

$$v_i(t) / R_1 = -C_1 v'_{o1}(t) \quad , \quad v_{o1}(t) / R_2 = -C_2 v'_o(t) - v_o(t) / R_f$$

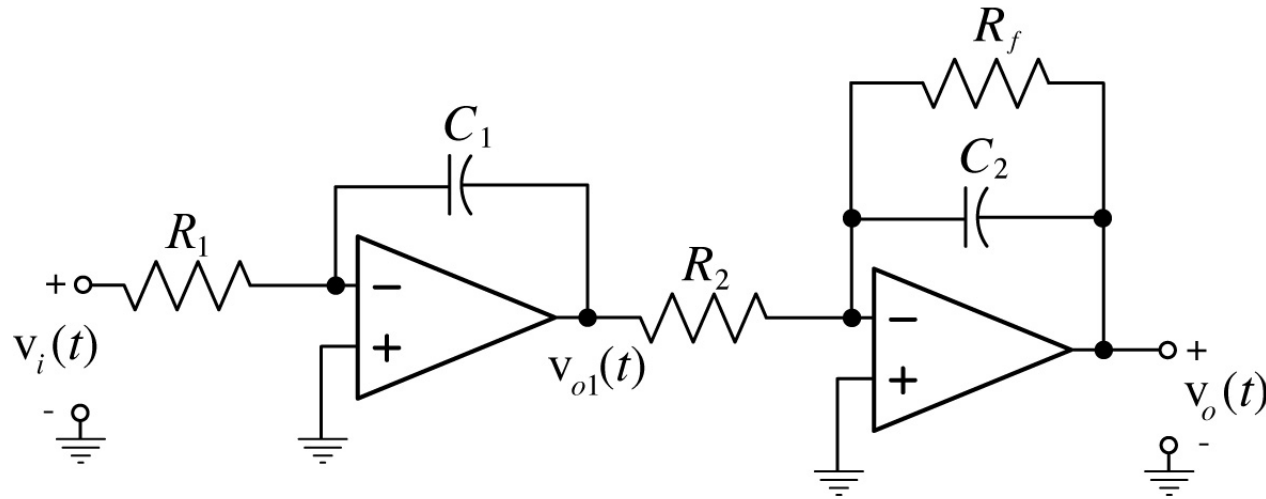
$$v_{o1}(t) = -R_2 C_2 v'_o(t) - v_o(t) R_2 / R_f$$

$$v'_{o1}(t) = -R_2 C_2 v''_o(t) - v'_o(t) R_2 / R_f$$

$$v_i(t) / R_1 = -C_1 \left[-R_2 C_2 v''_o(t) - v'_o(t) R_2 / R_f \right]$$

$$R_1 R_2 C_1 C_2 v''_o(t) + v'_o(t) R_1 C_1 R_2 / R_f = v_i(t)$$

$$v''_o(t) + \frac{v'_o(t)}{R_f C_2} = \frac{1}{R_1 R_2 C_1 C_2} v_i(t)$$



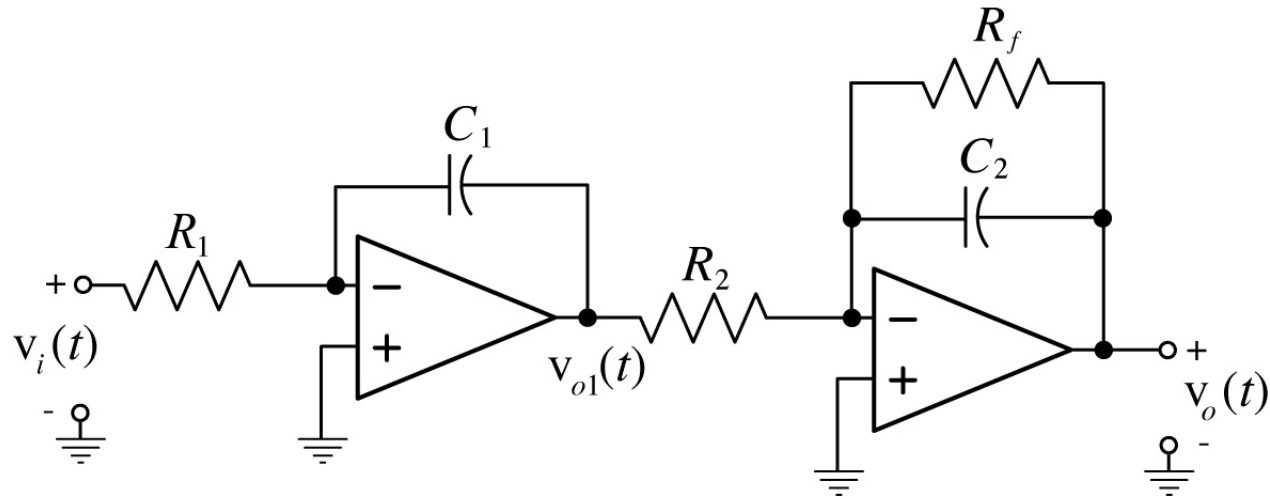
$$v_i(t)/R_1 = -C_1 v'_{o1}(t) \quad , \quad v_{o1}(t)/R_2 = -C_2 v'_o(t) - v_o(t)/R_f$$

$$v''_o(t) + \frac{v'_o(t)}{R_f C_2} = \frac{1}{R_1 R_2 C_1 C_2} v_i(t)$$

$$s^2 V_o(s) - s v_o(0^-) - \left(\frac{d}{dt} (v_o(t)) \right)_{t=0^-} + \frac{1}{R_f C_2} (s V_o(s) - v_o(0^-)) = \frac{1}{R_1 R_2 C_1 C_2} V_i(s)$$

$$\text{Let } v_o(0^-) = 0 \text{ and } \left(\frac{d}{dt} (v_o(t)) \right)_{t=0^-} = 0 \text{ and } V_i(s) = 1/s.$$

$$s^2 V_o(s) + \frac{s V_o(s)}{R_f C_2} = \frac{1}{s R_1 R_2 C_1 C_2} \Rightarrow V_o(s) = \frac{1}{R_1 R_2 C_1 C_2} \times \frac{1}{s^2 (s + 1/R_f C_2)}$$



$$V_o(s) = \frac{1}{R_1 R_2 C_1 C_2} \times \frac{1}{s^2 (s + 1/R_f C_2)}$$

Let $R_1 = 10 \text{ k}\Omega$, $R_2 = 1 \text{ k}\Omega$, $C_1 = 20 \text{ nF}$, $C_2 = 50 \text{ nF}$, $R_f = 20 \text{ k}\Omega$

$$V_o(s) = \frac{10^8}{s^2 (s + 1000)} = 100 \left[\frac{1000}{s^2} - \frac{1}{s} + \frac{1}{s + 1000} \right]$$

$$v_o(t) = 100 \left[1000 \text{ramp}(t) - (1 - e^{-1000t})u(t) \right]$$