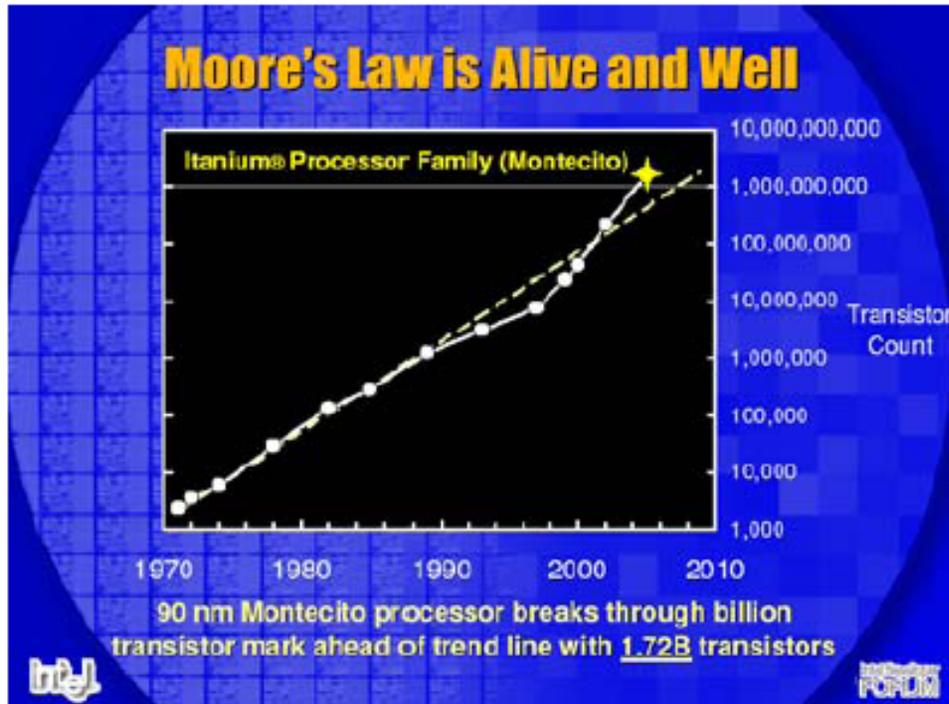
Transistor radio!

1965: \$1/transistor



2006: 1 "microdolar"/transistor

# Moore's Law is Alive and Well

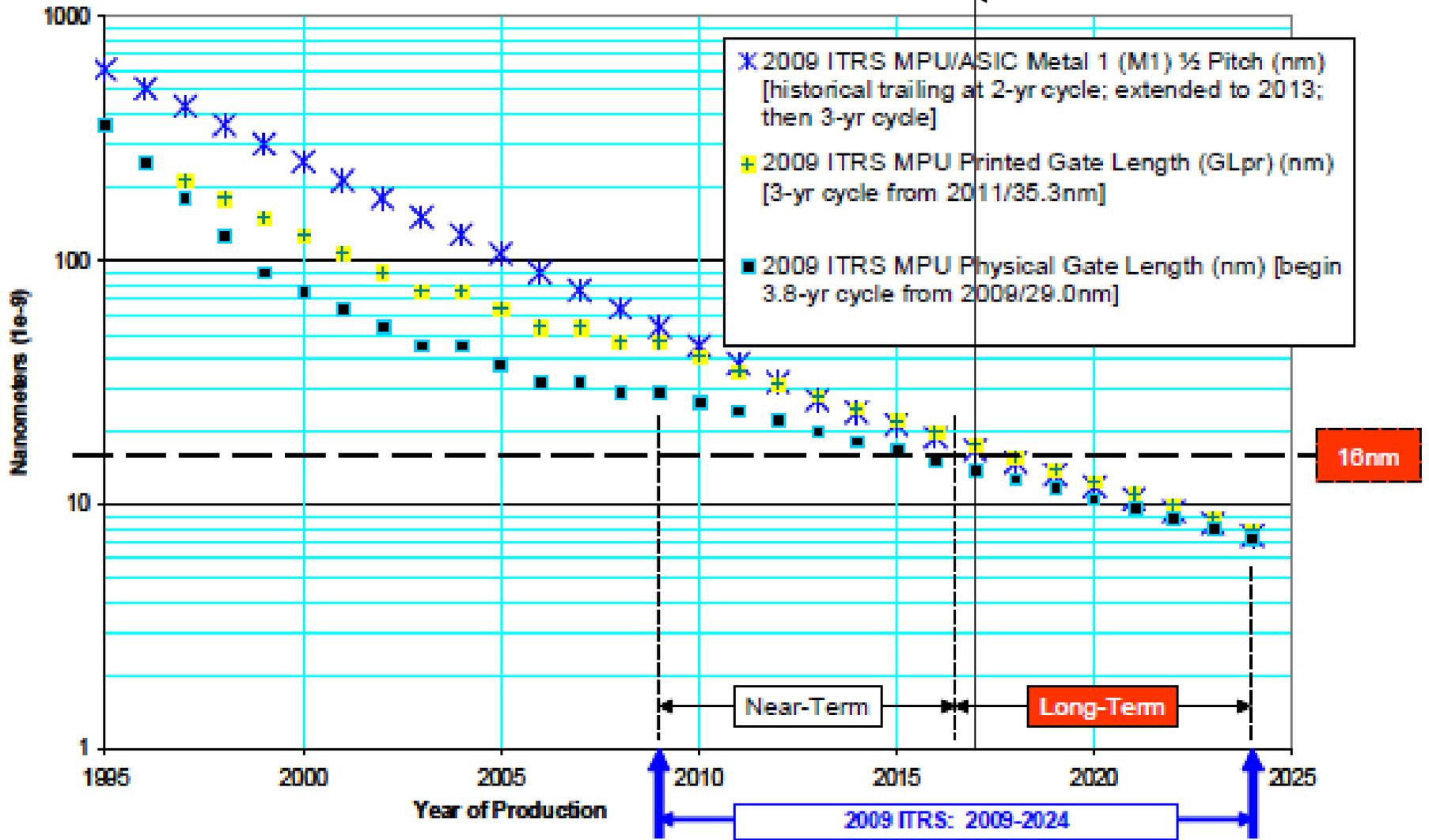


Source: M. Bohr, Intel Development Forum, September 2004.



**2009 ITRS - Technology Trends**

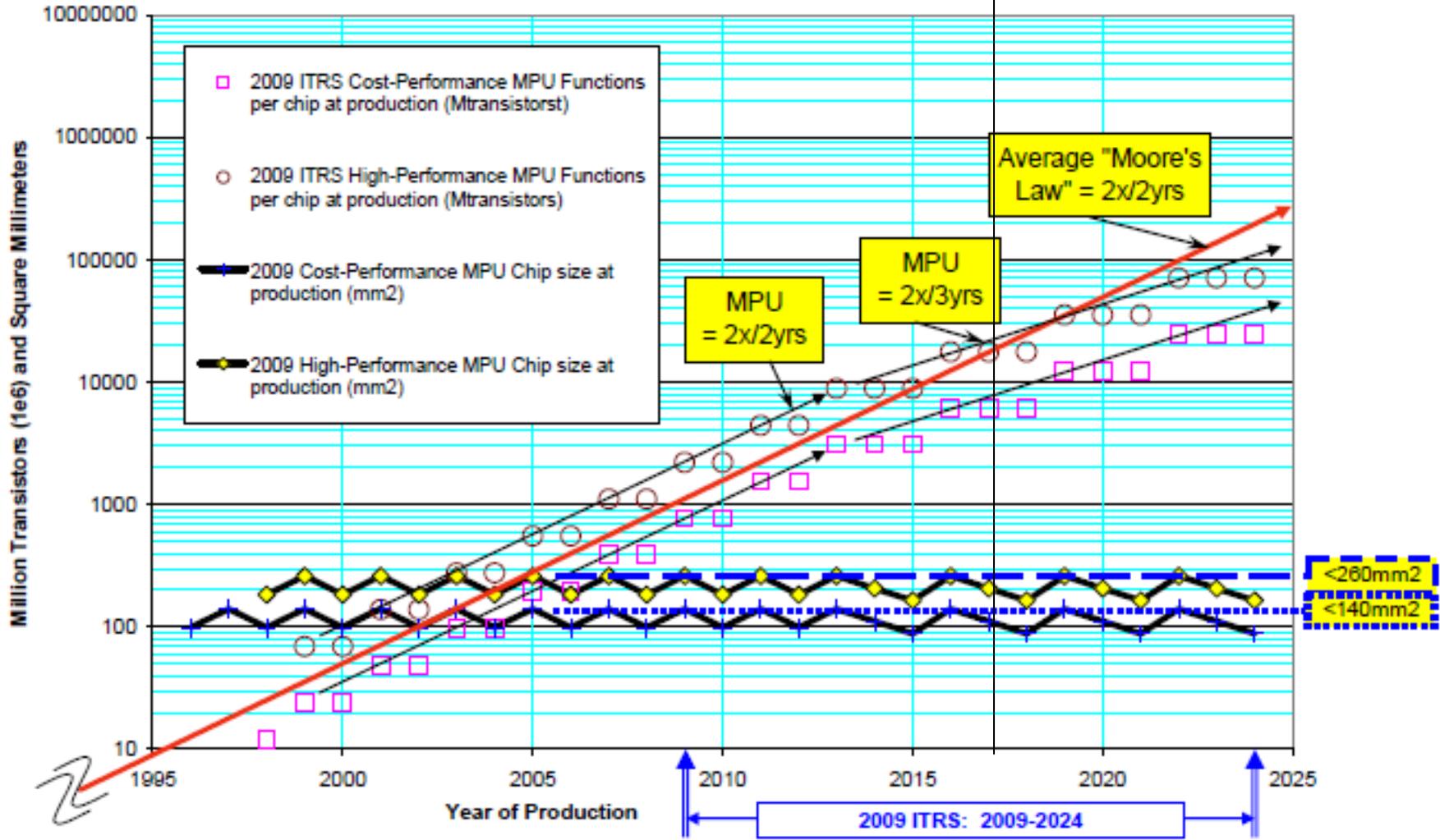
2017, ~10 nm



With 10 nm feature size, we are near the end of the road...

