## Solution of ECE 300 Test 7 S12

1. Fill in the blanks with correct numbers.







At  $t = 0^-$ , the switch is open, the capacitor is equivalent to an open circuit and all the  $I_s$  current flows through the three resistors counterclockwise. The voltage across the capacitor is  $i_2 R_2 = -I_s R_2$  and does not change instantaneously when the switch is closed. So at  $t = 0^+$  the switch is closed and the capacitor voltage and the current  $i_2$  stay the same. The resistor  $R_1$  is now in parallel with the capacitor so  $v_1 = -v_c$  and  $i_1 = v_1/R_1$ . The voltage across  $R_3$  stays the same because it is in series with a current source that is constant. The time constant is  $\tau = R_{eq}C$  where  $R_{eq} = R_1 \parallel R_2$ .

$$i_{1}(0^{-}) = -2 \text{ mA} \qquad i_{2}(0^{-}) = -2 \text{ mA} \qquad i_{c}(0^{-}) = 0 \text{ mA}$$
$$v_{1}(0^{-}) = -4.6 \text{ V} \qquad v_{c}(0^{-}) = -3.6 \text{ V} \qquad v_{3}(0^{-}) = 1.8 \text{ V}$$
$$i_{1}(0^{+}) = 1.5652 \text{ mA} \qquad i_{2}(0^{+}) = -2 \text{ mA} \qquad i_{c}(0^{+}) = 3.5652 \text{ mA}$$
$$v_{1}(0^{+}) = 3.6 \text{ V} \qquad v_{c}(0^{+}) = -3.6 \text{ V} \qquad v_{3}(0^{+}) = 1.8 \text{ V}$$

For t > 0, the time constant  $\tau$  is 22.2 ms.

2. Fill in the blanks with correct numbers.

$$\begin{array}{c} i_{1}(0^{-}) = \underline{\qquad} & mA \quad i_{2}(0^{-}) = \underline{\qquad} & mA \quad i_{L}(0^{-}) = \underline{\qquad} & mA \\ v_{1}(0^{-}) = \underline{\qquad} & V \quad v_{L}(0^{-}) = \underline{\qquad} & V \quad v_{ds}(0^{-}) = \underline{\qquad} & V \\ i_{1}(0^{+}) = \underline{\qquad} & mA \quad i_{2}(0^{+}) = \underline{\qquad} & mA \quad i_{L}(0^{+}) = \underline{\qquad} & mA \\ v_{1}(0^{+}) = \underline{\qquad} & V \quad v_{L}(0^{+}) = \underline{\qquad} & V \quad v_{ds}(0^{+}) = \underline{\qquad} & V \\ \end{array}$$





At  $t = 0^-$ , the switch is closed, the inductor is equivalent to a short circuit so the voltage across it is zero, making the voltage across  $R_2$  zero, making the current  $i_2$  zero, making the current  $ki_2$  also zero. So  $v_1 = V_s$  and the current through both  $R_1$  and the inductor is  $V_s / R_1$ . At  $t = 0^+$ ,  $i_L + i_2 = ki_2$  (because the switch is now open) therefore  $i_2 = \frac{i_L}{k-1}$ . The currents  $ki_2$  and  $i_1$  are the same and  $v_1 = i_1 R_1$ . Also  $v_L = i_2 R_2$  and  $v_{ds} = v_L + v_1$ . For t > 0, the equivalent resistance in parallel with the inductor is the Thevenin equivalent resistance of the network formed by the two resistors and the dependent source. Applying a 1 V test source at the load terminals of that network the current  $i_s$  flowing into the network is set by  $i_2 = ki_2 + i_s$  and  $i_2 = 1/R_2$ . Solving,  $i_s = (1-k)/R_2$ and  $R_{eq} = R_2 / (1-k)$  and  $\tau = L / R_{eq} = (1-k)L / R_2$ .

$$i_{1}(0^{-}) = 2.2642 \text{ mA} \qquad i_{2}(0^{-}) = 0 \text{ mA} \qquad i_{L}(0^{-}) = 2.2642 \text{ mA}$$
$$v_{1}(0^{-}) = 12 \text{ V} \qquad v_{L}(0^{-}) = 0 \text{ V} \qquad v_{ds}(0^{-}) = 12 \text{ V}$$
$$i_{1}(0^{+}) = -3.3962 \text{ mA} \qquad i_{2}(0^{+}) = -5.6604 \text{ mA} \qquad i_{L}(0^{+}) = 2.2642 \text{ mA}$$
$$v_{1}(0^{+}) = -18 \text{ V} \qquad v_{L}(0^{+}) = -49.8115 \text{ V} \qquad v_{ds}(0^{+}) = -67.8115 \text{ V}$$

For t > 0, the time constant  $\tau$  is 1.091  $\mu$ s.

