

Genetic Algorithms

- Developed by John Holland in '60s
- Did not become popular until late '80s
- A simplified model of genetics and evolution by natural selection
- Most widely applied to optimization problems (maximize "fitness")

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Assumptions

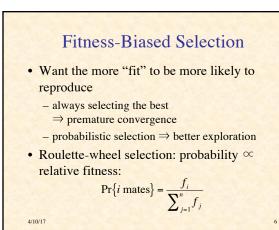
- Existence of fitness function to quantify merit of potential solutions
 - This "fitness" is what the GA will maximize
- A mapping from bit-strings to potential solutions
 - best if each possible string generates a legal potential solution
 - choice of mapping is important
 - can use strings over other finite alphabets

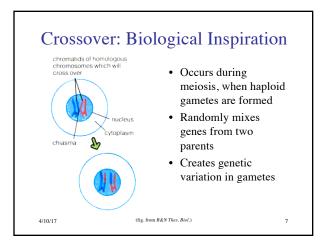
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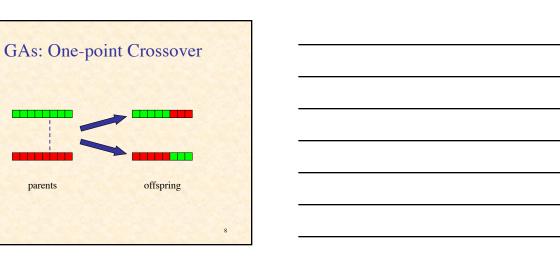
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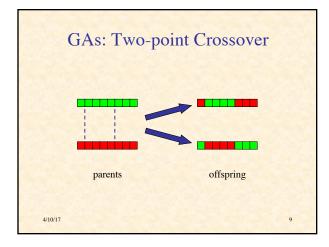
Outline of Simplified GA

- 1. Random initial population P(0)
- 2. Repeat for $t = 0, ..., t_{max}$ or until converges:
 - a) create empty population P(t + 1)
 - b) repeat until P(t + 1) is full:
 - 1) select two individuals from P(t) based on fitness
 - 2) optionally mate & replace with offspring
 - 3) optionally mutate offspring
 - 4) add two individuals to P(t + 1)





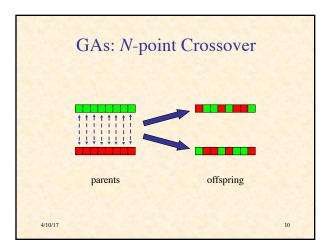




offspring

parents



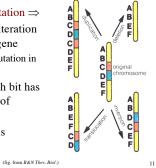




Mutation: Biological Inspiration

- Chromosome mutation \Rightarrow
- Gene mutation: alteration
 of the DNA in a gene
 inspiration for mutation in
 GAs
- In typical GA each bit has a low probability of changing
- Some GAs models rearrange bits

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The Red Queen Hypothesis



"Now, here, you see, it takes all the running you can do, to keep in the same place." — Through the Looking-Glass and What Alice Found There

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- *Observation*: a species probability of extinction is independent of time it has existed
- *Hypothesis*: species continually adapt to each other
- Extinction occurs with insufficient variability for further adaptation

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Demonstration of GA: Finding Maximum of Fitness Landscape

<u>Run Genetic Algorithms — An Intuitive</u> <u>Introduction</u> <u>by Pascal Glauser</u> <www.glauserweb.ch/gentore.htm>

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Demonstration of GA: Evolving to Generate a Pre-specified Shape (Phenotype)

<u>Run Genetic Algorithm Viewer</u> <www.rennard.org/alife/english/gavgb.html>

> Demonstration of GA: Eaters Seeking Food

http://math.hws.edu/eck/js/genetic-algorithm/GA.html

Morphology Project by Michael "Flux" Chang

- Senior Independent Study project at UCLA – users.design.ucla.edu/~mflux/morphology
- Researched and programmed in 10 weeks

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Programmed in Processing language
 www.processing.org

Genotype \Rightarrow Phenotype

- Cells are "grown," not specified individually
- Each gene specifies information such as:
 - angle

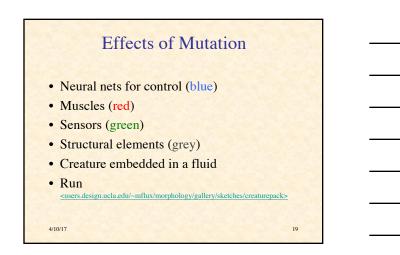
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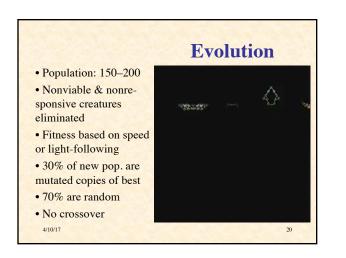
- distance
- type of cell
- how many times to replicate
- following gene
- Cells connected by "springs"
- Run phenome: <users.design.ucla.edu/~mflux/morphology/gallery/sketches/phenome>

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Complete Creature

- Neural nets for control (blue) – integrate-and-fire neurons
- Muscles (red)
- Decrease "spring length" when fire
- Sensors (green)
 - fire when exposed to "light"
- Structural elements (grey)
 anchor other cells together
- Creature embedded in a fluid
- Run <users.design.ucla.edu/~mflux/morphology/gallery/sketches/creature> 4/10/17