2009 ITRS - Functions/chip and Chip Size

2017, 10 nm,  
> 10<sup>9</sup> transistors

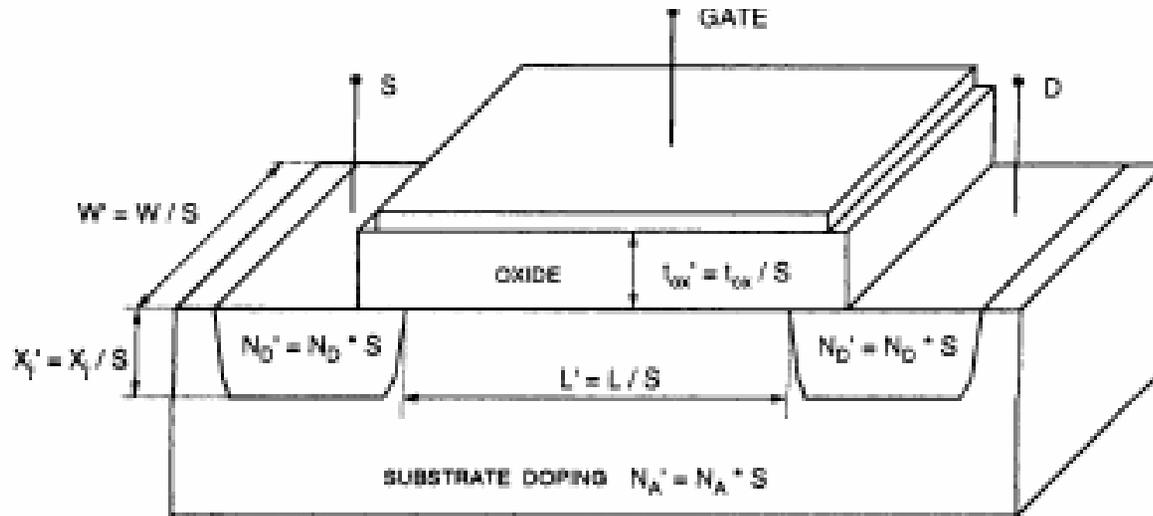


# Can Moore's Law Go On Forever?

- People have had doubts for many years
- But so far so good (?)
- In the past, the doubts were more about processing limits than physics limits
- Processing limits have been overcome  
And probably will continue to be overcome
- Are we hitting the physics limits?

Before we look at the physics limits and alternative materials/devices, let's look at issues with CMOS scaling and new CMOS structures that currently let CMOS get by.

**Full Scaling (Constant-Field Scaling)** (which makes (some) physical sense)



Scale all dimensions and voltages by the same factor, so the field does not change, and the device physics will be about the same. Makes sense at the first glance.

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| Doping densities     | $N_A$          | $N'_A = S \cdot N_A$   |
|                      | $N_D$          | $N'_D = S \cdot N_D$   |

Now we talk about these

Constant field  $\rightarrow$  constant current density  $\left. \begin{array}{l} \text{(A/cm)} \\ W' = W/S \end{array} \right\} \Rightarrow I_D' = I_D/S$

But we did not say why. Let's now have a closer look.

Areal carrier charge density in channel  $qn = \epsilon E_{ox} \Rightarrow n = n'$   
e's per area

$J_s = \mu q n E_{lateral}$   
A/cm

$\frac{\cancel{\text{cm}^2}}{\cancel{\text{Vs}}} \frac{\text{C}}{\cancel{\text{cm}^2}} \frac{\cancel{\text{V}}}{\text{cm}} = \text{A/cm}$

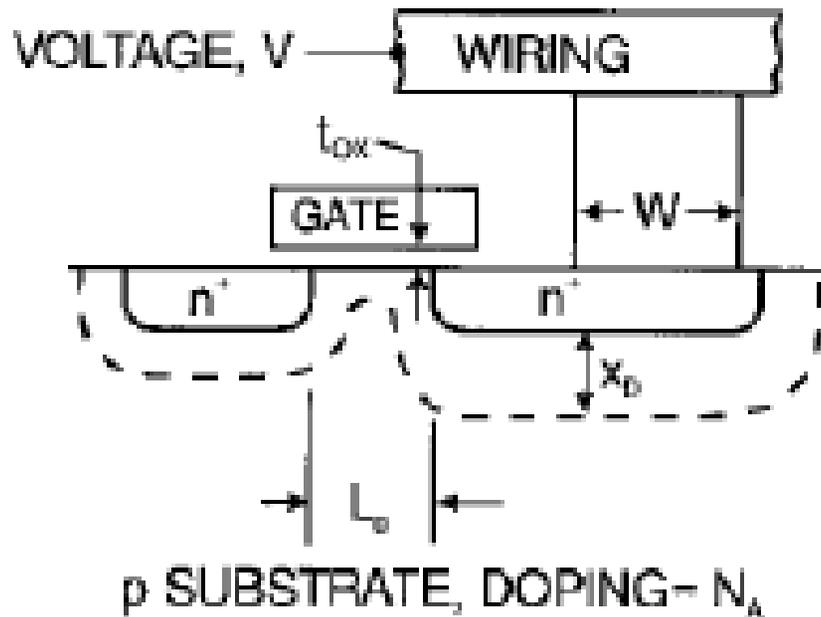
$I_D = J_s W \Rightarrow I_D' = I_D/S$

if we truly have constant field

$$\alpha = S$$

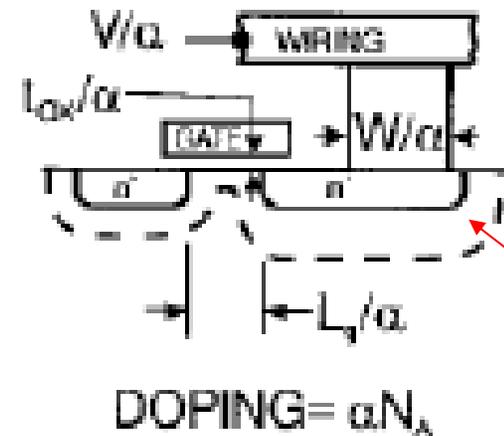
Simple constant-field scaling:  $V \rightarrow \alpha V, I \rightarrow \alpha I$

### ORIGINAL DEVICE



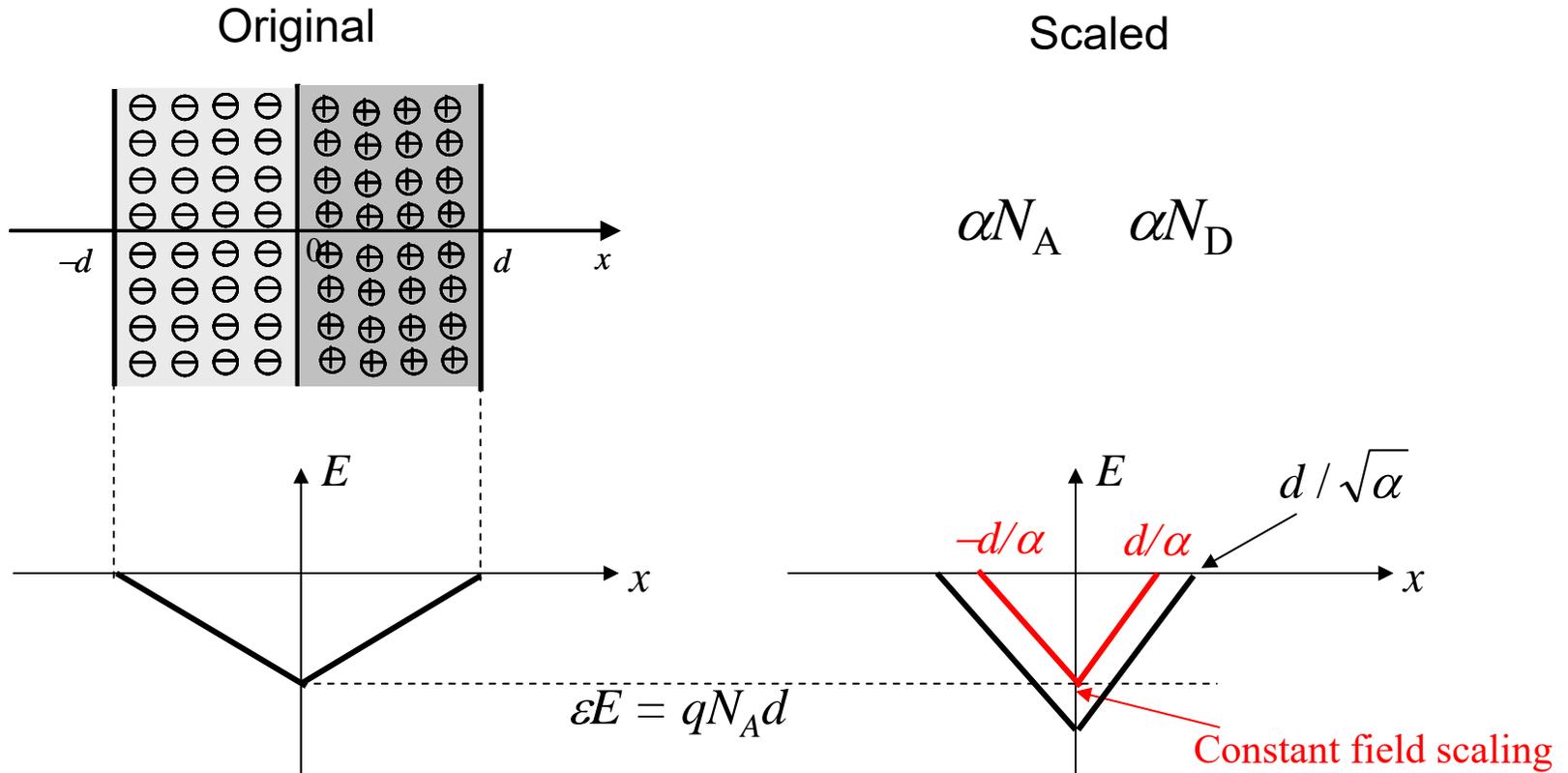
### SCALED DEVICE

$$\alpha > 1$$



Justified?