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At  $t = 0^-$ , the switch is open, the capacitor is equivalent to an open circuit and all the  $I_s$  current flows through the three resistors counterclockwise. The voltage across the capacitor is  $i_2 R_2 = -I_s R_2$  and does not change instantaneously when the switch is closed. So at  $t = 0^+$  the switch is closed and the capacitor voltage and the current  $i_2$  stay the same. The resistor  $R_1$  is now in parallel with the capacitor so  $v_1 = -v_c$  and  $i_1 = v_1/R_1$ . The voltage across  $R_3$  stays the same because it is in series with a current source that is constant. The time constant is  $\tau = R_{eq}C$  where  $R_{eq} = R_1 \parallel R_2$ .

$$i_{1}(0^{-}) = -1 \text{ mA} \qquad i_{2}(0^{-}) = -1 \text{ mA} \qquad i_{C}(0^{-}) = 0 \text{ mA}$$
$$v_{1}(0^{-}) = -2.3 \text{ V} \qquad v_{C}(0^{-}) = -1.8 \text{ V} \qquad v_{3}(0^{-}) = 0.9 \text{ V}$$
$$i_{1}(0^{+}) = 0.7826 \text{ mA} \qquad i_{2}(0^{+}) = -1 \text{ mA} \qquad i_{C}(0^{+}) = 1.7826 \text{ mA}$$
$$v_{1}(0^{+}) = 1.8 \text{ V} \qquad v_{C}(0^{+}) = -1.8 \text{ V} \qquad v_{3}(0^{+}) = 0.9 \text{ V}$$

For t > 0, the time constant  $\tau$  is 47.43 ms.

2. Fill in the blanks with correct numbers.

$$\begin{array}{c} i_{1}(0^{-}) = \underline{\qquad} & mA \quad i_{2}(0^{-}) = \underline{\qquad} & mA \quad i_{L}(0^{-}) = \underline{\qquad} & mA \\ v_{1}(0^{-}) = \underline{\qquad} & V \quad v_{L}(0^{-}) = \underline{\qquad} & V \quad v_{ds}(0^{-}) = \underline{\qquad} & V \\ i_{1}(0^{+}) = \underline{\qquad} & mA \quad i_{2}(0^{+}) = \underline{\qquad} & mA \quad i_{L}(0^{+}) = \underline{\qquad} & mA \\ v_{1}(0^{+}) = \underline{\qquad} & V \quad v_{L}(0^{+}) = \underline{\qquad} & V \quad v_{ds}(0^{+}) = \underline{\qquad} & V \\ \end{array}$$





At  $t = 0^-$ , the switch is closed, the inductor is equivalent to a short circuit so the voltage across it is zero, making the voltage across  $R_2$  zero, making the current  $i_2$  zero, making the current  $ki_2$  also zero. So  $v_1 = V_s$  and the current through both  $R_1$  and the inductor is  $V_s / R_1$ . At  $t = 0^+$ ,  $i_L + i_2 = ki_2$  (because the switch is now open) therefore  $i_2 = \frac{i_L}{k-1}$ . The currents  $ki_2$  and  $i_1$  are the same and  $v_1 = i_1 R_1$ . Also  $v_L = i_2 R_2$  and  $v_{ds} = v_L + v_1$ . For t > 0, the equivalent resistance in parallel with the inductor is the Thevenin equivalent resistance of the network formed by the two resistors and the dependent source. Applying a 1 V test source at the load terminals of that network the current  $i_s$  flowing into the network is set by  $i_2 = ki_2 + i_s$  and  $i_2 = 1/R_2$ . Solving,  $i_s = (1-k)/R_2$ and  $R_{eq} = R_2 / (1-k)$  and  $\tau = L / R_{eq} = (1-k)L / R_2$ .

$$i_{1}(0^{-}) = 4.5284 \text{ mA} \qquad i_{2}(0^{-}) = 0 \text{ mA} \qquad i_{L}(0^{-}) = 4.5284 \text{ mA}$$
$$v_{1}(0^{-}) = 24 \text{ V} \qquad v_{L}(0^{-}) = 0 \text{ V} \qquad v_{ds}(0^{-}) = 24 \text{ V}$$
$$i_{1}(0^{+}) = -6.7924 \text{ mA} \qquad i_{2}(0^{+}) = -11.3208 \text{ mA} \qquad i_{L}(0^{+}) = 4.5284 \text{ mA}$$
$$v_{1}(0^{+}) = -36 \text{ V} \qquad v_{L}(0^{+}) = -99.623 \text{ V} \qquad v_{ds}(0^{+}) = -135.623 \text{ V}$$

For t > 0, the time constant  $\tau$  is 0.5455  $\mu$ s.