Gallery of Evolved Creatures







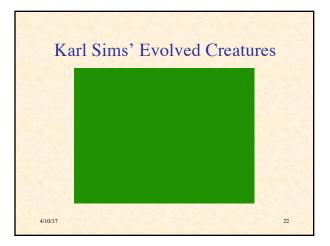
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- Selected for speed of movement
- Run

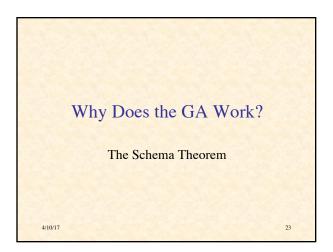
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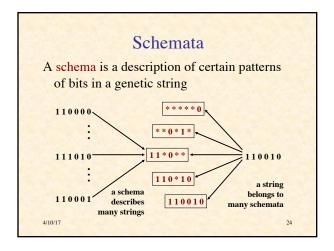
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The Fitness of Schemata

- The schemata are the building blocks of solutions
- We would like to know the average fitness of all possible strings belonging to a schema
- We cannot, but the strings in a population that belong to a schema give an estimate of the fitness of that schema
- Each string in a population is giving information about all the schemata to which it belongs (implicit parallelism)

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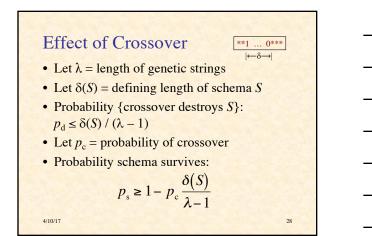
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Effect of Selection

Let n = size of populationLet m(S,t) = number of instances of schema S at time tString i gets picked with probability $\frac{f_i}{\sum_j f_j}$ Let f(S) = avg fitness of instances of S at time tSo expected $m(S,t+1) = m(S,t) \cdot n \cdot \frac{f(S)}{\sum_j f_j}$ Since $f_{av} = \frac{\sum_j f_j}{n}$, $m(S,t+1) = m(S,t) \frac{f(S)}{f_{av}}$ 40007 26

Exponential Growth

- We have discovered: $m(S, t+1) = m(S, t) \cdot f(S) / f_{av}$
- Suppose $f(S) = f_{av} (1 + c)$
- Then $m(S, t) = m(S, 0) (1 + c)^t$
- That is, exponential growth in aboveaverage schemata



Selection & Crossover Together

$$m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{av}} \left[1 - p_c \frac{\delta(S)}{\lambda - 1} \right]$$
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Effect of Mutation

- Let $p_{\rm m}$ = probability of mutation
- So $1 p_m =$ probability an allele survives
- Let o(S) = number of fixed positions in S

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- The probability they all survive is $(1 - p_m)^{o(S)}$
- If $p_{\rm m} \ll 1$, $(1 p_{\rm m})^{o(S)} \approx 1 o(S) p_{\rm m}$

Schema Theorem: "Fundamental Theorem of GAs" $m(S,t+1) \ge m(S,t) \frac{f(S)}{f_{av}} \left[1 - p_c \frac{\delta(S)}{\lambda - 1} - o(S) p_m \right]$ 4707

The Bandit Problem

- Two-armed bandit:
 - random payoffs with (unknown) means m_1, m_2 and variances σ_1^2, σ_2^2
 - optimal strategy: allocate exponentially greater number of trials to apparently better lever
- *k*-armed bandit: similar analysis applies
- Analogous to allocation of population to schemata
- Suggests GA may allocate trials optimally

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Goldberg's Analysis of Competent & Efficient GAs

Paradox of GAs

- Individually uninteresting operators: – selection, recombination, mutation
- Selection + mutation ⇒ continual improvement
- Selection + recombination ⇒ innovation
 fundamental to invention: generation vs. evaluation

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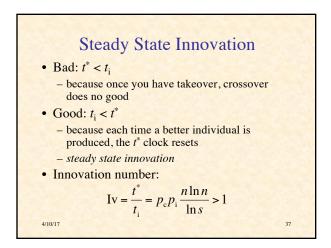
Fundamental intuition of GAs: the three work well together

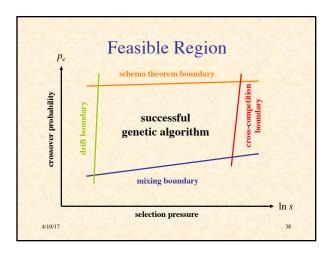
- Race Between Selection & Innovation: Takeover Time
- Takeover time *t*^{*} = average time for most fit to take over population
- Transaction selection: population replaced by *s* copies of top 1/*s*
- s quantifies selective pressure
- Estimate $t^* \approx \ln n / \ln s$
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Innovation Time

- Innovation time t_i = average time to get a better individual through crossover & mutation
- Let p_i = probability a single crossover produces a better individual
- Number of individuals undergoing crossover = $p_c n$
- Number of probable improvements = $p_i p_c n$
- Estimate: $t_i \approx 1 / (p_c p_i n)$





Other Algorithms Inspired by Genetics and Evolution

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- Evolutionary Programming

 natural representation, no crossover, time-varying continuous mutation
- Evolutionary Strategies
 - similar, but with a kind of recombination
- Genetic Programming
- like GA, but program trees instead of strings
- Classifier Systems
 - GA + rules + bids/payments
- and many variants & combinations...

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Additional Bibliography

- 1. Goldberg, D.E. *The Design of Innovation: Lessons from and for Competent Genetic Algorithms*. Kluwer, 2002.
- 2. Milner, R. *The Encyclopedia of Evolution*. Facts on File, 1990.