Consider a simple pn junction within the depletion approximation  
 (keep in mind the S/D junctions & the depletion under the channel)

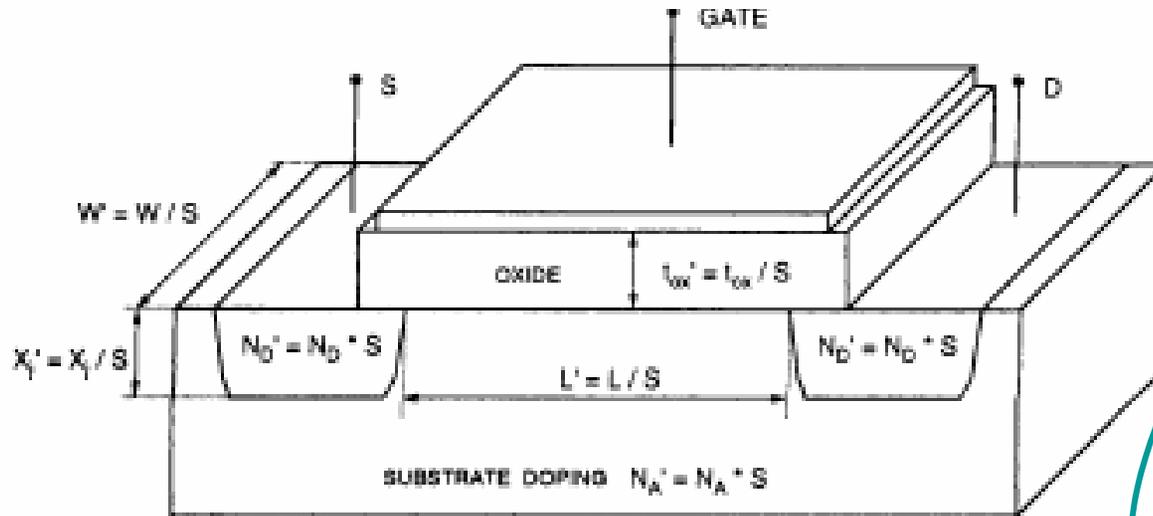


The integral of the field is the built-in potential.

But the built-in voltage is largely determined by the band gap..., not much changed in the scaled junction

Think graphically about E, potential, and the band diagram

**Full Scaling (Constant-Field Scaling)** (which makes **some** physical sense)



$$x_d \propto \ln(N_D N_A / n_i^2) / \sqrt{N_A}$$

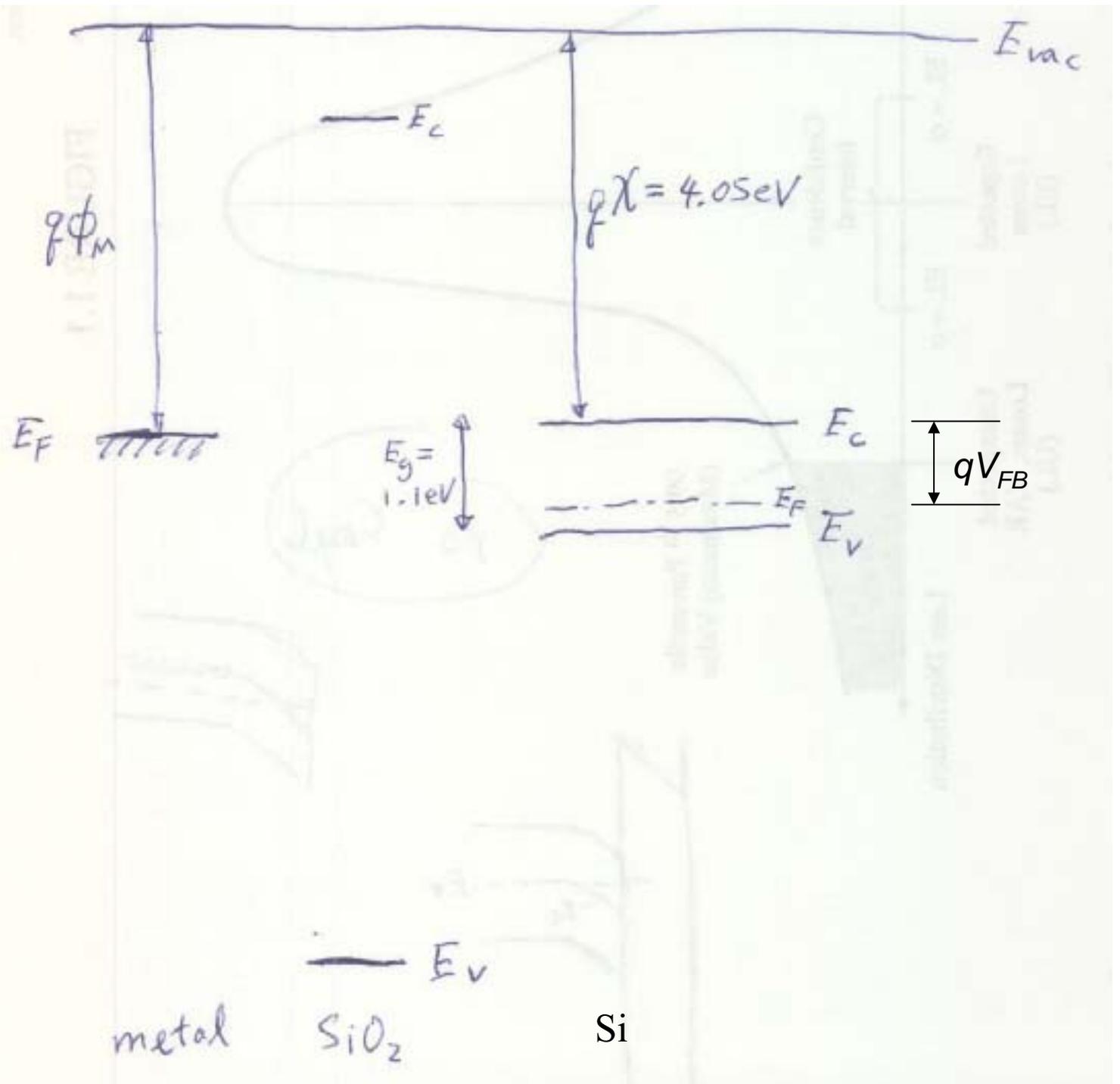
$$V_{th} = V_{FB} + 2\phi_p + \frac{\sqrt{2\epsilon q N_A (2\phi_p)}}{C_{ox}}$$

Doesn't scale.  
Need  $V_{th}$  adjustment.

**Table 3.2** Full scaling of MOSFET dimensions, potentials, and doping densities

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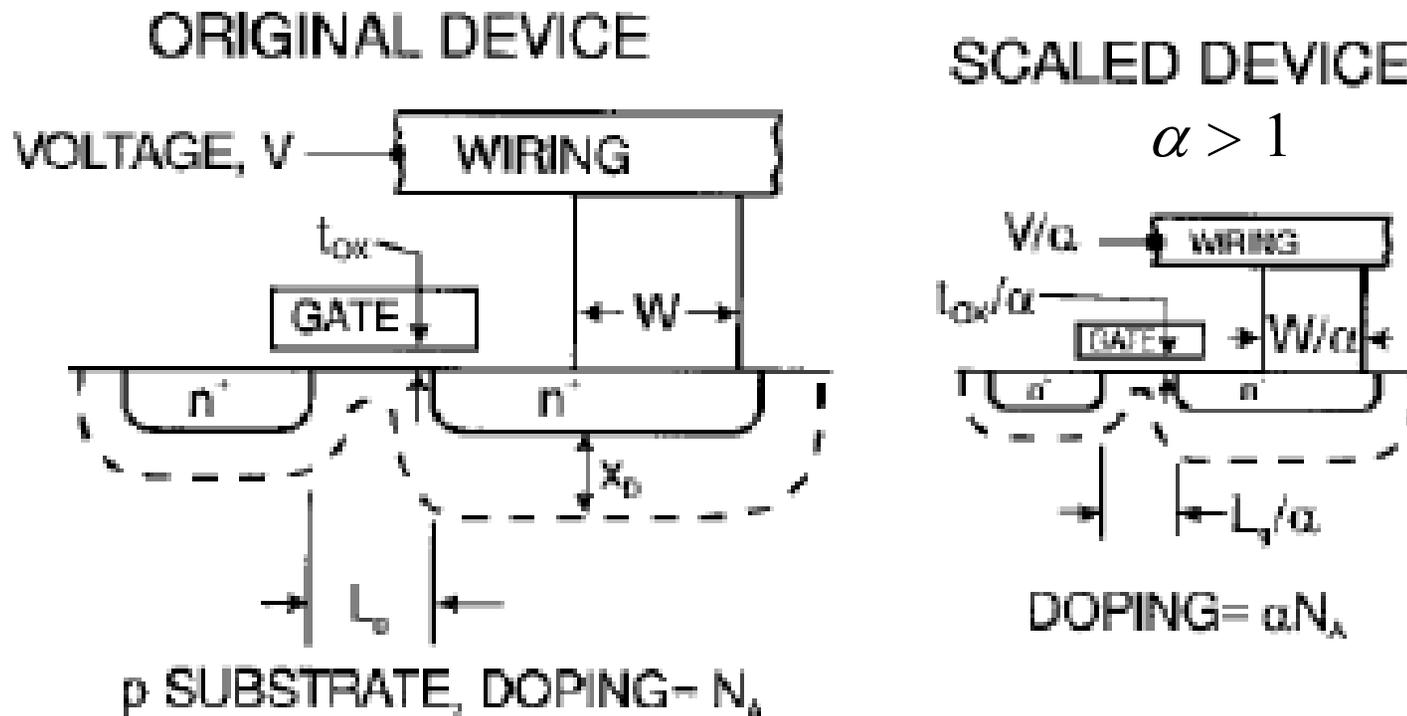
Not exactly



