

Solution of ECE 300 Test 9 F11

1. Reduce each expression to a complex number in polar form with an angle in the range -180° to $+180^\circ$. (Remember, the polar form is magnitude-angle and the magnitude cannot be negative.)

(a) $(5\angle 100^\circ)^4 = 625\angle 400^\circ = 625\angle 40^\circ$

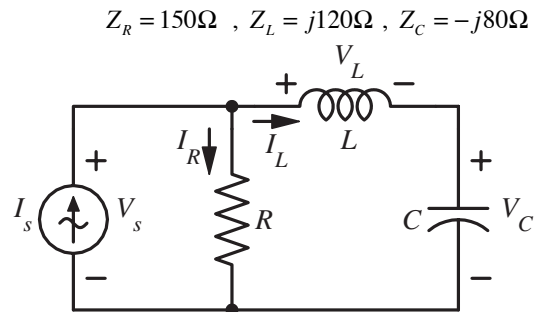
(b) $\frac{1}{-10 + j7} = \frac{1}{12.207\angle 145^\circ} = 0.0819\angle -145^\circ$

2. If $v_1(t) = 9\cos(200\pi t + 30^\circ)$ and $v_2(t) = 18\sin(200\pi t - 110^\circ)$, which sinusoid is leading and by how many degrees? (The numerical value of the angle in degrees must lie in the range -180° to $+180^\circ$.)

$$v_1(t) = 9\cos(200\pi t + 30^\circ) \quad , \quad v_2(t) = 18\cos(200\pi t - 200^\circ) = 18\cos(200\pi t + 160^\circ)$$

v_2 leads by 130°

3. In the circuit below, if $I_L = 1\angle 0^\circ$ find the numerical values of all the other phasor voltages and currents.



$$I_s = I_R + I_L = 1.035\angle 14.93^\circ \text{ A} \quad I_R = V_s / R = 0.2667\angle 90^\circ \text{ A}$$

$$V_s = V_L + V_C = j40 = 40\angle 90^\circ \text{ V} \quad V_L = Z_L I_L = j120 = 120\angle 90^\circ \text{ V} \quad V_C = Z_C I_L = -j80 = 80\angle -90^\circ \text{ V}$$

Solution of ECE 300 Test 9 F11

1. Reduce each expression to a complex number in polar form with an angle in the range -180° to $+180^\circ$. (Remember, the polar form is magnitude-angle and the magnitude cannot be negative.)

(a) $(4\angle 110^\circ)^4 = 256\angle 440^\circ = 256\angle 80^\circ$

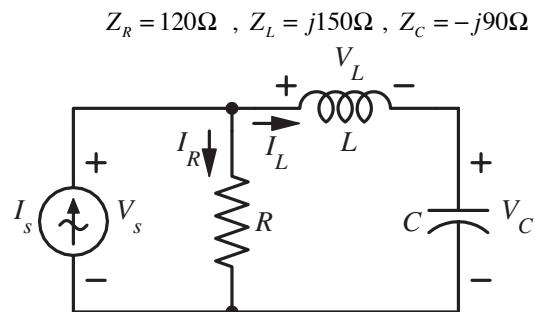
(b) $\frac{1}{-7 + j9} = \frac{1}{11.4\angle 127.88^\circ} = 0.0877\angle -127.88^\circ$

2. If $v_1(t) = 9\cos(200\pi t + 50^\circ)$ and $v_2(t) = 18\sin(200\pi t - 100^\circ)$, which sinusoid is leading and by how many degrees? (The numerical value of the angle in degrees must lie in the range -180° to $+180^\circ$.)

$$v_1(t) = 9\cos(200\pi t + 50^\circ) \quad , \quad v_2(t) = 18\cos(200\pi t - 190^\circ) = 18\cos(200\pi t + 170^\circ)$$

v_2 leads by 120°

3. In the circuit below, if $I_L = 1\angle 0^\circ$ find the numerical values of all the other phasor voltages and currents.



$$I_s = I_R + I_L = 1.118\angle 26.57^\circ \text{ A} \quad I_R = V_s / R = 0.5\angle 90^\circ \text{ A}$$

$$V_s = V_L + V_C = j60 = 60\angle 90^\circ \text{ V} \quad V_L = Z_L I_L = j150 = 150\angle 90^\circ \text{ V} \quad V_C = Z_C I_L = -j90 = 90\angle -90^\circ \text{ V}$$

Solution of ECE 300 Test 9 F11

1. Reduce each expression to a complex number in polar form with an angle in the range -180° to $+180^\circ$. (Remember, the polar form is magnitude-angle and the magnitude cannot be negative.)

(a) $(3\angle 130^\circ)^4 = 81\angle 520^\circ = 81\angle 160^\circ$

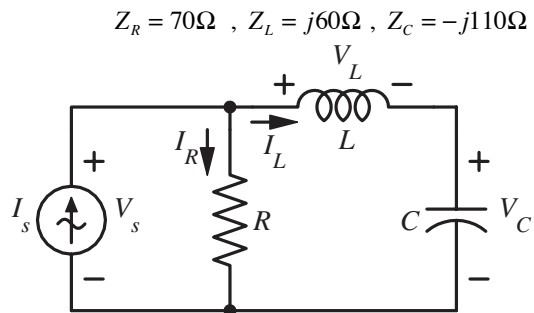
(b) $\frac{1}{-4 + j7} = \frac{1}{8.062\angle 119.74^\circ} = 0.124\angle -119.74^\circ$

2. If $v_1(t) = 9\cos(200\pi t + 20^\circ)$ and $v_2(t) = 18\sin(200\pi t - 140^\circ)$, which sinusoid is leading and by how many degrees? (The numerical value of the angle in degrees must lie in the range -180° to $+180^\circ$.)

$$v_1(t) = 9\cos(200\pi t + 20^\circ) \quad , \quad v_2(t) = 18\cos(200\pi t - 230^\circ) = 18\cos(200\pi t + 130^\circ)$$

v_2 leads by 110°

3. In the circuit below, if $I_L = 1\angle 0^\circ$ find the numerical values of all the other phasor voltages and currents.



$$I_s = I_R + I_L = 1.229\angle -35.53^\circ \text{ A} \quad I_R = V_s / R = 0.7143\angle -90^\circ \text{ A}$$

$$V_s = V_L + V_C = -j50 = 50\angle -90^\circ \text{ V} \quad V_L = Z_L I_L = j60 = 60\angle 90^\circ \text{ V} \quad V_C = Z_C I_L = -j110 = 110\angle -90^\circ \text{ V}$$