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At  $t = 0^-$ , the switch is open, the capacitor is equivalent to an open circuit and all the  $I_s$  current flows through the three resistors counterclockwise. The voltage across the capacitor is  $i_2 R_2 = -I_s R_2$  and does not change instantaneously when the switch is closed. So at  $t = 0^+$  the switch is closed and the capacitor voltage and the current  $i_2$  stay the same. The resistor  $R_1$  is now in parallel with the capacitor so  $v_1 = -v_c$  and  $i_1 = v_1/R_1$ . The voltage across  $R_3$  stays the same because it is in series with a current source that is constant. The time constant is  $\tau = R_{eq}C$  where  $R_{eq} = R_1 \parallel R_2$ .

$$i_{1}(0^{-}) = -4 \text{ mA} \qquad i_{2}(0^{-}) = -4 \text{ mA} \qquad i_{C}(0^{-}) = 0 \text{ mA}$$
$$v_{1}(0^{-}) = -9.2 \text{ V} \qquad v_{C}(0^{-}) = -7.2 \text{ V} \qquad v_{3}(0^{-}) = 3.6 \text{ V}$$
$$i_{1}(0^{+}) = 3.1304 \text{ mA} \qquad i_{2}(0^{+}) = -4 \text{ mA} \qquad i_{C}(0^{+}) = 7.1304 \text{ mA}$$
$$v_{1}(0^{+}) = 7.2 \text{ V} \qquad v_{C}(0^{+}) = -7.2 \text{ V} \qquad v_{3}(0^{+}) = 3.6 \text{ V}$$

For t > 0, the time constant  $\tau$  is 44.4 ms.

2. Fill in the blanks with correct numbers.

$$\begin{array}{c} i_{1}(0^{-}) = \underline{\qquad} & mA \quad i_{2}(0^{-}) = \underline{\qquad} & mA \quad i_{L}(0^{-}) = \underline{\qquad} & mA \\ v_{1}(0^{-}) = \underline{\qquad} & V \quad v_{L}(0^{-}) = \underline{\qquad} & V \quad v_{ds}(0^{-}) = \underline{\qquad} & V \\ i_{1}(0^{+}) = \underline{\qquad} & mA \quad i_{2}(0^{+}) = \underline{\qquad} & mA \quad i_{L}(0^{+}) = \underline{\qquad} & mA \\ v_{1}(0^{+}) = \underline{\qquad} & V \quad v_{L}(0^{+}) = \underline{\qquad} & V \quad v_{ds}(0^{+}) = \underline{\qquad} & V \\ \end{array}$$





At  $t = 0^-$ , the switch is closed, the inductor is equivalent to a short circuit so the voltage across it is zero, making the voltage across  $R_2$  zero, making the current  $i_2$  zero, making the current  $ki_2$  also zero. So  $v_1 = V_s$  and the current through both  $R_1$  and the inductor is  $V_s / R_1$ . At  $t = 0^+$ ,  $i_L + i_2 = ki_2$  (because the switch is now open) therefore  $i_2 = \frac{i_L}{k-1}$ . The currents  $ki_2$  and  $i_1$  are the same and  $v_1 = i_1 R_1$ . Also  $v_L = i_2 R_2$  and  $v_{ds} = v_L + v_1$ . For t > 0, the equivalent resistance in parallel with the inductor is the Thevenin equivalent resistance of the network formed by the two resistors and the dependent source. Applying a 1 V test source at the load terminals of that network the current  $i_s$  flowing into the network is set by  $i_2 = ki_2 + i_s$  and  $i_2 = 1/R_2$ . Solving,  $i_s = (1-k)/R_2$ and  $R_{eq} = R_2 / (1-k)$  and  $\tau = L / R_{eq} = (1-k)L / R_2$ .

$$i_{1}(0^{-}) = 1.1321 \text{ mA} \qquad i_{2}(0^{-}) = 0 \text{ mA} \qquad i_{L}(0^{-}) = 1.1321 \text{ mA}$$
$$v_{1}(0^{-}) = 6 \text{ V} \qquad v_{L}(0^{-}) = 0 \text{ V} \qquad v_{ds}(0^{-}) = 6 \text{ V}$$
$$i_{1}(0^{+}) = -1.6981 \text{ mA} \qquad i_{2}(0^{+}) = -2.8302 \text{ mA} \qquad i_{L}(0^{+}) = 1.1321 \text{ mA}$$
$$v_{1}(0^{+}) = -9 \text{ V} \qquad v_{L}(0^{+}) = -24.4058 \text{ V} \qquad v_{ds}(0^{+}) = -33.9057 \text{ V}$$

For t > 0, the time constant  $\tau$  is 2.182  $\mu$ s.