Work out the details of constant-voltage scaling offline

The happy (even with the mess) scaling days are long gone.  
 There are many issues with scaling... Among them, electrostatic control.  
 (We are not going to talk about all of them.)

Simple constant-field scaling:  $V \rightarrow \alpha V, I \rightarrow \alpha I$



But the wafer is still “infinitely thick”...

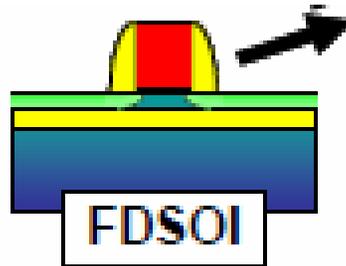
| $L_g$  | $t_{ox}$ |
|--------|----------|
| 800 nm | 18 nm    |
| 20 nm  | 0.45 nm  |

The Si-O bond length in  $\text{SiO}_2$  is 0.16 nm

Thicker high-k dielectric can be used, but...

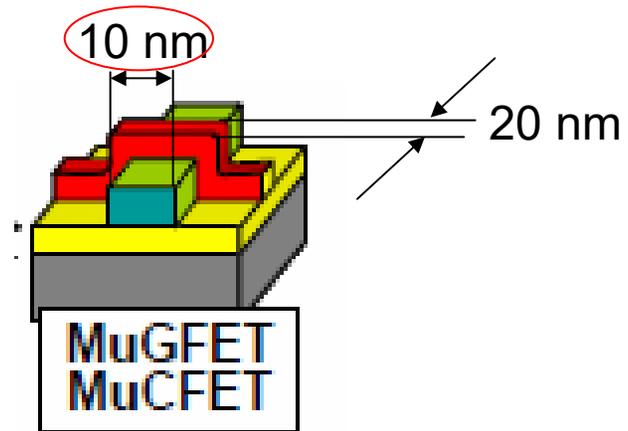
For good electrostatic control, we really need to get rid of the body (bulk)

Solutions (for now)



For  $L = 20$  nm,  
the Si needs to be  
thinner than 5 nm.

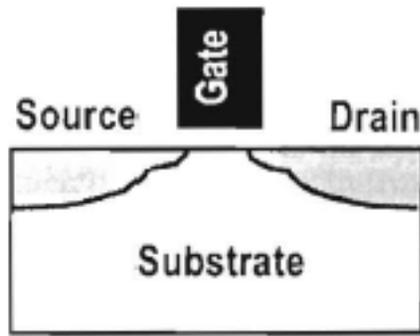
Ultra-thin body silicon-on-insulator



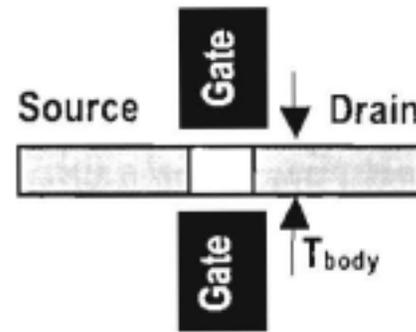
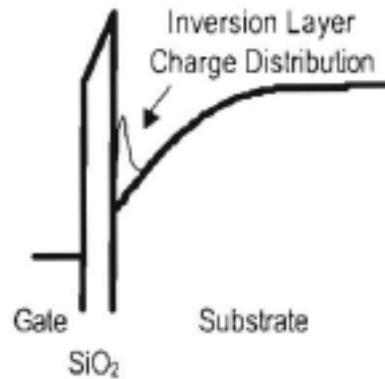
FinFET, 3D FET

Further reading: "Transistor Wars," IEEE spectrum, November 2011

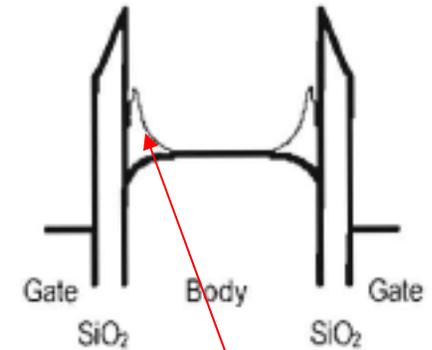
<http://spectrum.ieee.org/semiconductors/devices/transistor-wars>



a) Bulk MOSFET



b) Double-Gate MOSFET

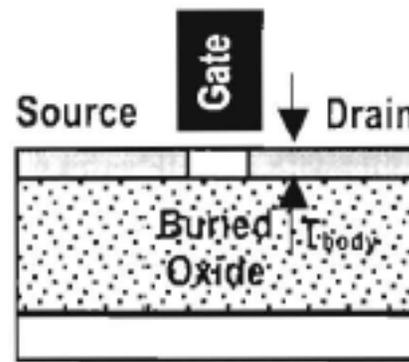


Carrier density

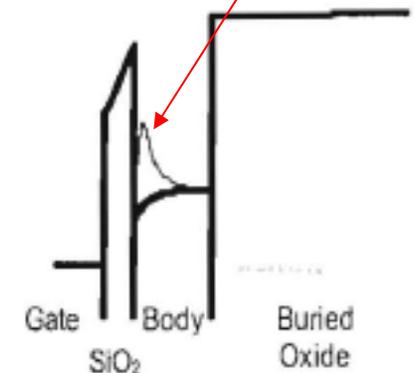
Deplete and then invert.

The bulk is a path for leakage.

Will need very high  $N_A$  for the substrate, to scale down the  $x_d$  of the S/D junctions, as well as the  $x_{dmax}$  of the FET channel. This will cause high S-to-D leakage.



c) Ultra-Thin Body MOSFET



Thin bodies don't have to be doped.

→ No need for depletion

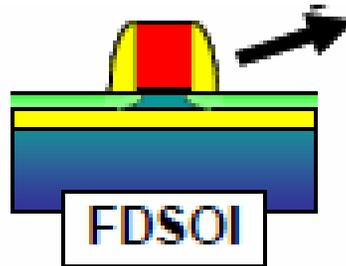
→ Lower vertical fields

Why is SOI a challenge?

[http://en.wikipedia.org/wiki/Silicon\\_on\\_Insulator](http://en.wikipedia.org/wiki/Silicon_on_Insulator)

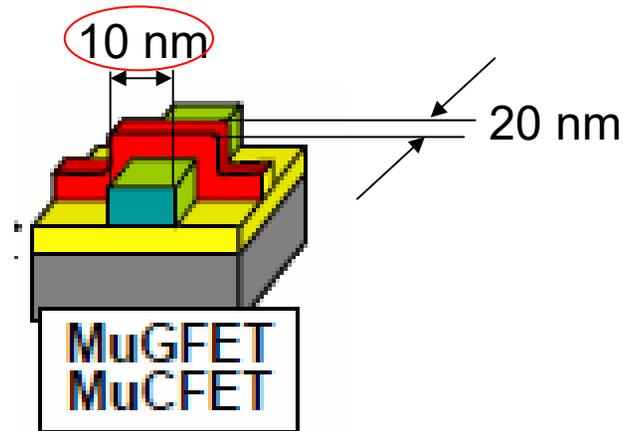
For good electrostatic control, we really need to get rid of the body (bulk)

Solutions (for now)



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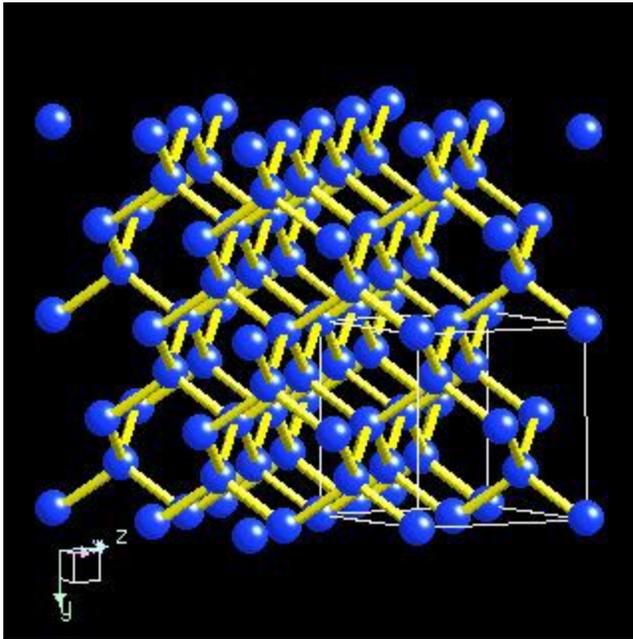
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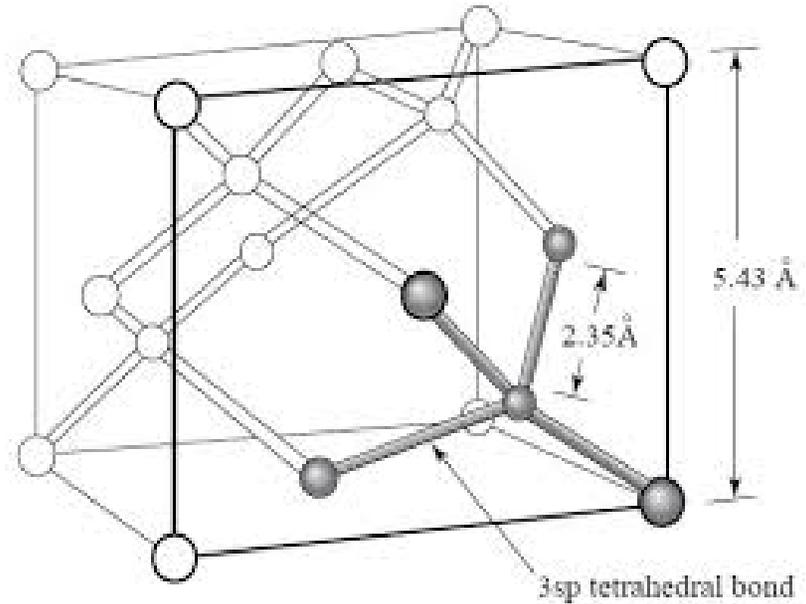
FinFET, 3D FET

Besides technical challenges,  
any issues with making the fin  
thinner?

# Crystal structure of Si

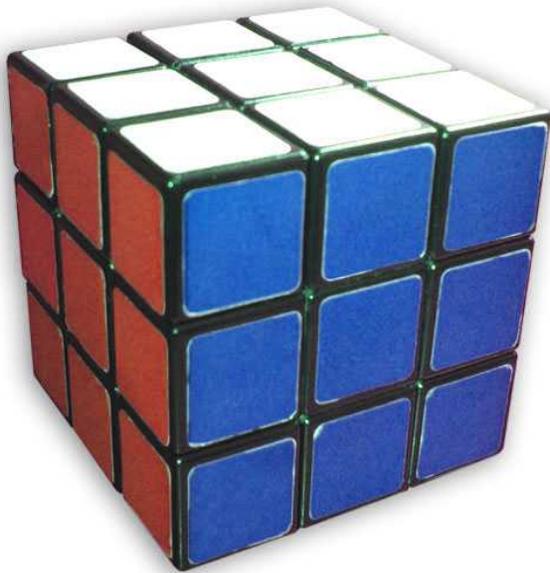


[http://www.webelements.com/silicon/crystal\\_structure.html](http://www.webelements.com/silicon/crystal_structure.html)



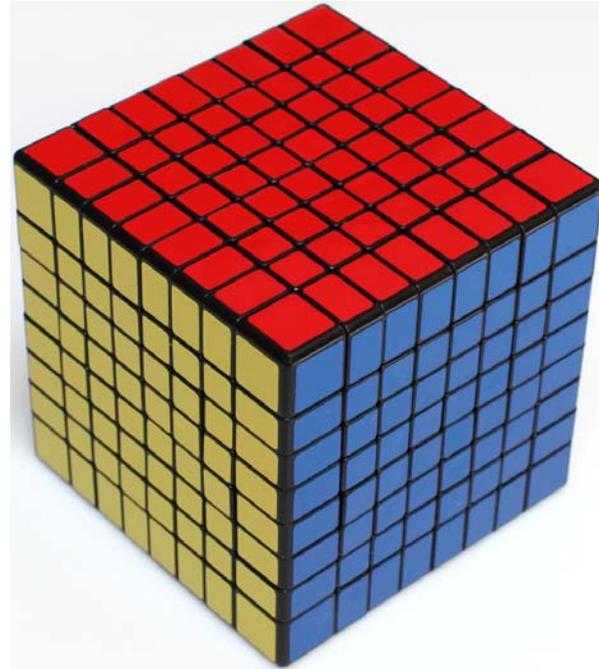
<http://onlineheavytheory.net/silicon.html>

If several monolayers thin, is Si still the Si as we know it?



$$3^3 = 27$$

$$(3-2)^3 = 1$$



$$10^3 = 1000$$

$$(10-2)^3 = 512$$

Half of the small cubes are on the surface!

# Can Moore's Law Go On Forever?

- People have had doubts for many years
- But so far so good (?)
- In the past, the doubts were more about processing limits than physics limits
- Processing limits have been overcome  
And probably will continue to be overcome
- Are we hitting the physics limits?

Forget about details.

The crystal constant of Si is 0.54 nm.

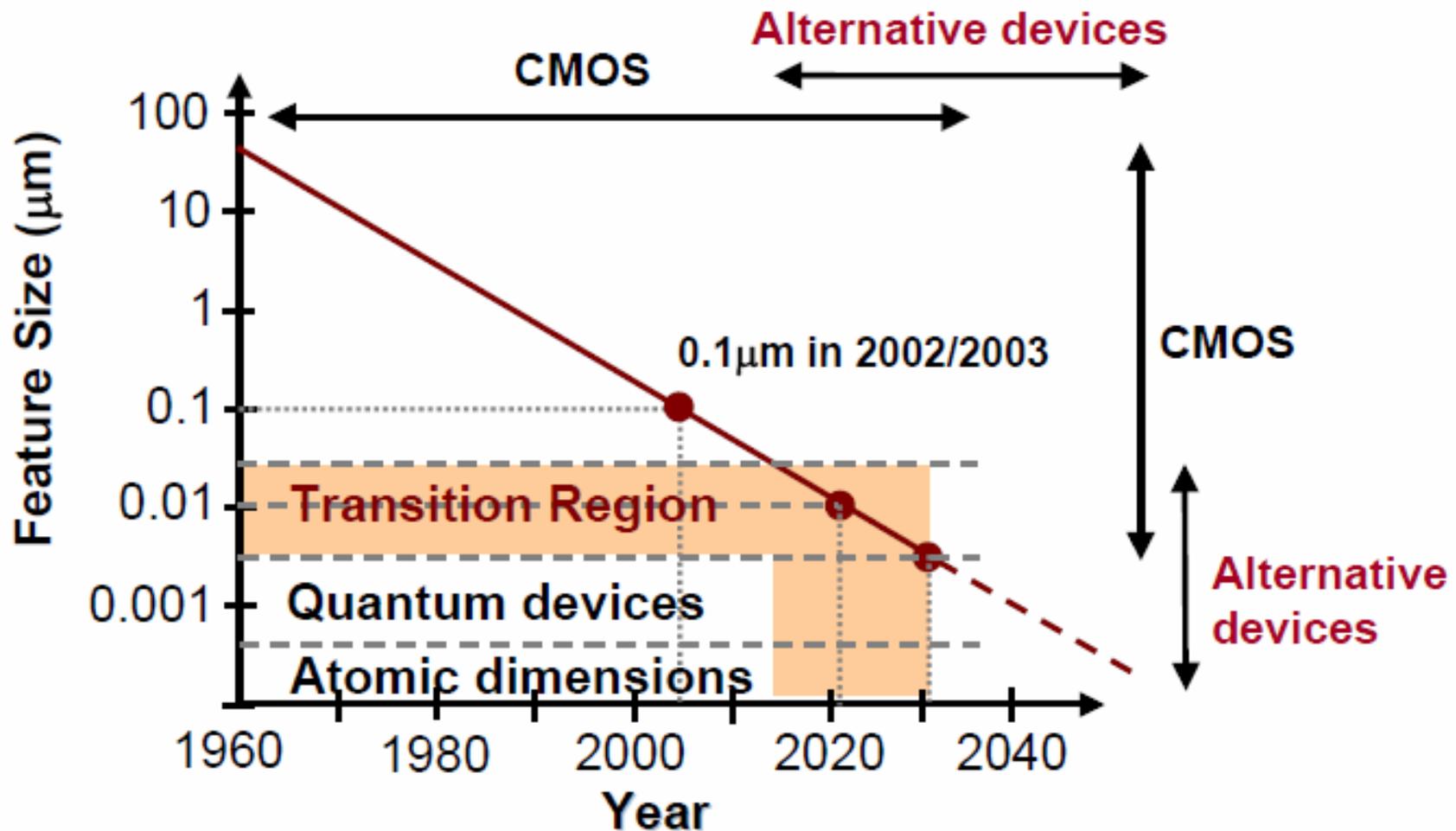
Fundamental scaling limit: 10 nm wall?

10 nm is only ~19 crystal constants!

Do the (semi-classical) semiconductor physics theories we rely on still work?

Are there alternatives to scaling to achieve faster devices?

# Nano-reality: CMOS IC evolution

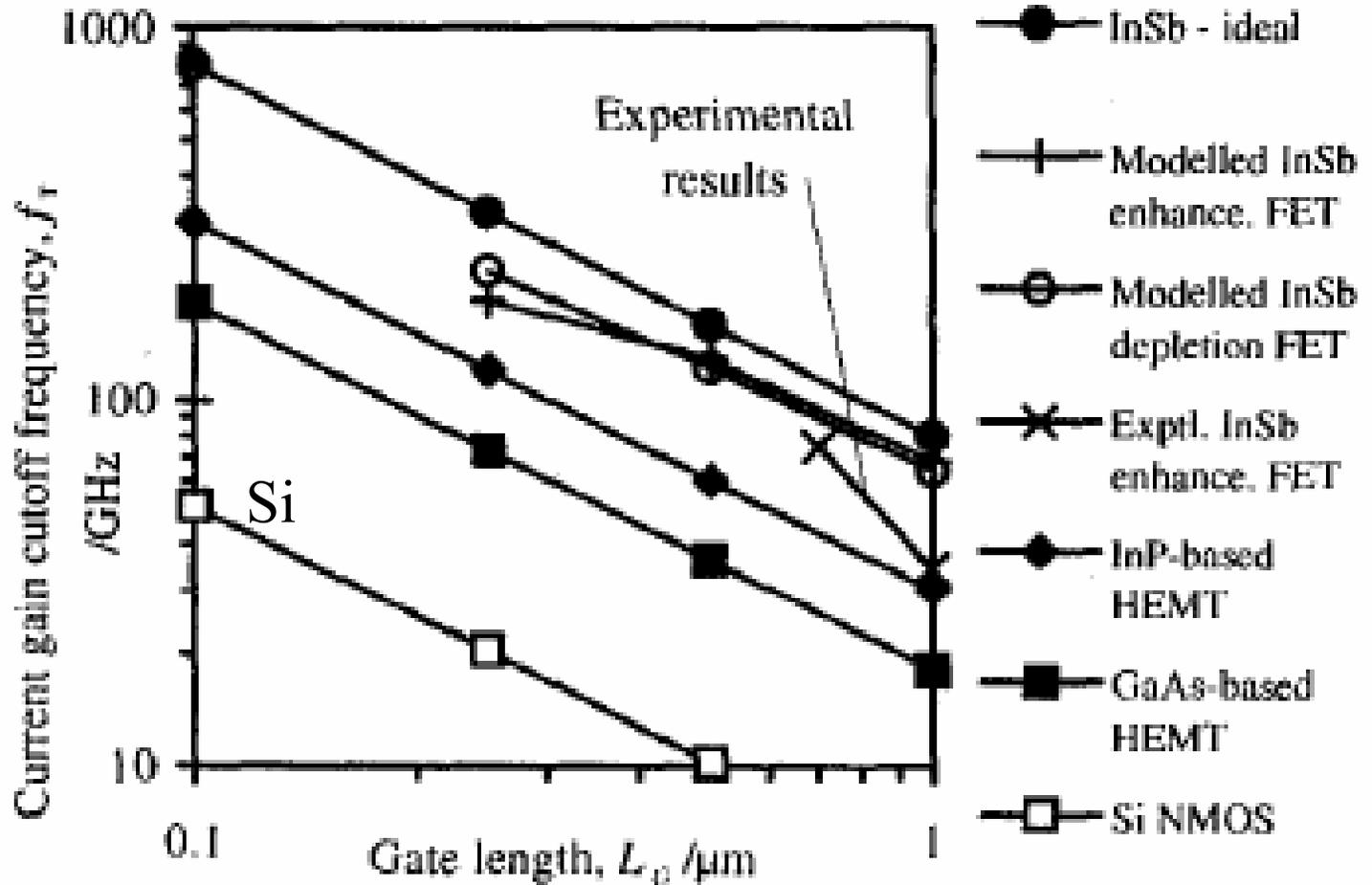


*Adapted from J.D. Plummer, Proceedings of IEEE, 2001.*

One alternative is semiconductors in which electrons travel faster.  
 (If our goal were only to make the device faster.)

But economics is in the driver's seat...

$$f_T = v_{sat} / (2\pi L)$$

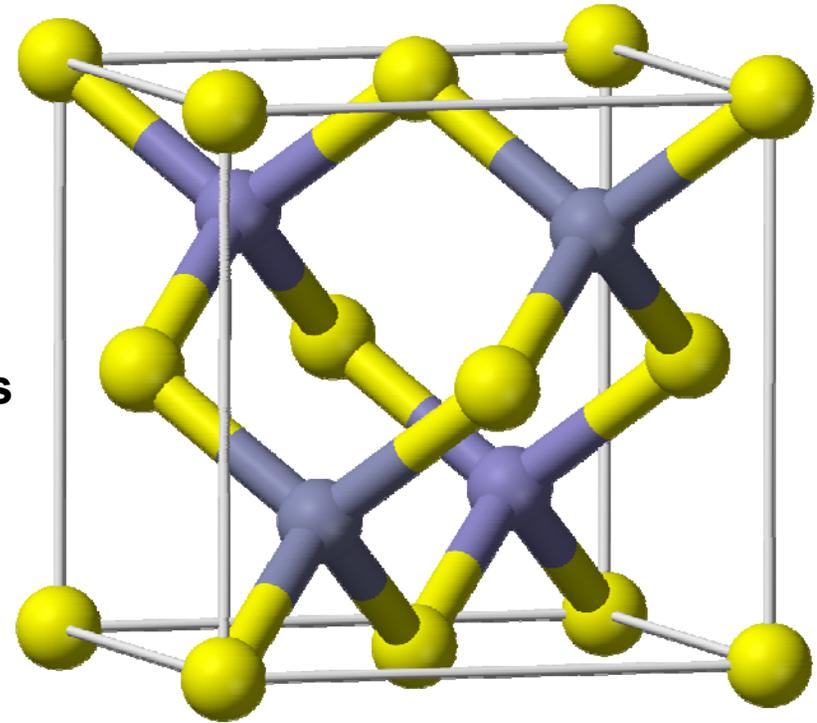
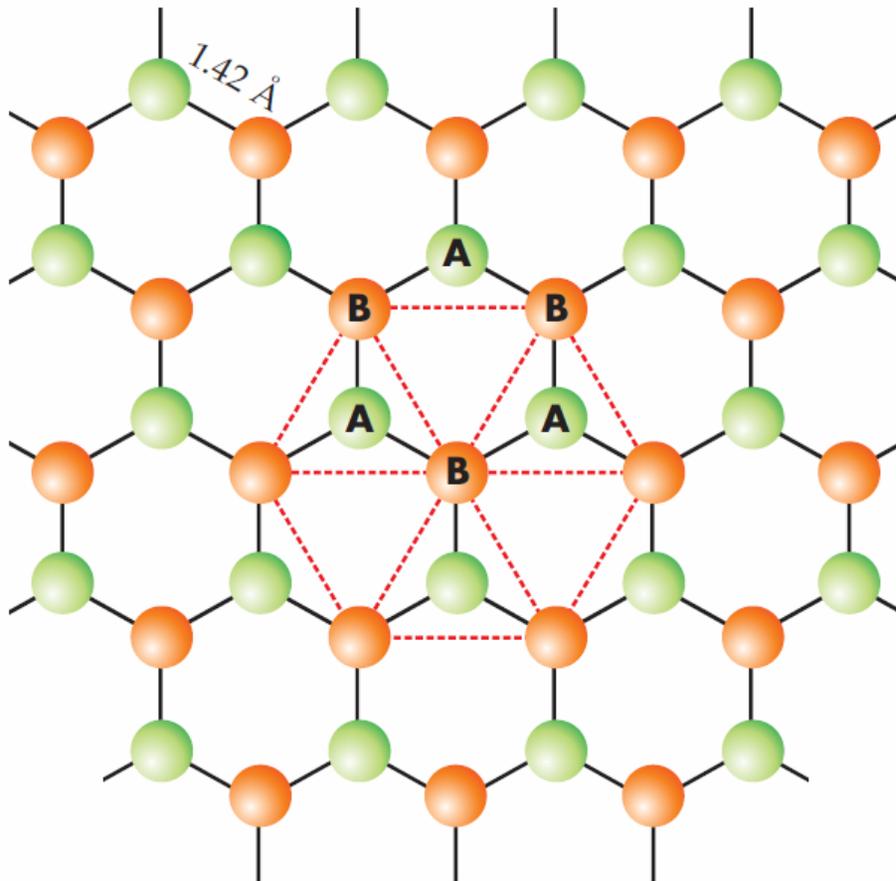


Ashley *et al*, IEEE IEDL '97, 751 (1997).

Reading: Ye, III-V MOSFETs (posted on course website).

How thin can Si (or any 3D stuff) go?  
For a 3D material, if we make it a few atoms thin, it's no longer that material as we know it!  
(Recall that 10X10X10 cube)

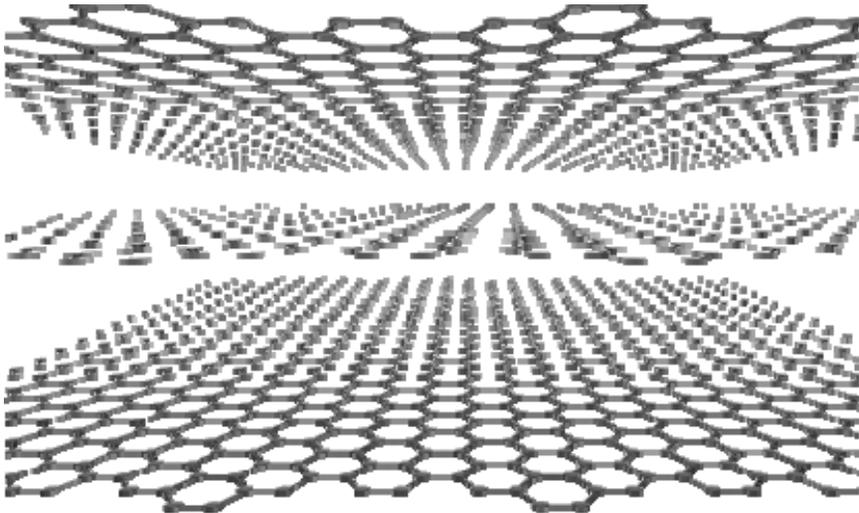
### The need for lower dimensional materials



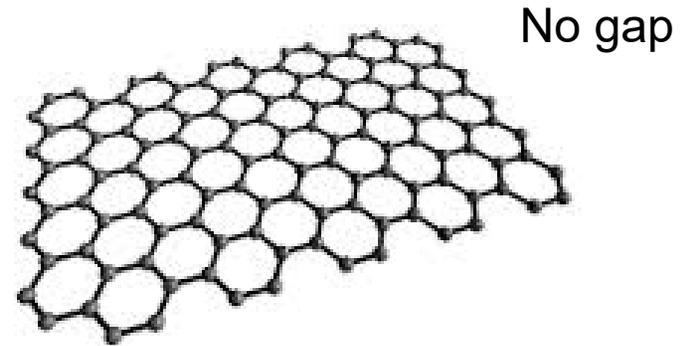
Graphene is 2D.  
It's 1-atom thin by nature.  
The "ultimate SOI" if we put it on an insulator.

If it ever (?) becomes the post-Si semiconductor, its 2D nature (actually, we may need to turn it into 1D) probably deserves more kudos than its fast moving electrons.

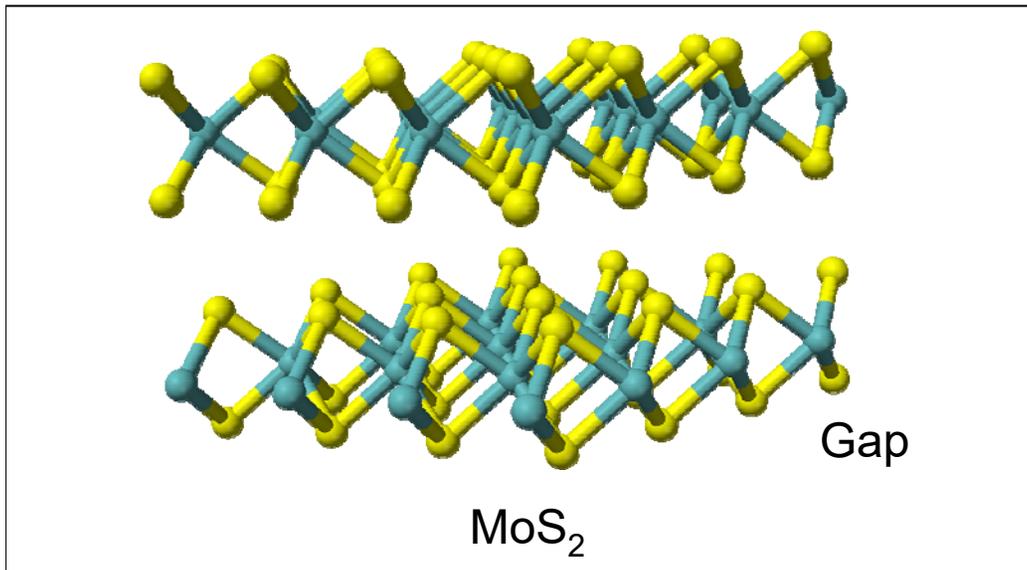
At the end of the road, we look for alternatives.  
We want things that are inherently low dimensional (2D or 1D)



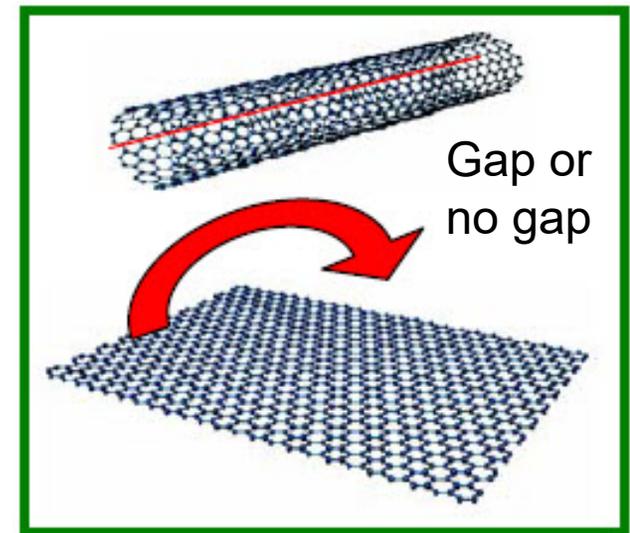
Graphite: 3D but layered (w/ van der Waals gaps)



Graphene: 2D



MoS<sub>2</sub>



Carbon nanotube: (quasi-)1D

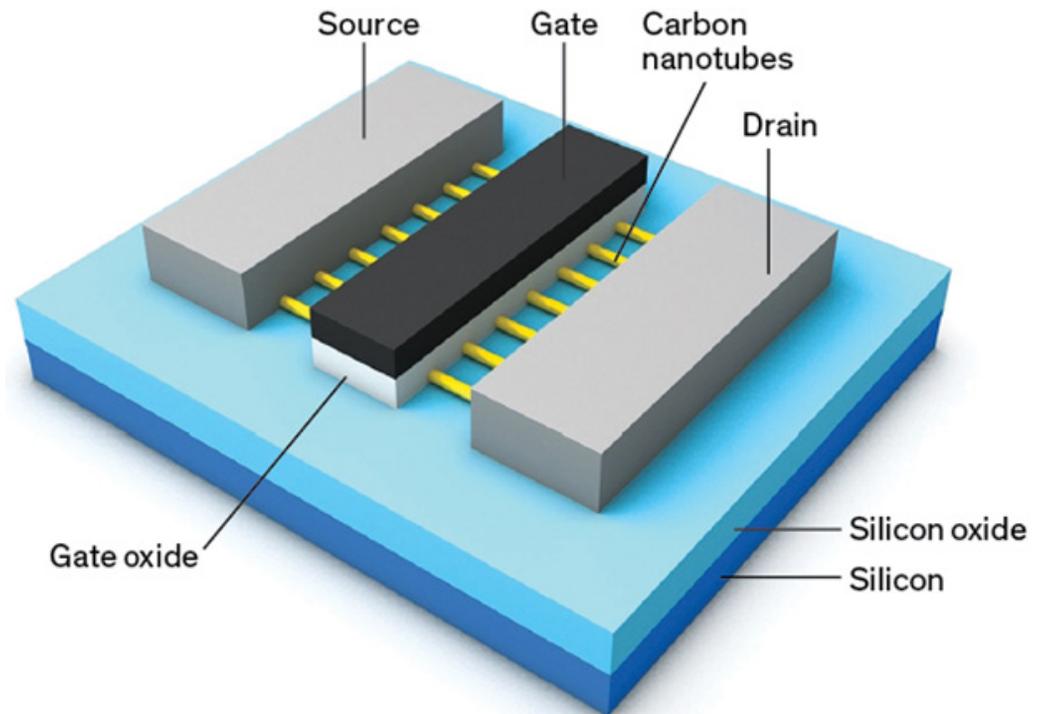
Carbon nanotube FETs are considered promising.

1D. Good electrostatic control.

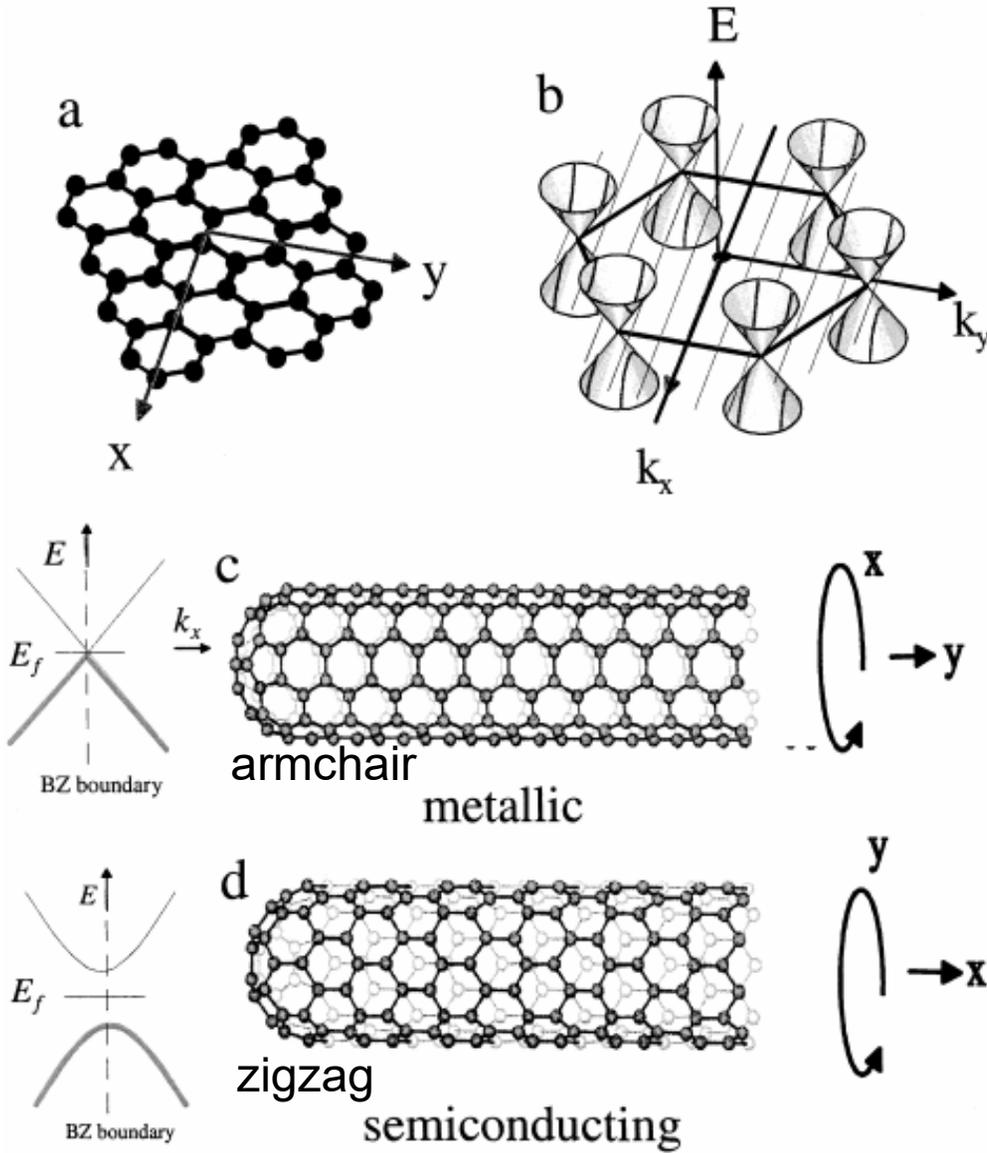
Challenges:

To achieve uniform diameter and chirality (for uniform band gap)

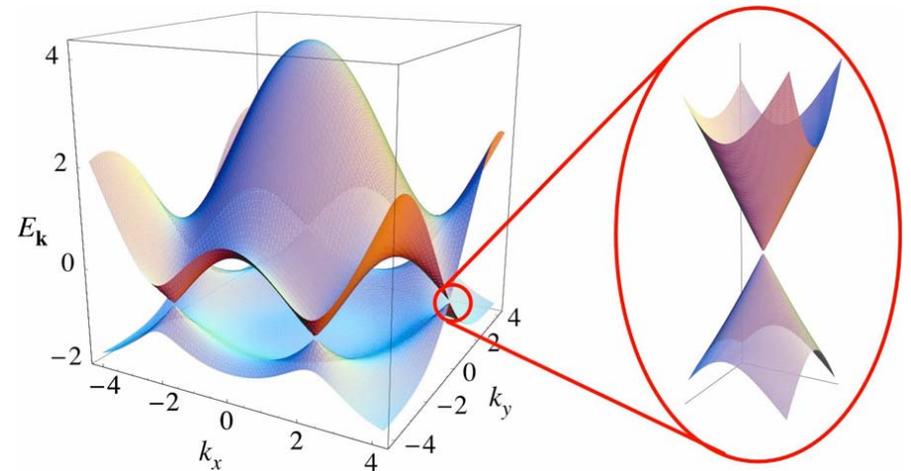
To place them into a dense, parallel array



# Band structures of single-wall carbon nanotubes



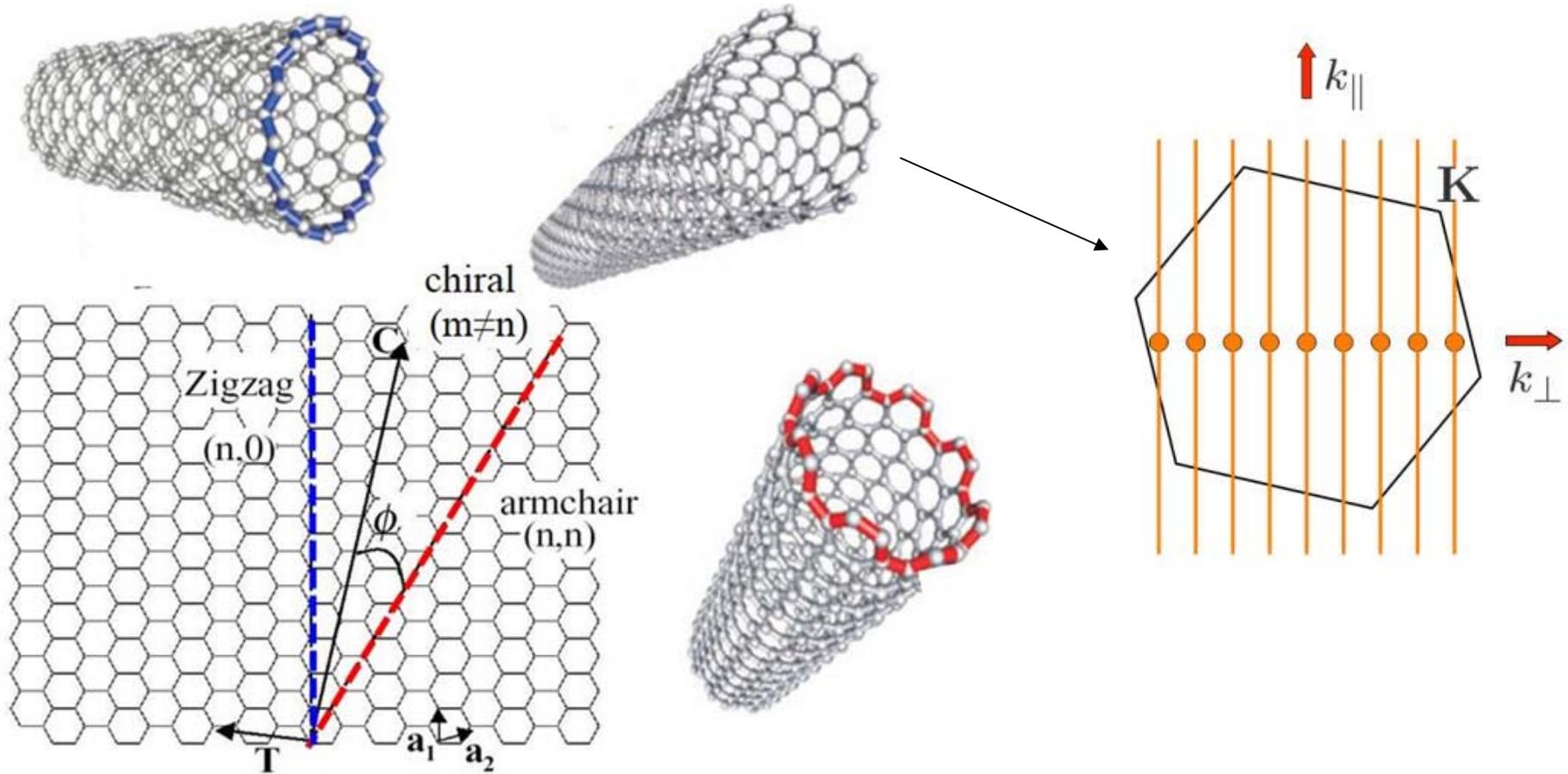
## Band structure of graphene



<http://exciting-code.org/carbon-graphene-from-the-ground-state-to-excitations>

Simple theory to construct nanotube  
 band structure:  
 Quantizing  $k$

# Carbon nanotube indexing



<https://www.frontiersin.org/articles/10.3389/fchem.2015.00059/full>

## Simple theory (not exact):

$n - m = \text{multiple of } 3 \rightarrow \text{metallic}$   
 Therefore, armchair  $(n,n)$  always metallic,  
 zigzag  $(n,0)$  metallic when  $n = \text{multiple of } 3$ ,  
 semiconducting otherwise.

Now you see how challenge it is to get all tubes to have the same bandwidth

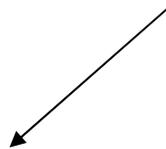
Happy scaling (long ago)



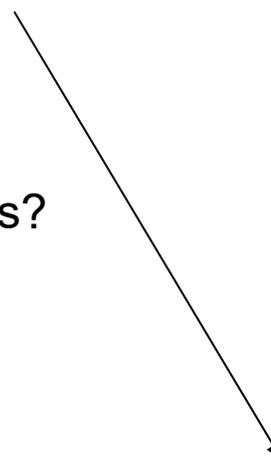
Scaling driven by density, cost



New Si MOS structures: FinFETs, SOI (solutions for now)



Alternative 3D semiconductors for MOSFETs?  
(Higher materials performance so we don't  
have to scale so aggressively)



Low dimensional semiconductors for MOSFETs?  
(Inherently provide better electrostatic control)

**Alternative devices, architectures, systems???**

## Invitation To Enter the NANO-World: Information on a small scale



There's Plenty of Room at the Bottom  
An Invitation to Enter a New Field of Physics  
*by Richard P. Feynman*  
*December 29<sup>th</sup>, 1959*



Why cannot we write the entire 24 volumes of the  
Encyclopedia Britannica on the head of a pin?

A future filled with tiny, molecule-sized computers-fast and  
powerful enough to do things like translate conversations on the  
fly or calculate complex climate models-may be closer than  
people think...

*American Association for the Advancement of Science (AAAS),  
Annual Meeting (Boston, February, 2002)*

## Emerging Nanoelectronics: what is expected from **beyond CMOS** technologies?

- Easier and cheaper to manufacture than CMOS:
  - *very low cost (<1µcent /transistor)* ?
- Need high current drive:
  - *able to drive capacitances of interconnects of any length* ?
- High level of integration:
  - *more than  $10^{10}$  transistors/circuit*
- High reproducibility
  - *better than  $\pm 5\%$*  ?
- Reliability
  - *operating time > 10 years*
- Better heat dissipation & lower power density

**Simultaneously further CMOS scaling must become difficult and not cost-effective!**

*M. Meyyappan, Center for Nanotechnology  
NASA Ames Research Center*